

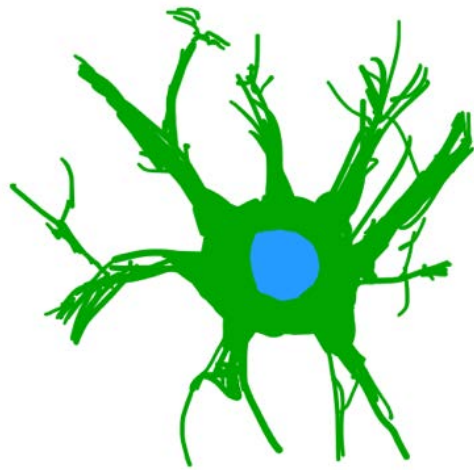
# Intro to Neural Networks

Cynthia Rudin

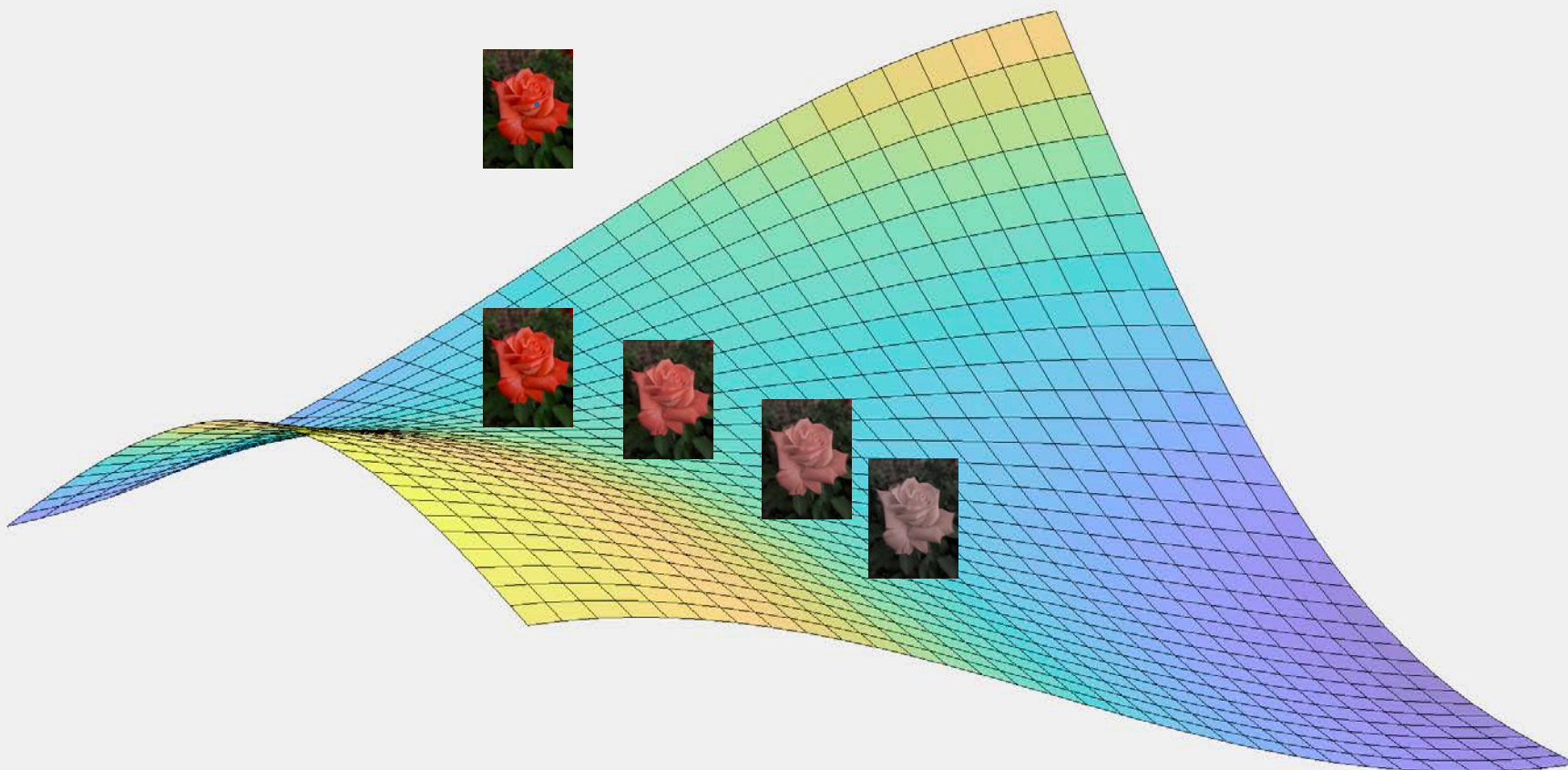
Duke Machine Learning

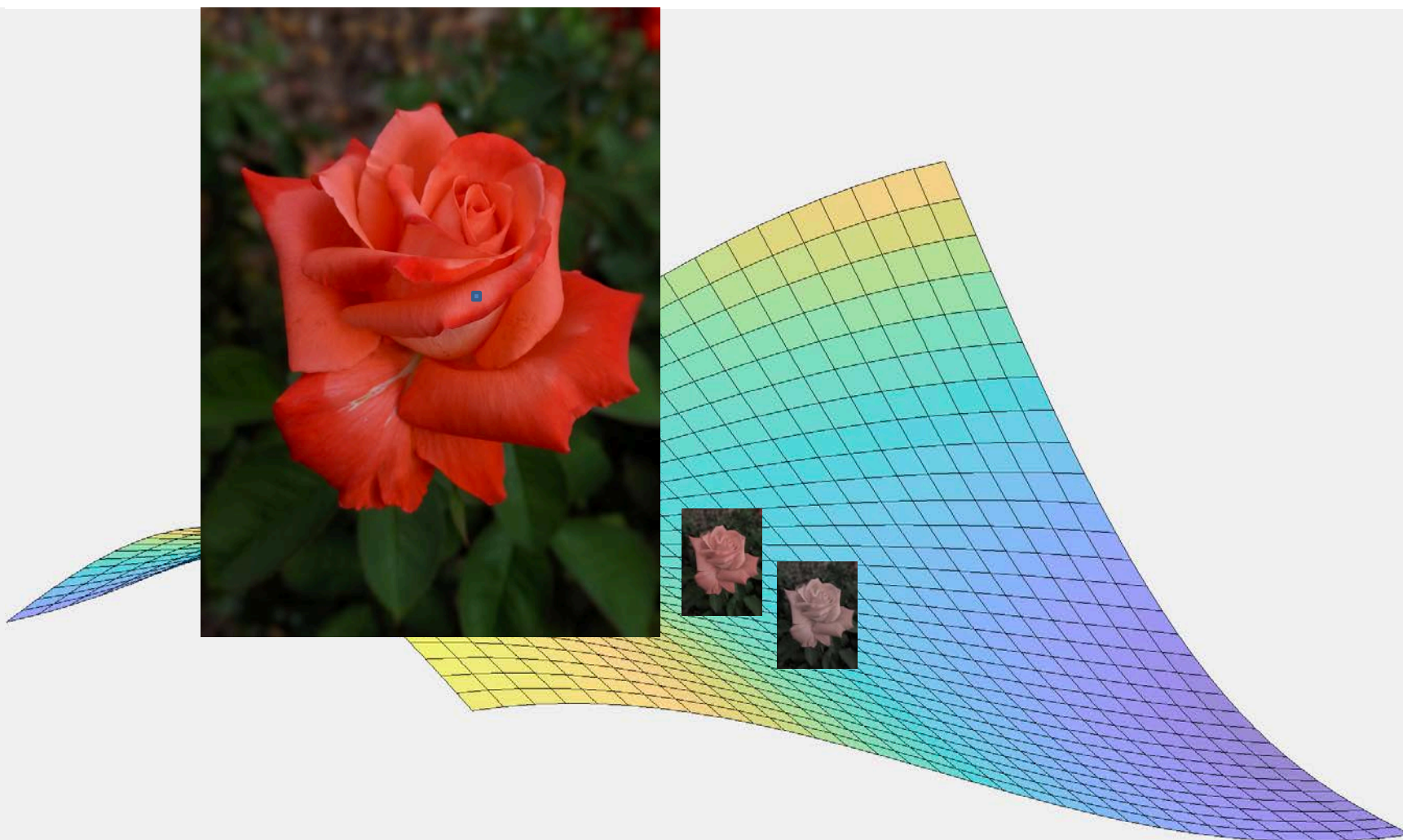
# Neurons

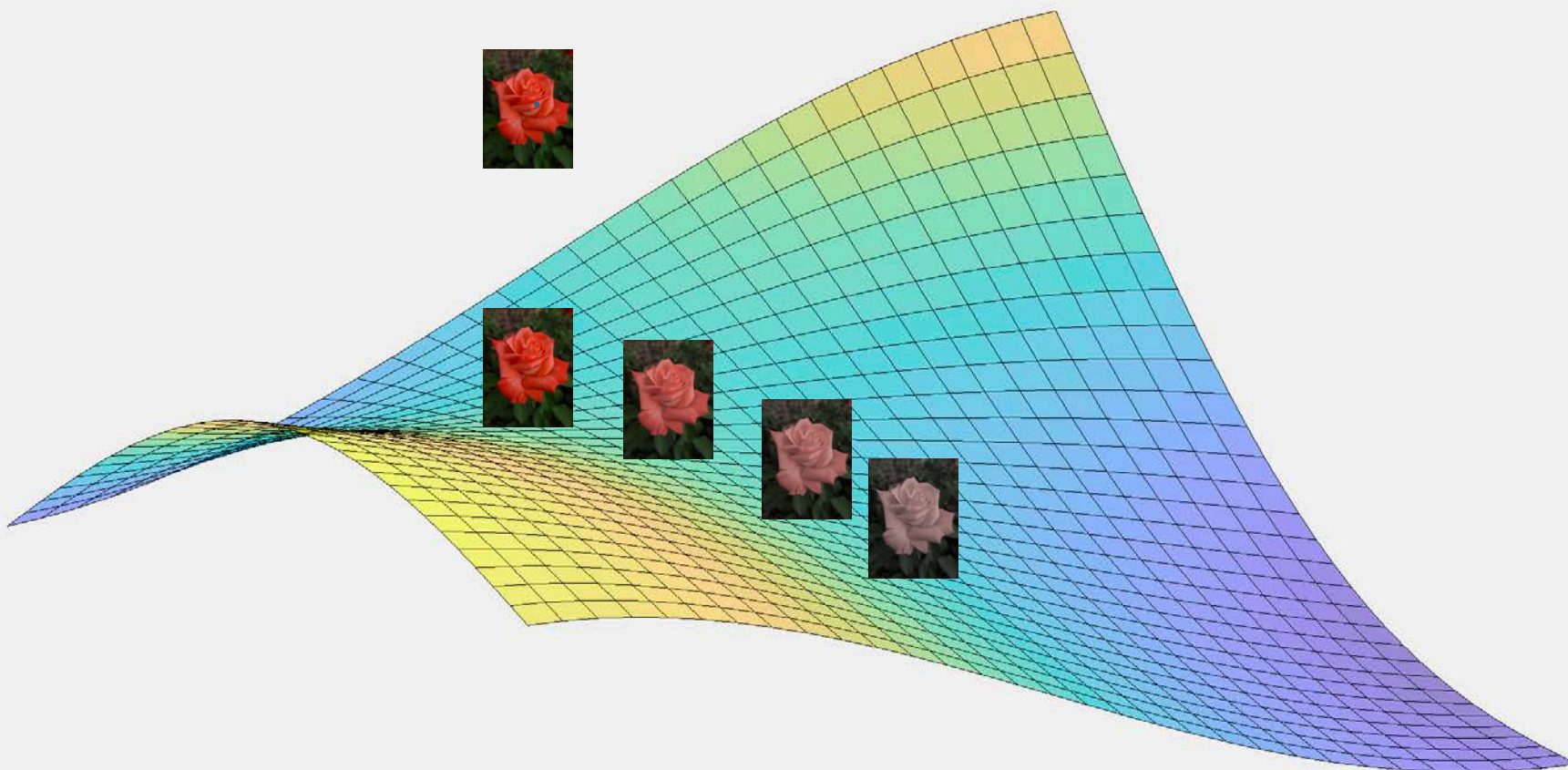
- $10^{11}$  neurons in a brain,  $10^{14}$  synapses (connections).
- Signals are electrical potential spikes that travel through the network.



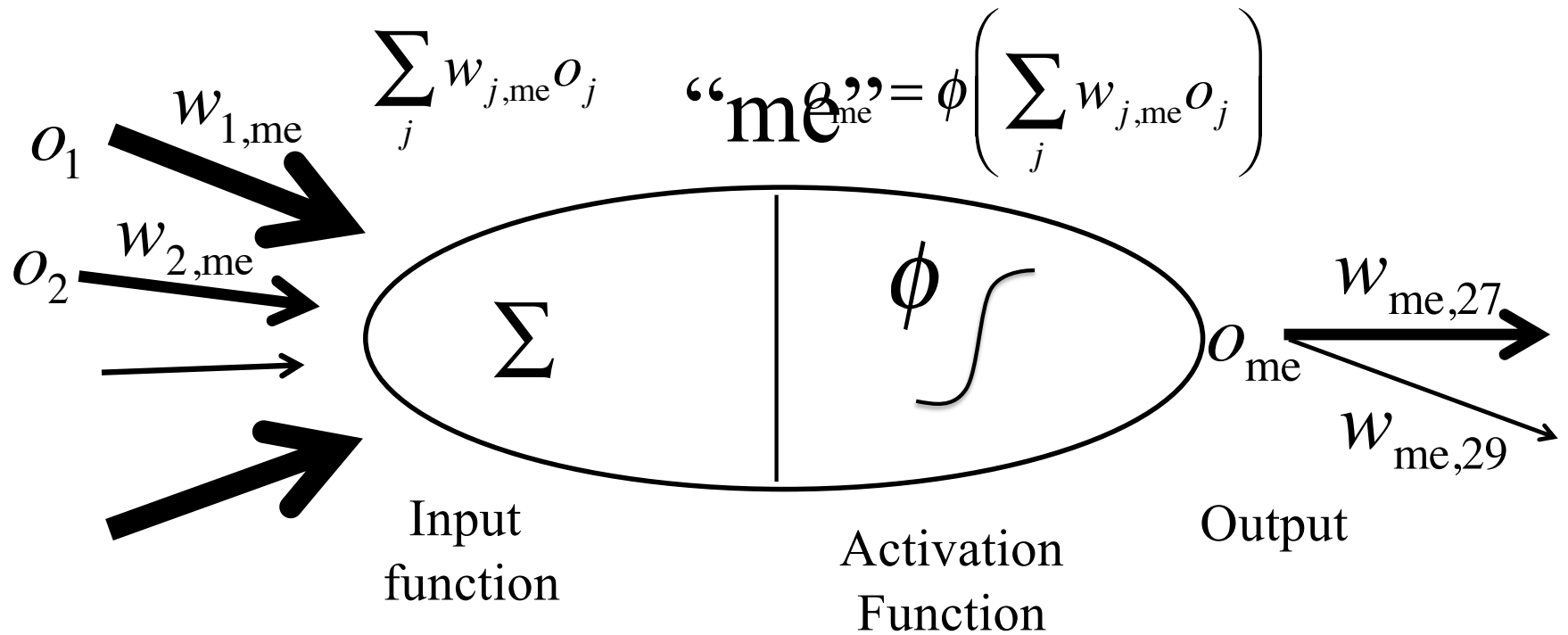
(Credit: Adapted from Russell and Norvig)



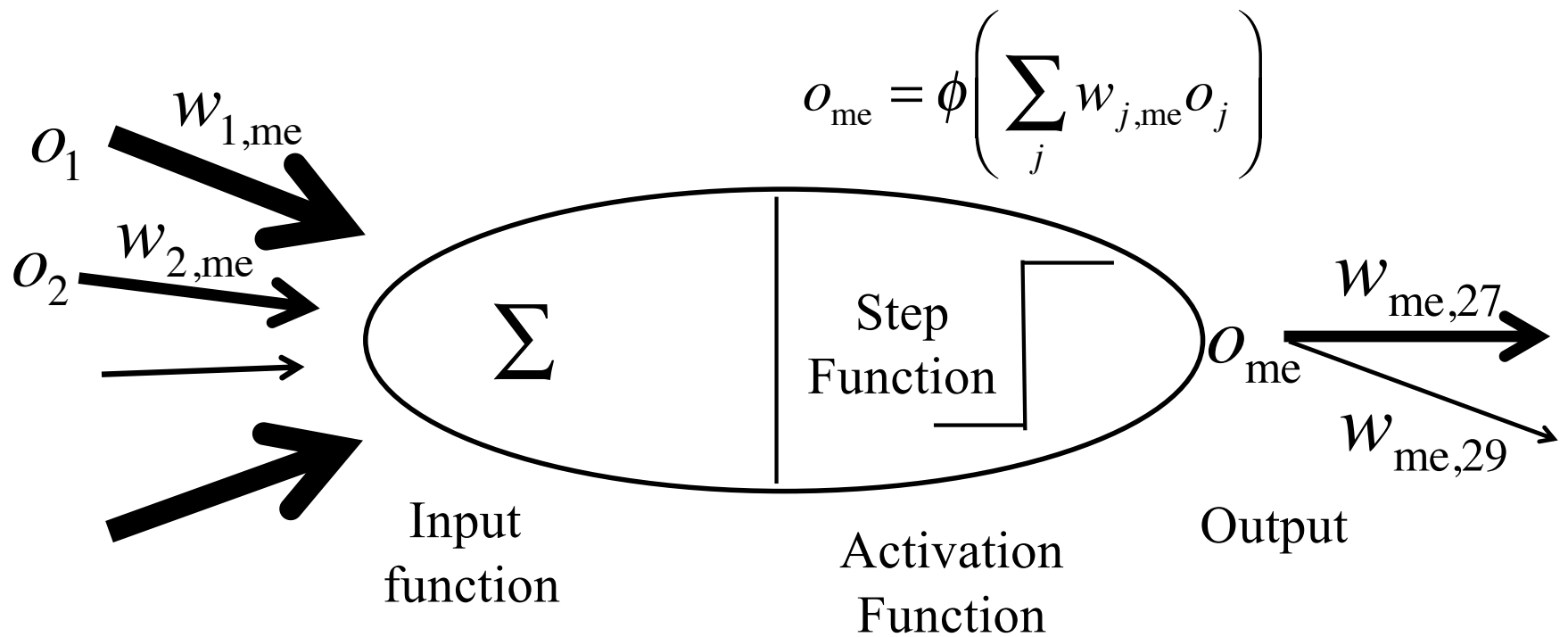




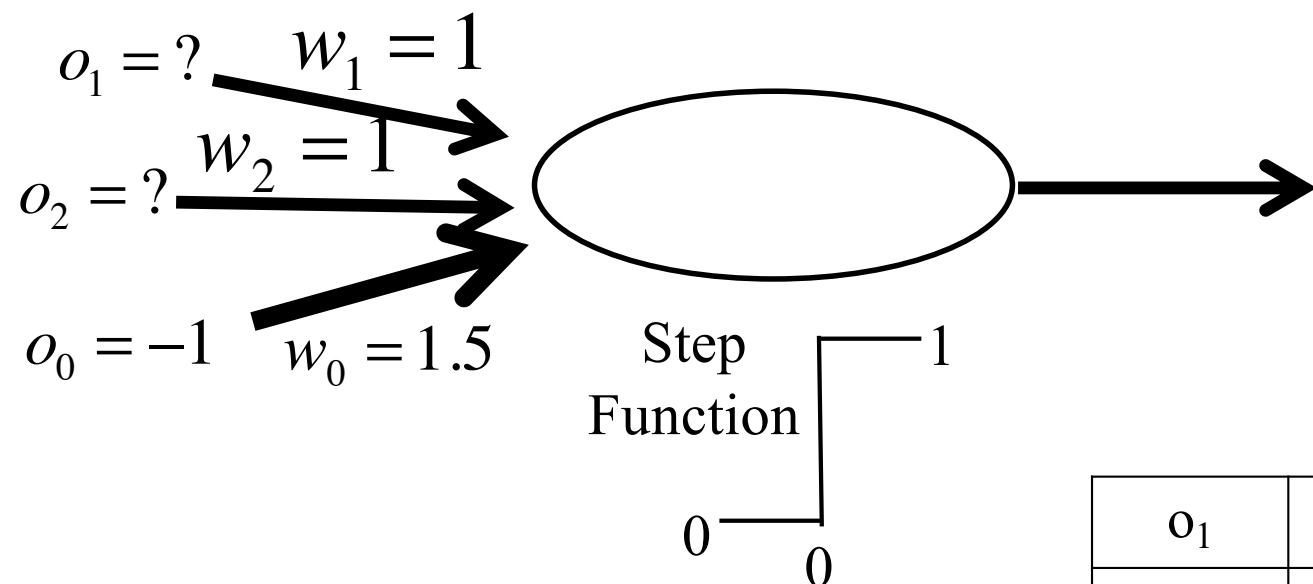
# McCulloch-Pitts “Neuron”



# McCulloch-Pitts “Neuron”



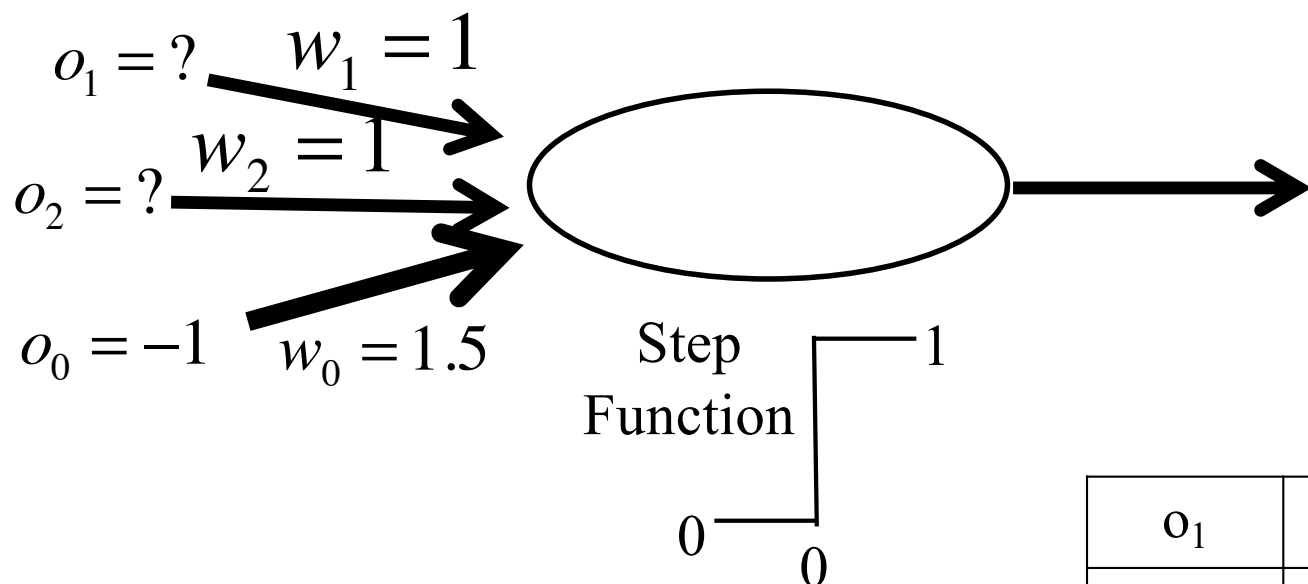
# McCulloch-Pitts “Neuron”



$o_1$	$o_2$	output



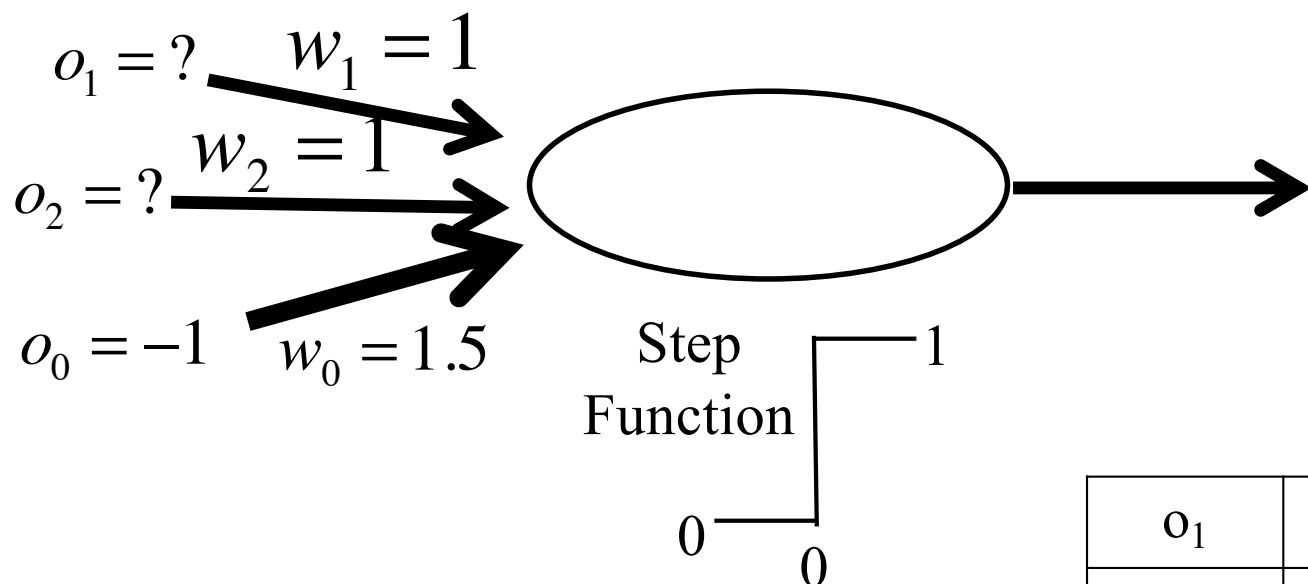
# McCulloch-Pitts “Neuron”



$$0+0-1.5 = -1.5$$

$o_1$	$o_2$	output
0	0	

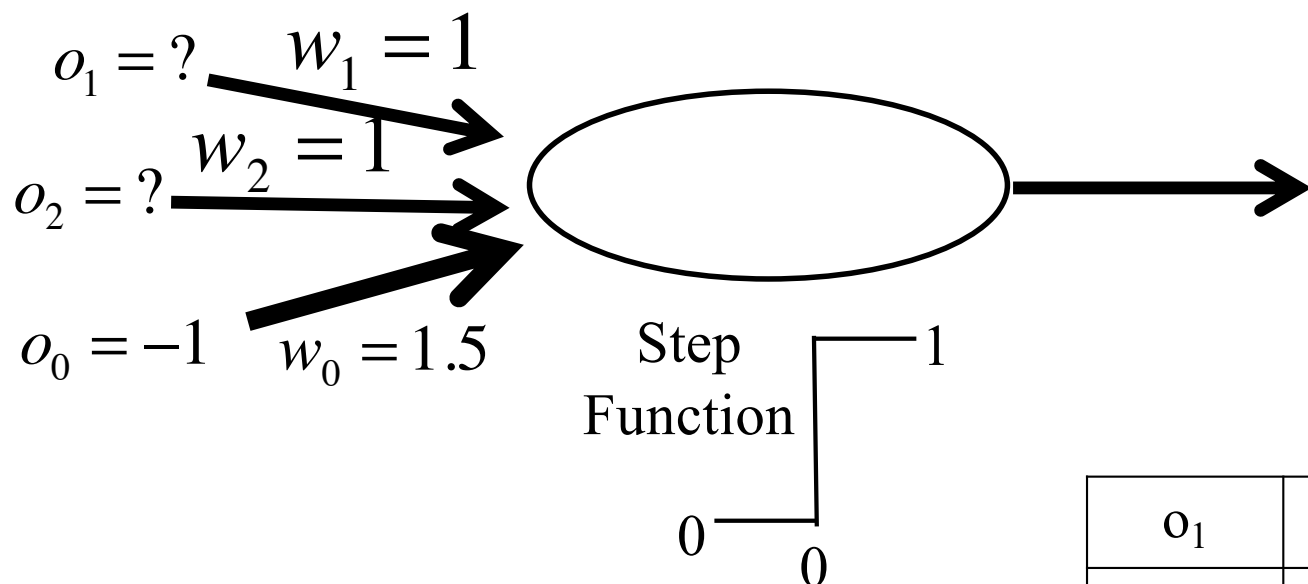
# McCulloch-Pitts “Neuron”



$$0 + 0 - 1.5 = -1.5$$

$o_1$	$o_2$	output
0	0	0

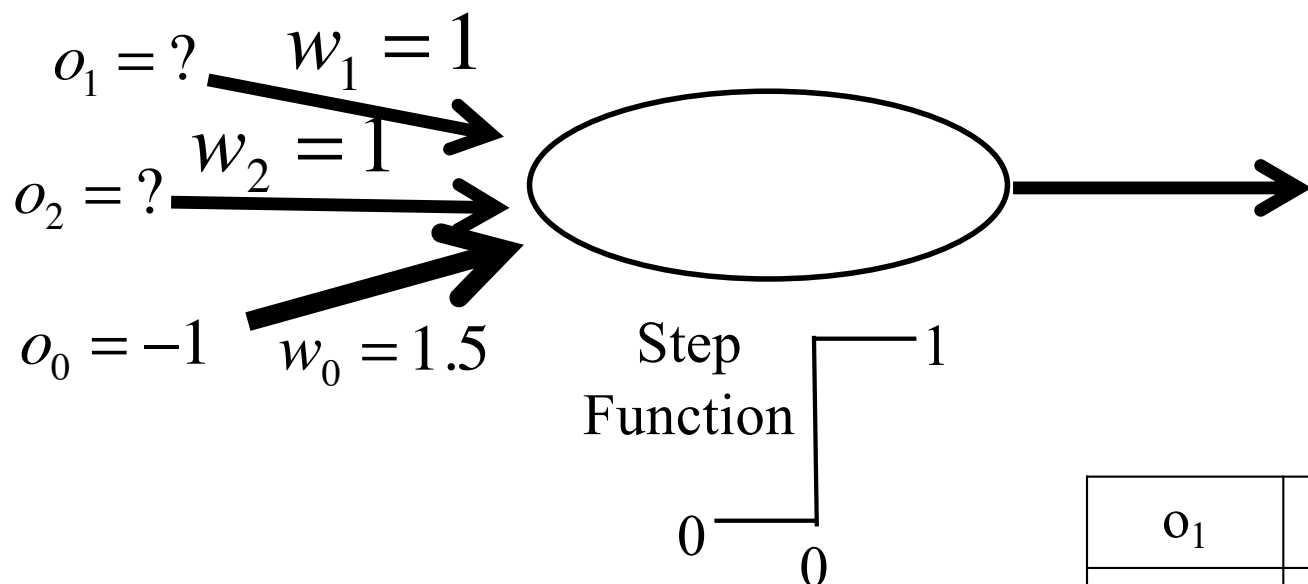
# McCulloch-Pitts “Neuron”



$$1 + 0 - 1.5 = -0.5$$

$o_1$	$o_2$	output
0	0	0
1	0	0

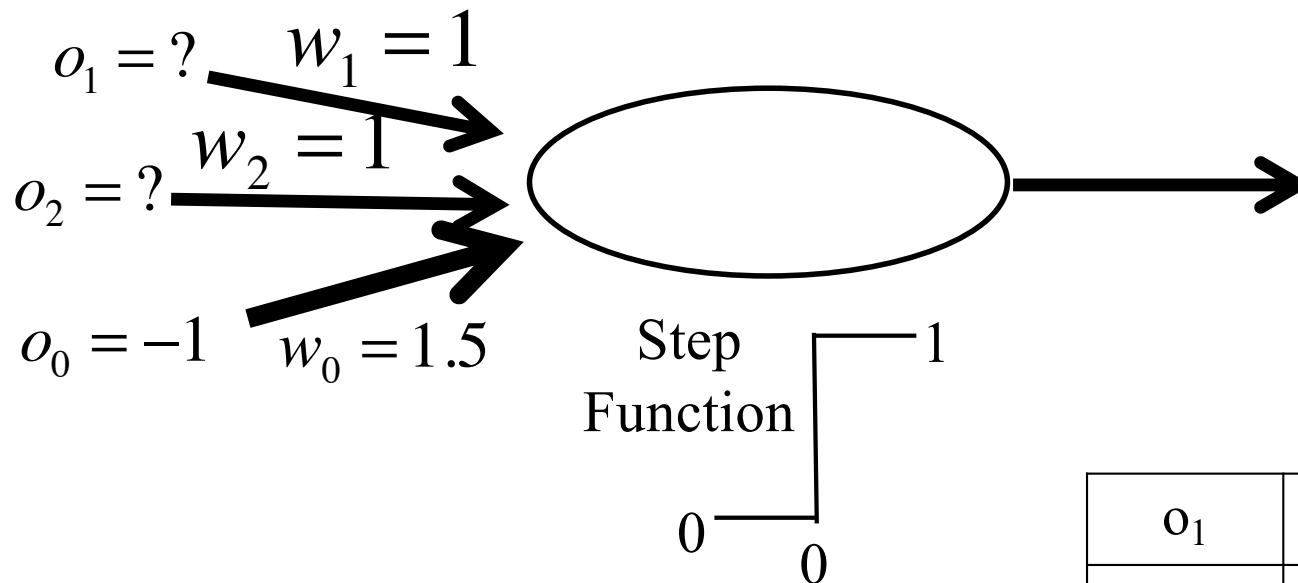
# McCulloch-Pitts “Neuron”



$$0 + 1 - 1.5 = -0.5$$

$o_1$	$o_2$	output
0	0	0
1	0	0
0	1	0

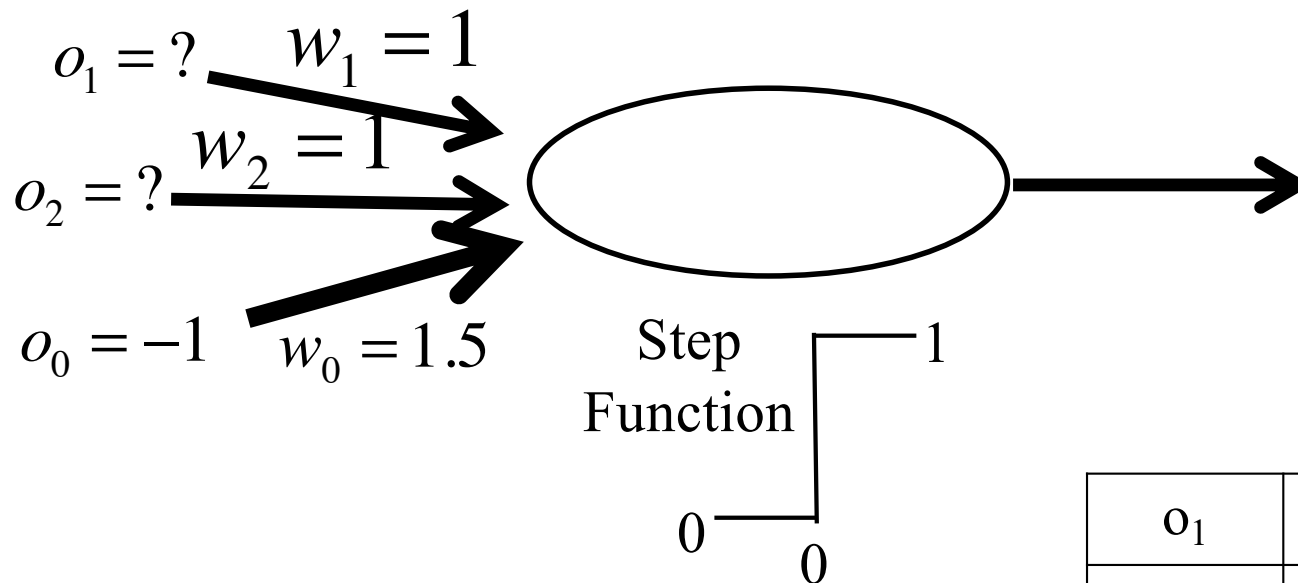
# McCulloch-Pitts “Neuron”



$$1 + 1 - 1.5 = 0.5$$

$o_1$	$o_2$	output
0	0	0
1	0	0
0	1	0
1	1	

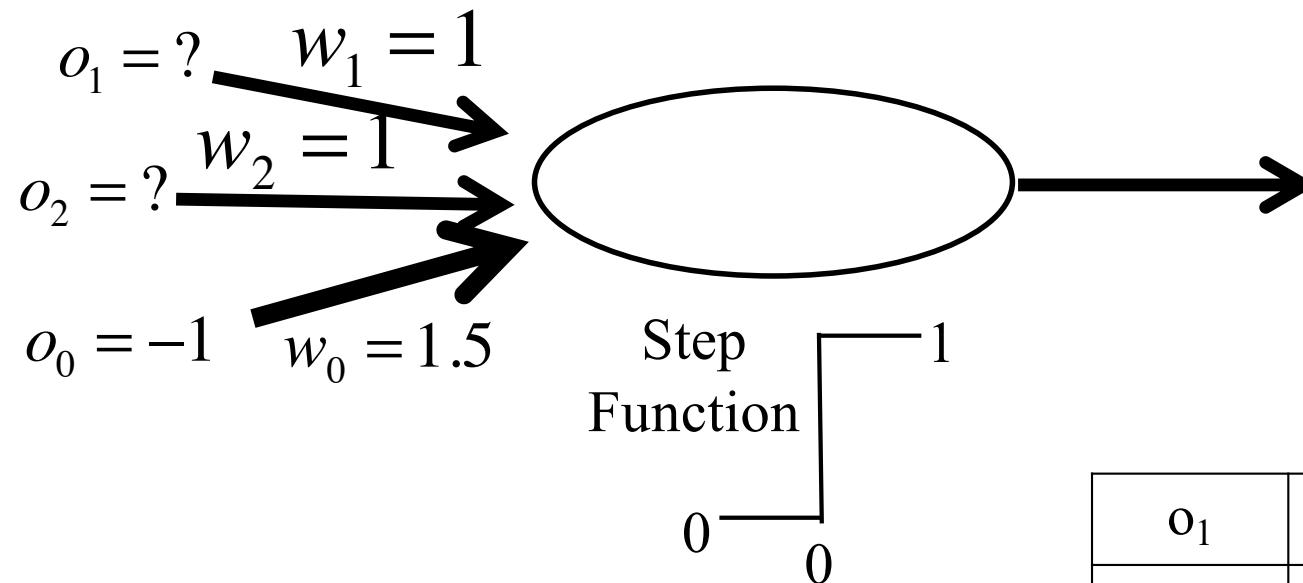
# McCulloch-Pitts “Neuron”



$$1+1-1.5 = 0.5$$

$o_1$	$o_2$	output
0	0	0
1	0	0
0	1	0
1	1	1

# McCulloch-Pitts “Neuron”



This neuron computes  
the function “and.”

There are “or” and “not” neurons too.

$o_1$	$o_2$	output
0	0	0
1	0	0
0	1	0
1	1	1

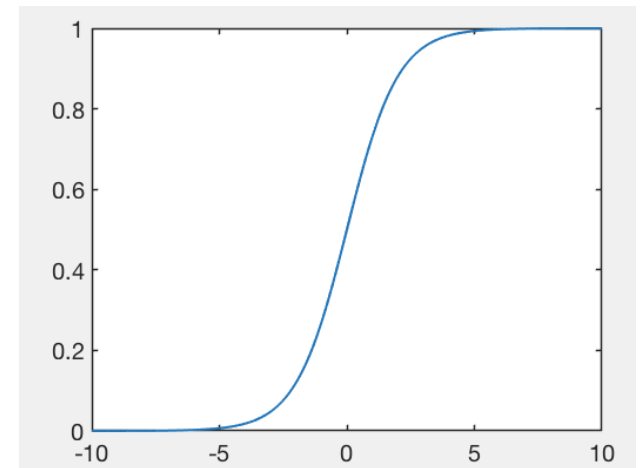
# McCulloch-Pitts “Neuron”

$$\phi\left(\sum_j w_{j,\text{me}} a_j\right) = 1 / (1 + e^{-x})$$

“Sigmoid”

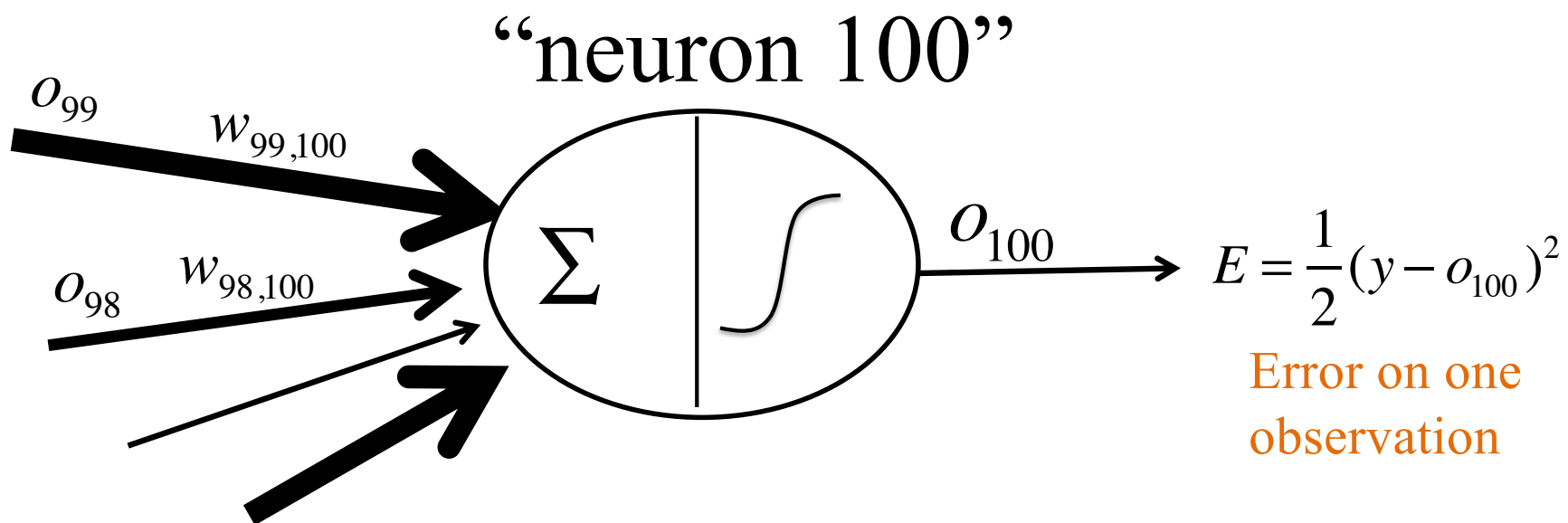


Activation  
Function

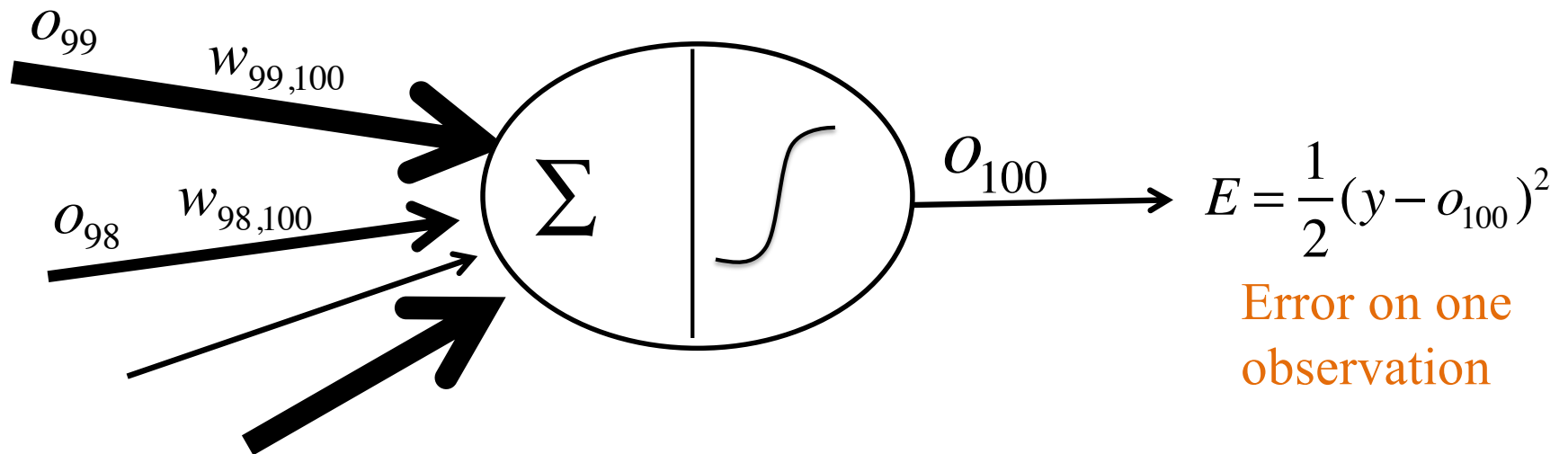




# Single Layer



# Single Layer



- In a brain, the synapses strengthen and weaken in order to learn.
- Say the same thing happens here.
- How should we set the weights in order to learn (reduce the error)?
- Minimize  $E$  with respect to the weights.

# Backpropagation

- An algorithm that trains the weights of a neural network
- Requires us to propagate information backwards through the network, then forwards, then backwards, then forwards, etc.
- Propagate backwards = chain rule from calculus.



# Backpropagation

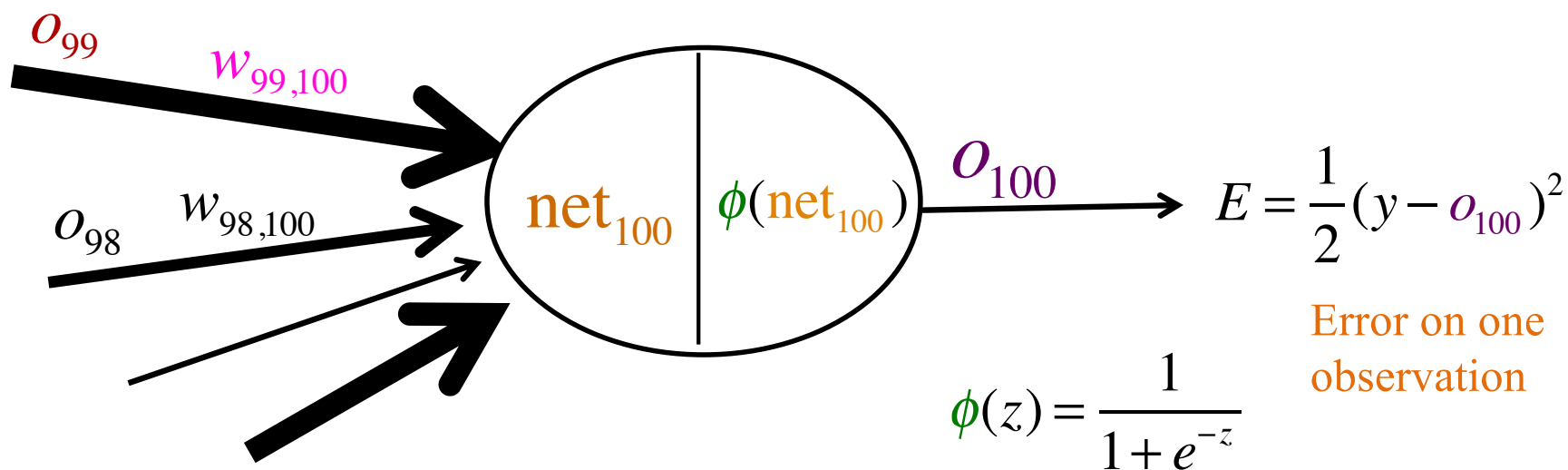
Cynthia Rudin

Duke Machine Learning

# Backpropagation

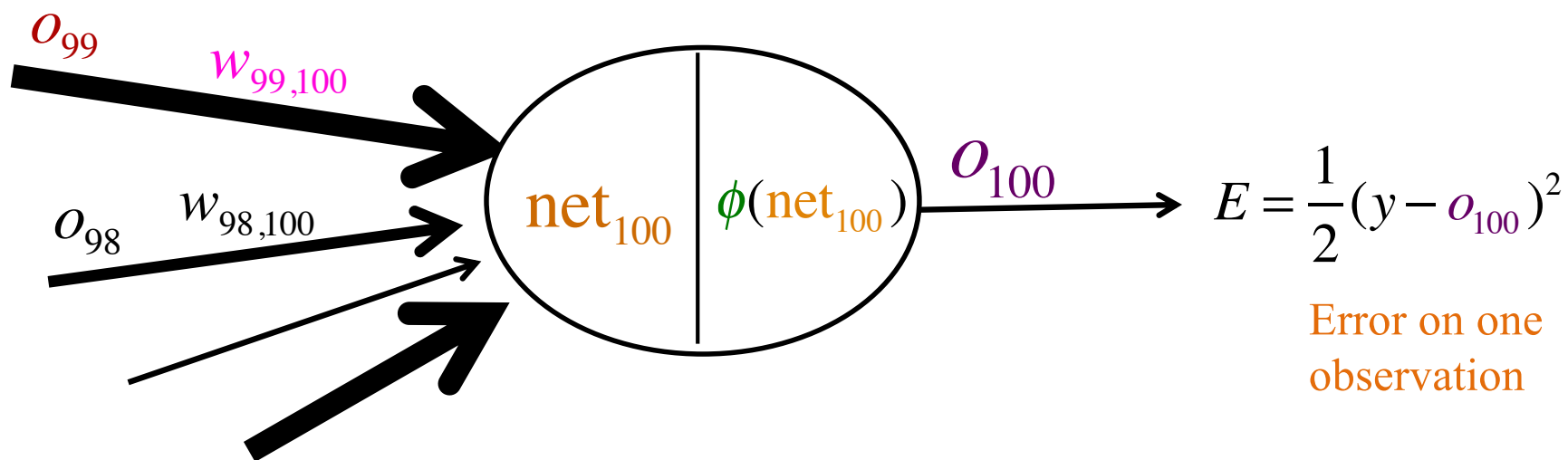
- An algorithm that trains the weights of a neural network
- Requires us to propagate information backwards through the network, then forwards, then backwards, then forwards, etc.
- Propagate backwards = chain rule from calculus.

# Single Layer



$$\frac{dE}{dw_{99,100}} = \frac{dE}{do_{100}} \frac{do_{100}}{d \text{net}_{100}} \frac{d \text{net}_{100}}{dw_{99,100}}$$

# Single Layer



$$\frac{dE}{dw_{99,100}} = \frac{dE}{dO_{100}} \frac{dO_{100}}{d\text{net}_{100}} \frac{d\text{net}_{100}}{dw_{99,100}}$$



# Single Layer

$$E = \frac{1}{2}(y - o_{100})^2$$

Error on one  
observation

$$\frac{dE}{do_{100}} = -\frac{1}{2}2(y - o_{100})$$

$$\frac{dE}{dw_{99,100}} = \frac{dE}{do_{100}} \frac{do_{100}}{d \text{net}_{100}} \frac{d \text{net}_{100}}{dw_{99,100}}$$

$-(y - o_{100})$

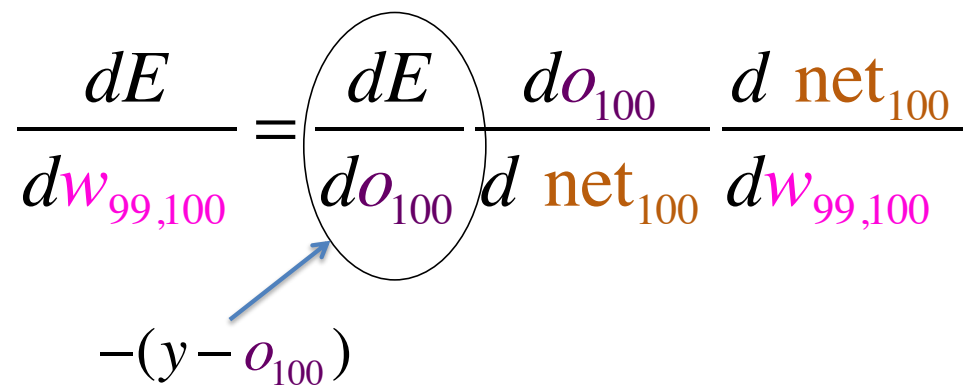
# Single Layer

$$E = \frac{1}{2}(y - o_{100})^2$$

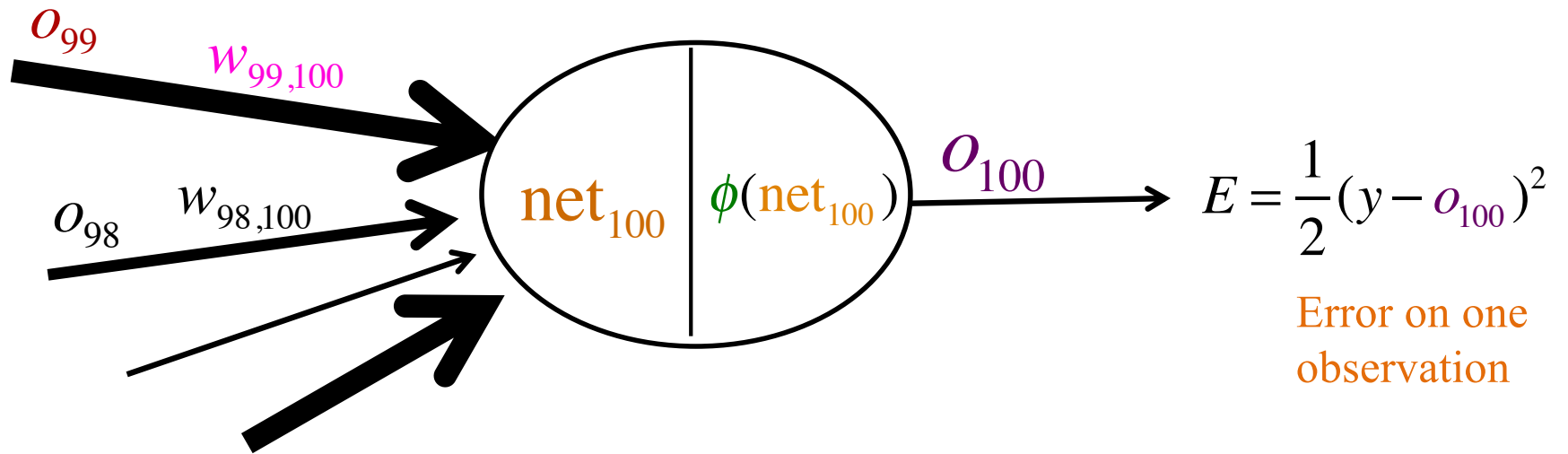
Error on one  
observation

$$\frac{dE}{d\mathbf{w}_{99,100}} = \left( \frac{dE}{do_{100}} \right) \frac{do_{100}}{d \text{net}_{100}} \frac{d \text{net}_{100}}{d\mathbf{w}_{99,100}}$$

$-(y - o_{100})$



# Single Layer



$$\frac{dE}{dw_{99,100}} = \frac{dE}{dO_{100}} \left( \frac{dO_{100}}{d\text{net}_{100}} \right) \frac{d\text{net}_{100}}{dw_{99,100}}$$

$-(y - O_{100})$

# Single Layer

$$\phi(\text{net}_{100}) \quad o_{100}$$

$$\frac{do_{100}}{d \text{net}_{100}} = \frac{d\phi(\text{net}_{100})}{d \text{net}_{100}} = \phi'(\text{net}_{100}) = \phi(\text{net}_{100})(1 - \phi(\text{net}_{100})) = o_{100}(1 - o_{100})$$

$$\frac{dE}{dw_{99,100}} = \frac{dE}{do_{100}} \left( \frac{do_{100}}{d \text{net}_{100}} \right) \frac{d \text{net}_{100}}{dw_{99,100}}$$

$$-(y - o_{100})$$

# Single Layer

$$\phi(\text{net}_{100}) \quad o_{100}$$

$$\frac{do_{100}}{d \text{net}_{100}} = \frac{d\phi(\text{net}_{100})}{d \text{net}_{100}} = \phi'(\text{net}_{100}) = \phi(\text{net}_{100})(1 - \phi(\text{net}_{100})) = o_{100}(1 - o_{100})$$

$$\frac{dE}{dw_{99,100}} = \frac{dE}{do_{100}} \left( \frac{do_{100}}{d \text{net}_{100}} \right) \frac{d \text{net}_{100}}{dw_{99,100}}$$


Diagram illustrating the backpropagation of error through the output layer:

- The term  $\frac{dE}{do_{100}}$  is associated with the error  $-(y - o_{100})$ .
- The term  $\left( \frac{do_{100}}{d \text{net}_{100}} \right)$  is associated with the derivative  $o_{100}(1 - o_{100})$ .
- The term  $\frac{d \text{net}_{100}}{dw_{99,100}}$  represents the local gradient of the net input with respect to the weight.

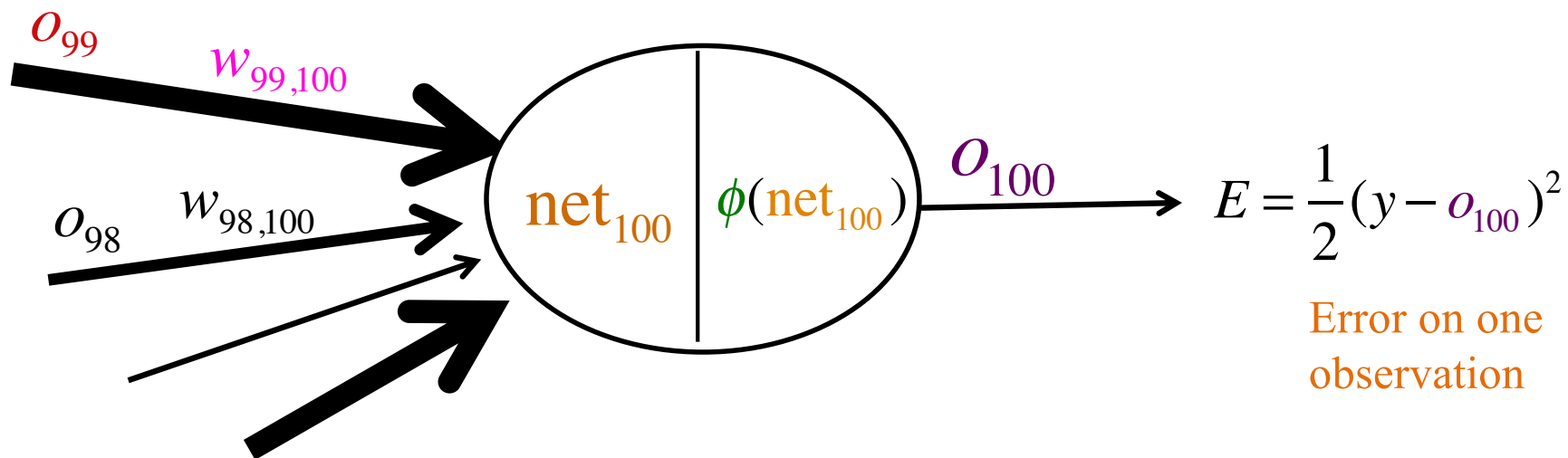
# Single Layer

$$\frac{dE}{d\mathbf{w}_{99,100}} = \frac{dE}{d\mathbf{o}_{100}} \frac{d\mathbf{o}_{100}}{d\mathbf{net}_{100}} \frac{d\mathbf{net}_{100}}{d\mathbf{w}_{99,100}}$$

$-(y - \mathbf{o}_{100})$        $\mathbf{o}_{100}(1 - \mathbf{o}_{100})$



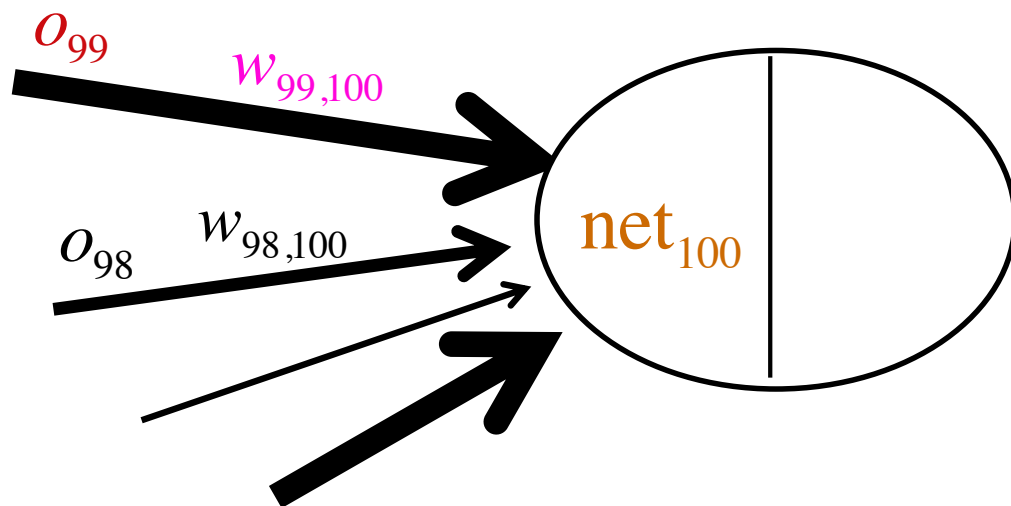
# Single Layer



$$\frac{dE}{dw_{99,100}} = \frac{dE}{dO_{100}} \frac{dO_{100}}{d\text{net}_{100}} \frac{d\text{net}_{100}}{dw_{99,100}}$$

$\frac{dE}{dO_{100}} = -(y - O_{100})$   
 $\frac{d\text{net}_{100}}{dw_{99,100}} = O_{100}(1 - O_{100})$

$$\frac{d \text{net}_{100}}{dw_{99,100}} = \frac{d (w_{99,100} o_{99} + w_{98,100} o_{98} + w_{97,100} o_{97} + \dots)}{dw_{99,100}} = o_{99}$$




$$\frac{dE}{dw_{99,100}} = \frac{dE}{do_{100}} \frac{do_{100}}{d \text{net}_{100}} \frac{d \text{net}_{100}}{dw_{99,100}}$$

Diagram illustrating the chain rule for the derivative of the error  $E$  with respect to the weight  $w_{99,100}$ . The equation is shown with annotations:


- The term  $\frac{dE}{do_{100}}$  is annotated with a blue arrow pointing to it from the expression  $-(y - o_{100})$  below.
- The term  $\frac{do_{100}}{d \text{net}_{100}}$  is annotated with a blue arrow pointing to it from the expression  $o_{100}(1 - o_{100})$  below.
- The term  $\frac{d \text{net}_{100}}{dw_{99,100}}$  is enclosed in a circle, and a blue arrow points to it from the expression  $o_{99}$  to the right.




$$\frac{dE}{d\textcolor{violet}{w}_{99,100}} = \frac{dE}{d\textcolor{violet}{o}_{100}} \frac{d\textcolor{violet}{o}_{100}}{d\textcolor{brown}{net}_{100}} \frac{d\textcolor{brown}{net}_{100}}{d\textcolor{violet}{w}_{99,100}}$$



$-(y - \textcolor{violet}{o}_{100})$



$\textcolor{violet}{o}_{100} (1 - \textcolor{violet}{o}_{100})$



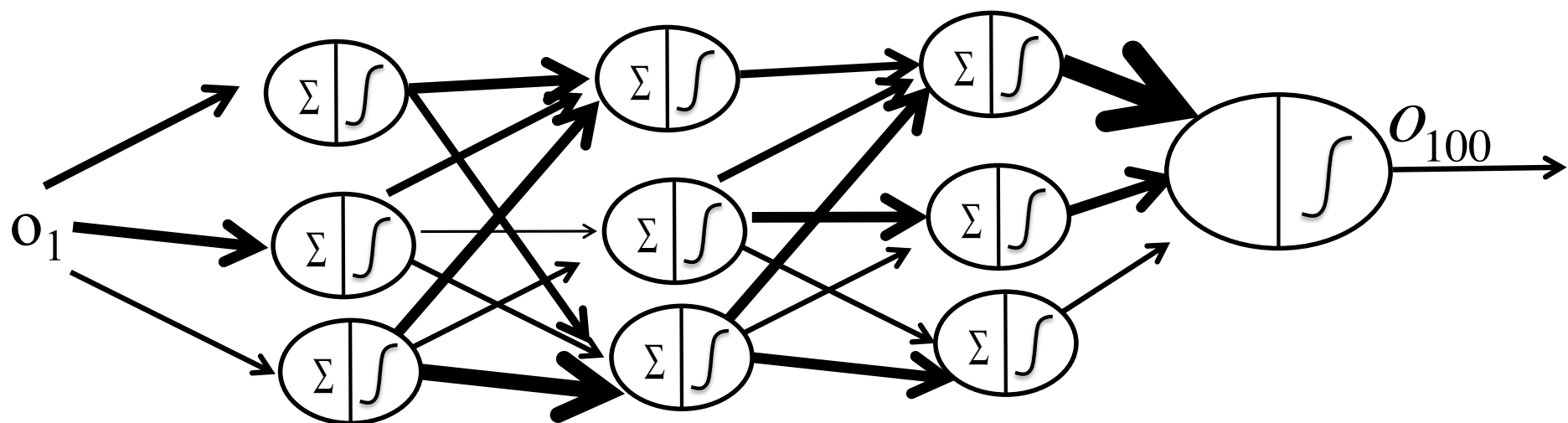
$\textcolor{red}{o}_{99}$

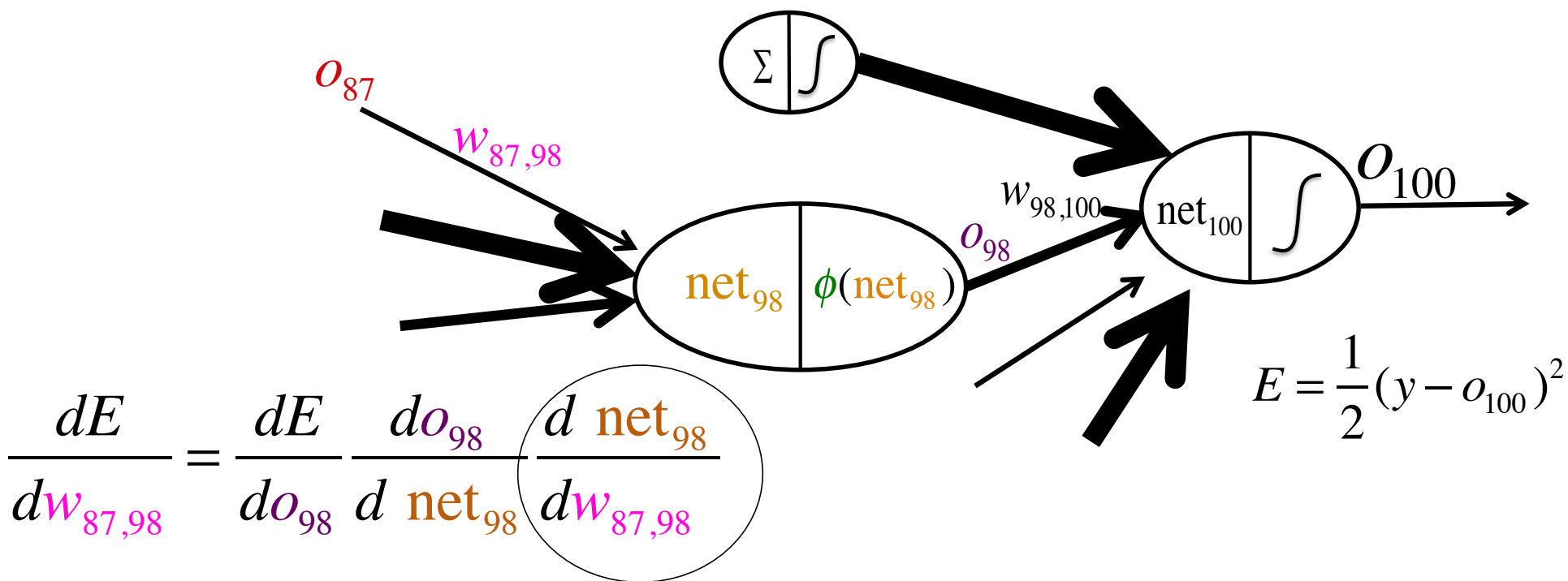
We will need this later – it depends only on node 100

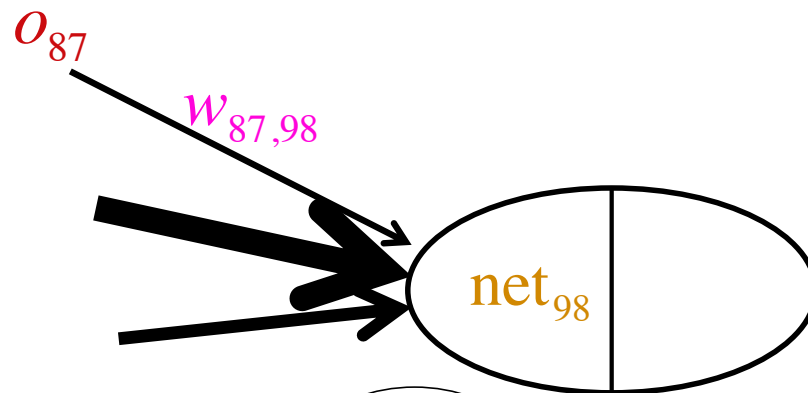
$$\begin{aligned}
 \frac{dE}{d\mathbf{w}_{99,100}} &= \frac{\delta_{100}}{\frac{dE}{do_{100}} \frac{d \mathbf{net}_{100}}{d \mathbf{w}_{99,100}}} \\
 &= (-(y - o_{100})) o_{100} (1 - o_{100}) o_{99}
 \end{aligned}$$

# Backpropagation

- Go one layer deeper.

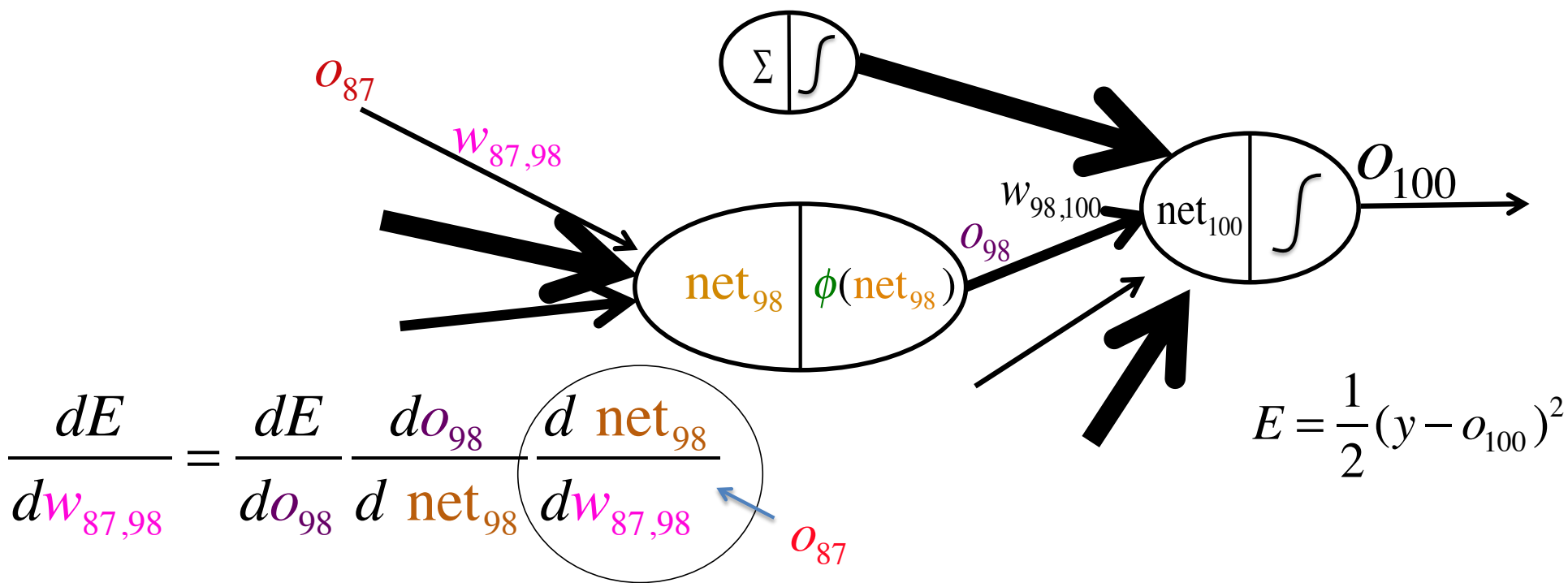


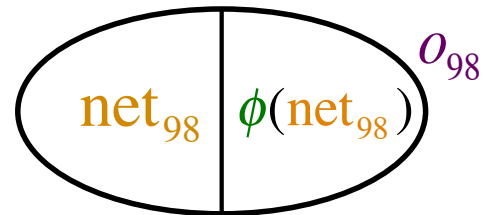




$$\frac{dE}{dw_{87,98}} = \frac{dE}{do_{98}} \frac{do_{98}}{d \text{net}_{98}} \frac{d \text{net}_{98}}{dw_{87,98}}$$

$$\frac{d \text{net}_{98}}{dw_{87,98}} = \frac{d (w_{87,98} O_{87} + w_{86,98} O_{86} + w_{85,98} O_{85} + \dots)}{dw_{87,98}} = O_{87}$$



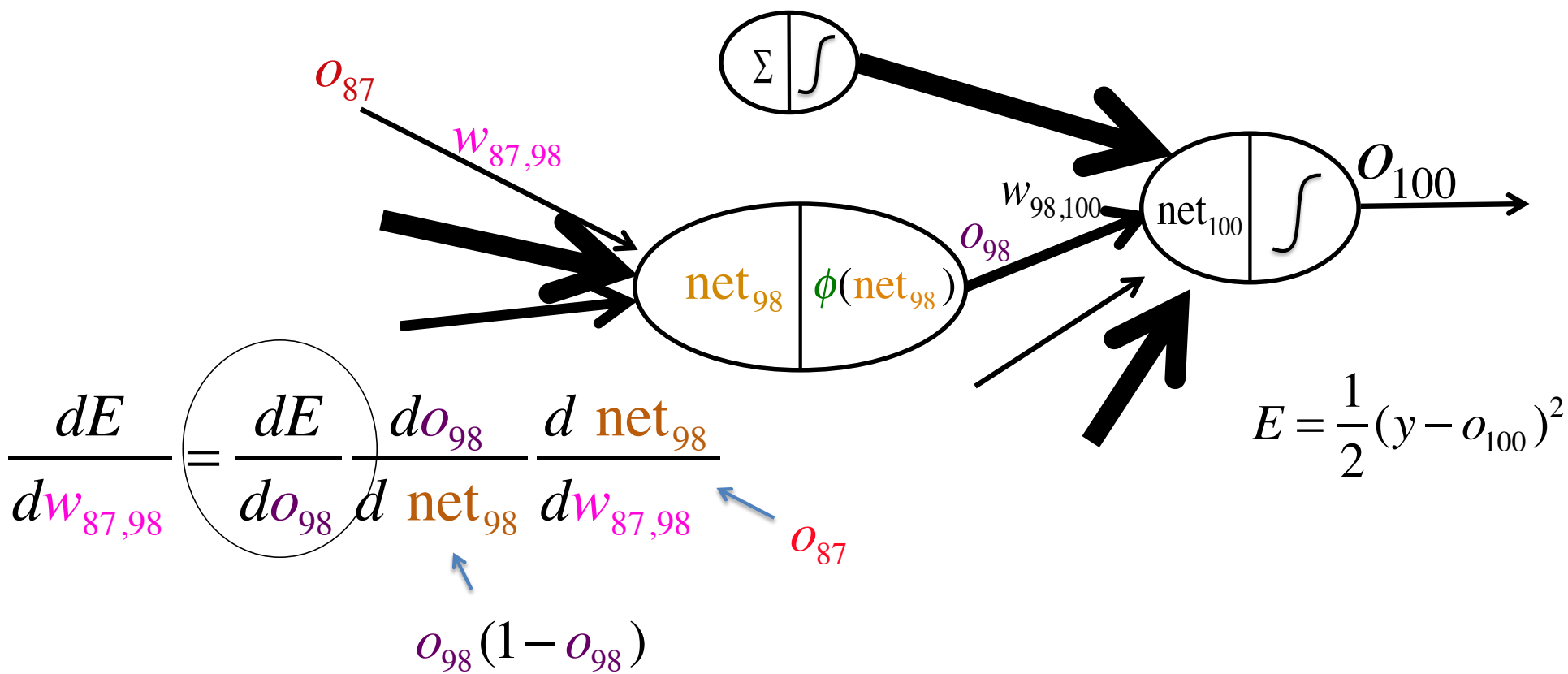


$$\frac{dE}{d\mathbf{w}_{87,98}} = \frac{dE}{do_{98}} \frac{do_{98}}{d\text{net}_{98}} \frac{d\text{net}_{98}}{d\mathbf{w}_{87,98}}$$

A blue arrow points from the label  $o_{87}$  (red) to the term  $\frac{d\text{net}_{98}}{d\mathbf{w}_{87,98}}$  in the equation.

$$\frac{do_{98}}{d\text{net}_{98}} = \frac{d\phi(\text{net}_{98})}{d\text{net}_{98}} = \phi'(\text{net}_{98}) = \phi(\text{net}_{98})(1 - \phi(\text{net}_{98})) = o_{98}(1 - o_{98})$$

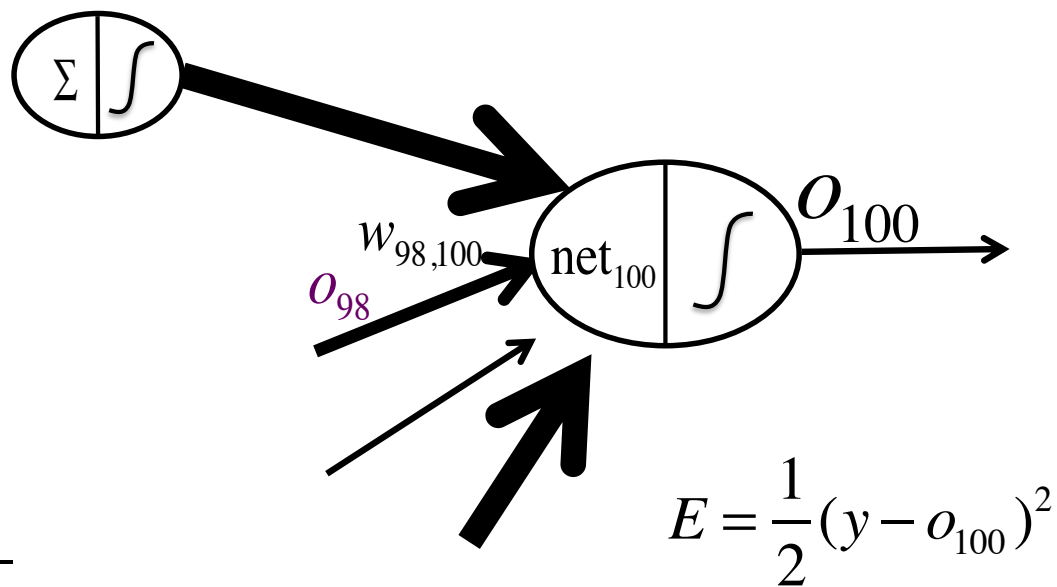




$$\frac{dE}{dw_{87,98}} = \frac{dE}{do_{98}} \frac{do_{98}}{d \text{net}_{98}} \frac{d \text{net}_{98}}{dw_{87,98}}$$

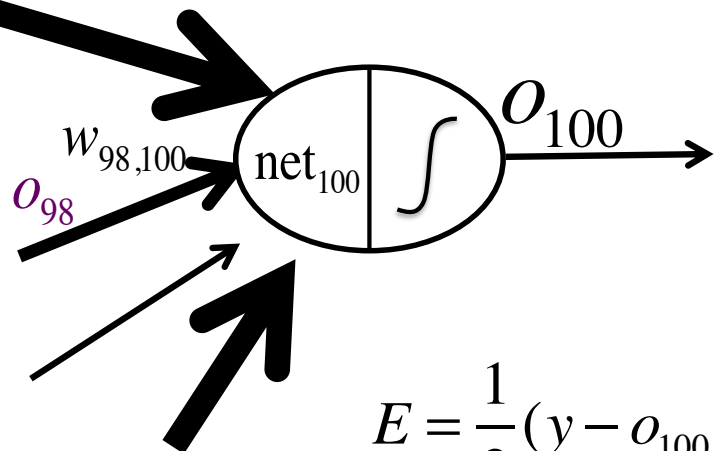
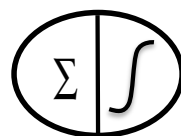
$o_{98}(1 - o_{98})$

$o_{87}$



$$\frac{dE}{do_{98}} = \left( \frac{dE}{d\text{net}_{100}} \right) \frac{d\text{net}_{100}}{do_{98}}$$

$$\frac{dE}{dw_{87,98}} = \left( \frac{dE}{do_{98}} \right) \frac{do_{98}}{d\text{net}_{98}} \frac{d\text{net}_{98}}{dw_{87,98}}$$



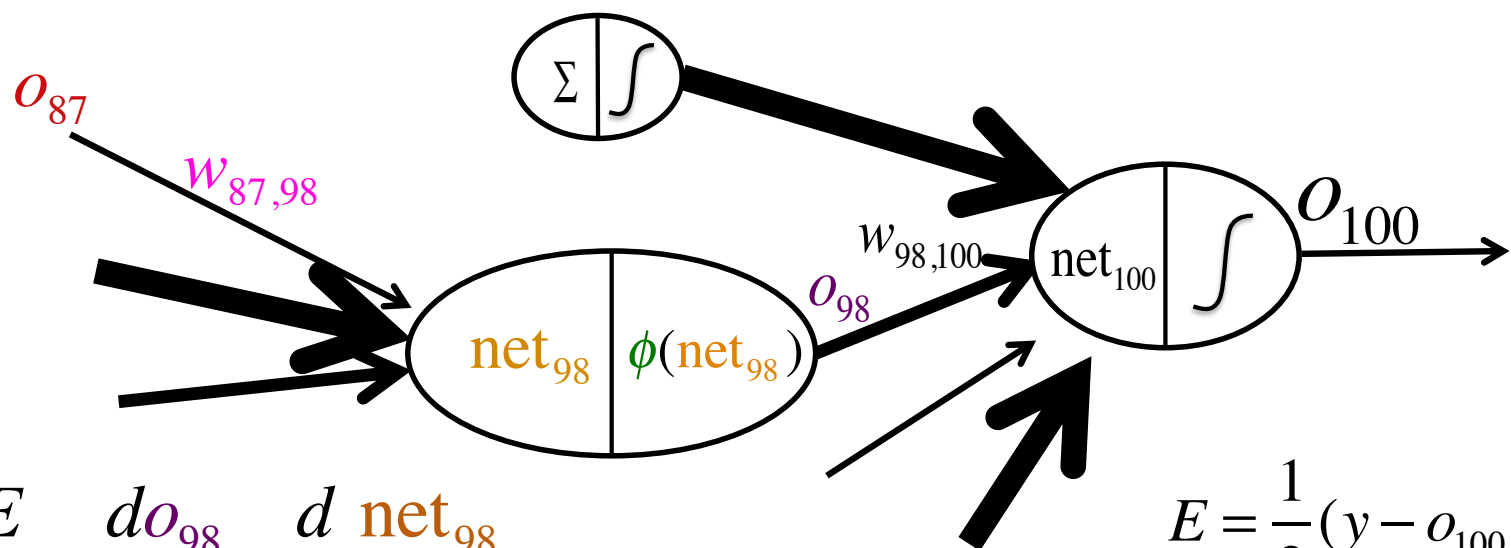
$$E = \frac{1}{2} (y - o_{100})^2$$

$$\frac{d \text{net}_{100}}{d o_{98}} = \frac{d(w_{99,100} o_{99} + w_{98,100} o_{98} + \dots)}{d o_{98}} = w_{98,100}$$

$$\frac{dE}{d o_{98}} = \frac{\frac{dE}{d \text{net}_{100}} \frac{d \text{net}_{100}}{d o_{98}}}{\frac{d \text{net}_{100}}{d o_{98}}}$$

$$\frac{dE}{d w_{87,98}} = \frac{dE}{d o_{98}} \frac{d o_{98}}{d \text{net}_{98}} \frac{d \text{net}_{98}}{d w_{87,98}}$$

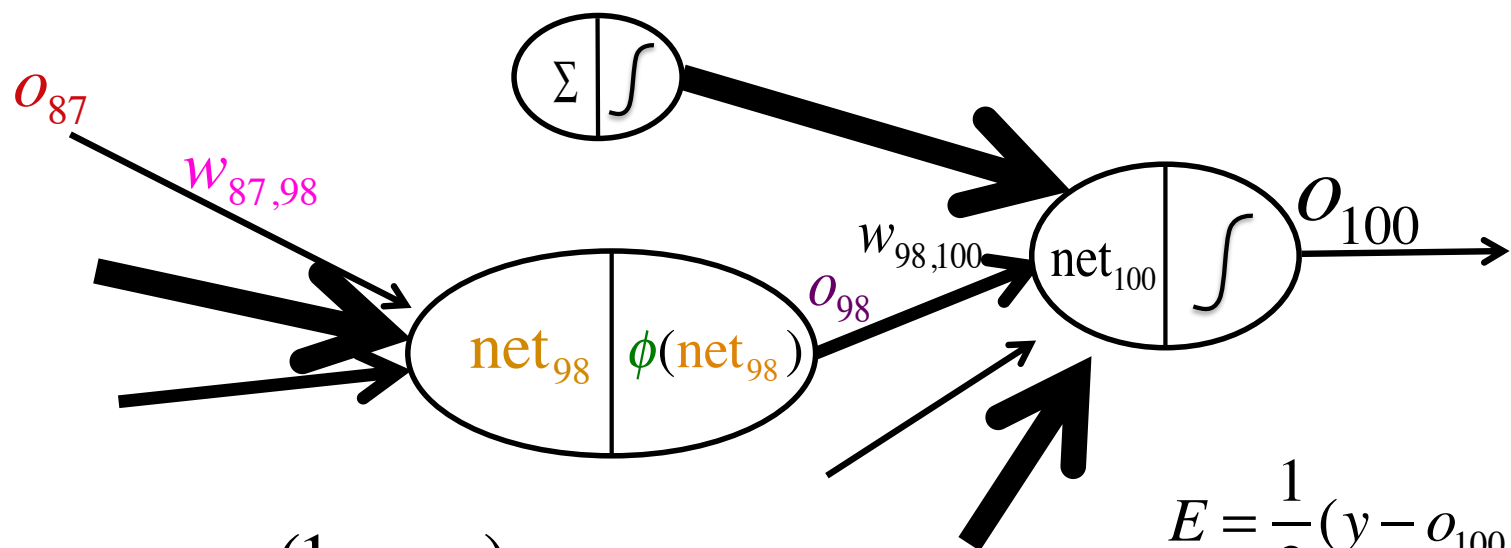
$o_{98}(1 - o_{98})$



$$\frac{dE}{dw_{87,98}} = \frac{dE}{do_{98}} \frac{do_{98}}{d\text{net}_{98}} \frac{d\text{net}_{98}}{dw_{87,98}}$$

Annotations for the chain rule terms:

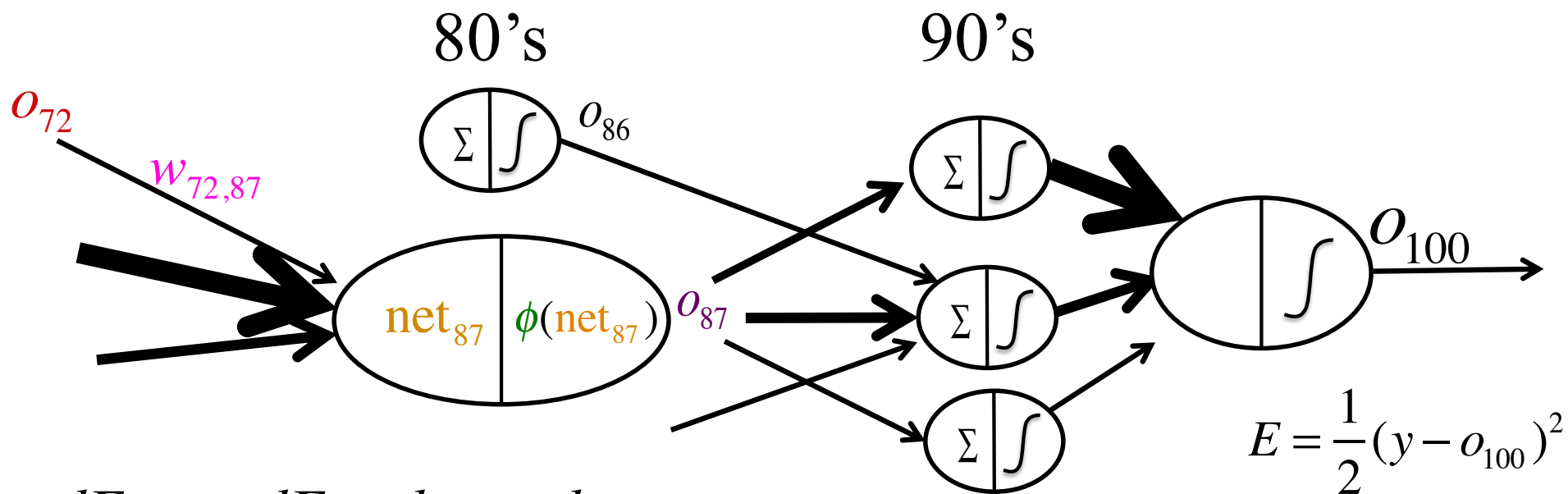
- $\frac{dE}{do_{98}}$  is associated with  $\delta_{100} w_{98,100}$  (blue arrow pointing to  $do_{98}$ ).
- $\frac{do_{98}}{d\text{net}_{98}}$  is associated with  $o_{98}(1 - o_{98})$  (blue arrow pointing to  $d\text{net}_{98}$ ).
- $\frac{d\text{net}_{98}}{dw_{87,98}}$  is associated with  $o_{87}$  (blue arrow pointing to  $dw_{87,98}$ ).



$$\frac{dE}{dw_{87,98}} = \delta_{100} w_{98,100} o_{98} (1 - o_{98}) o_{87}$$

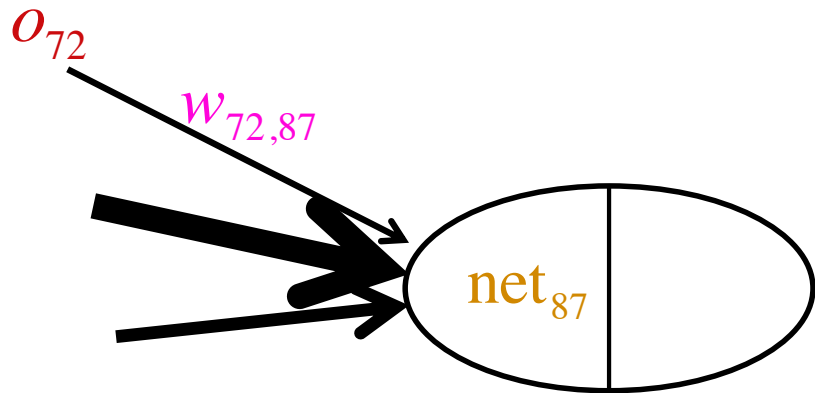
# Backpropagation

- Go even one layer deeper.
- Third time is a charm.



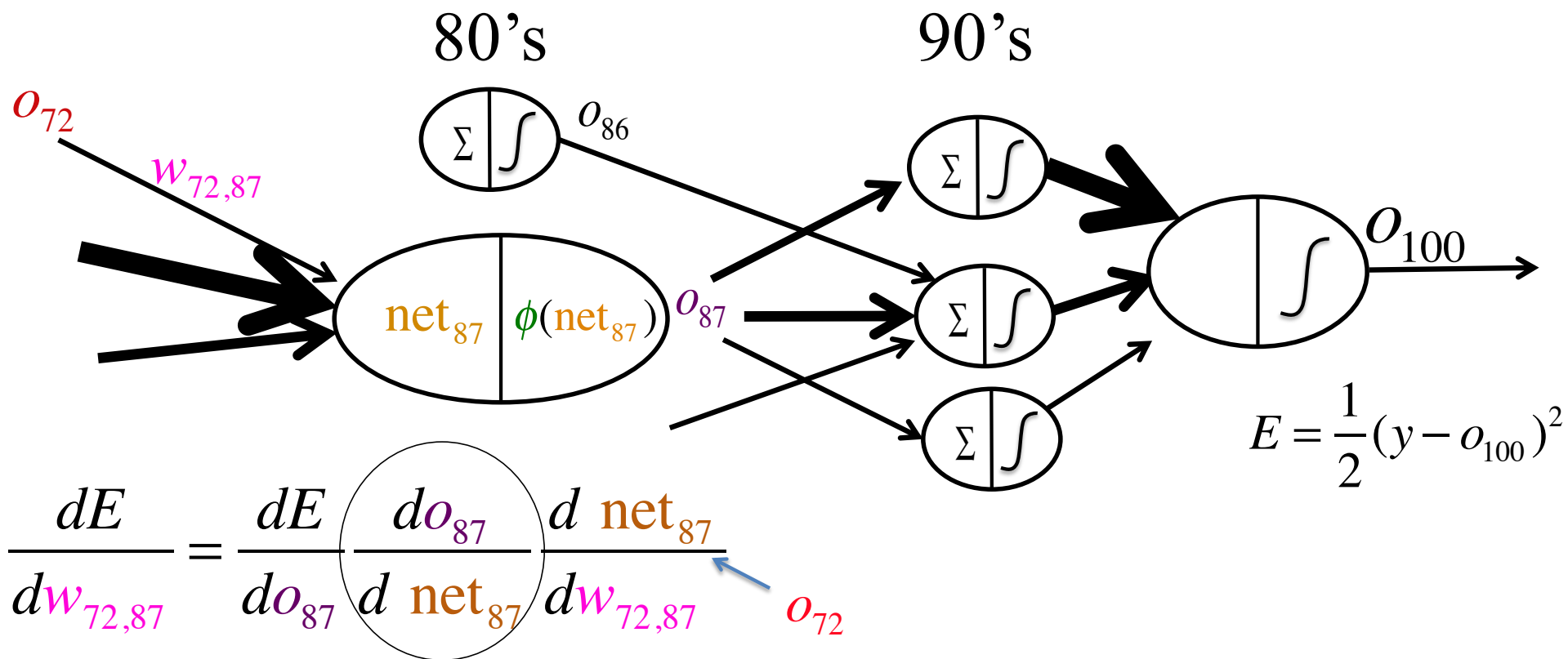
$$\frac{dE}{dw_{72,87}} = \frac{dE}{do_{87}} \frac{do_{87}}{d \text{net}_{87}} \frac{d \text{net}_{87}}{dw_{72,87}}$$

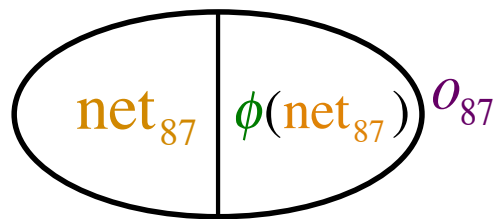




$$\frac{dE}{dw_{72,87}} = \frac{dE}{do_{87}} \frac{do_{87}}{d \text{net}_{87}} \frac{d \text{net}_{87}}{dw_{72,87}}$$

The third term,  $\frac{d \text{net}_{87}}{dw_{72,87}}$ , is circled. A blue arrow points from the red label  $o_{72}$  to the circle.

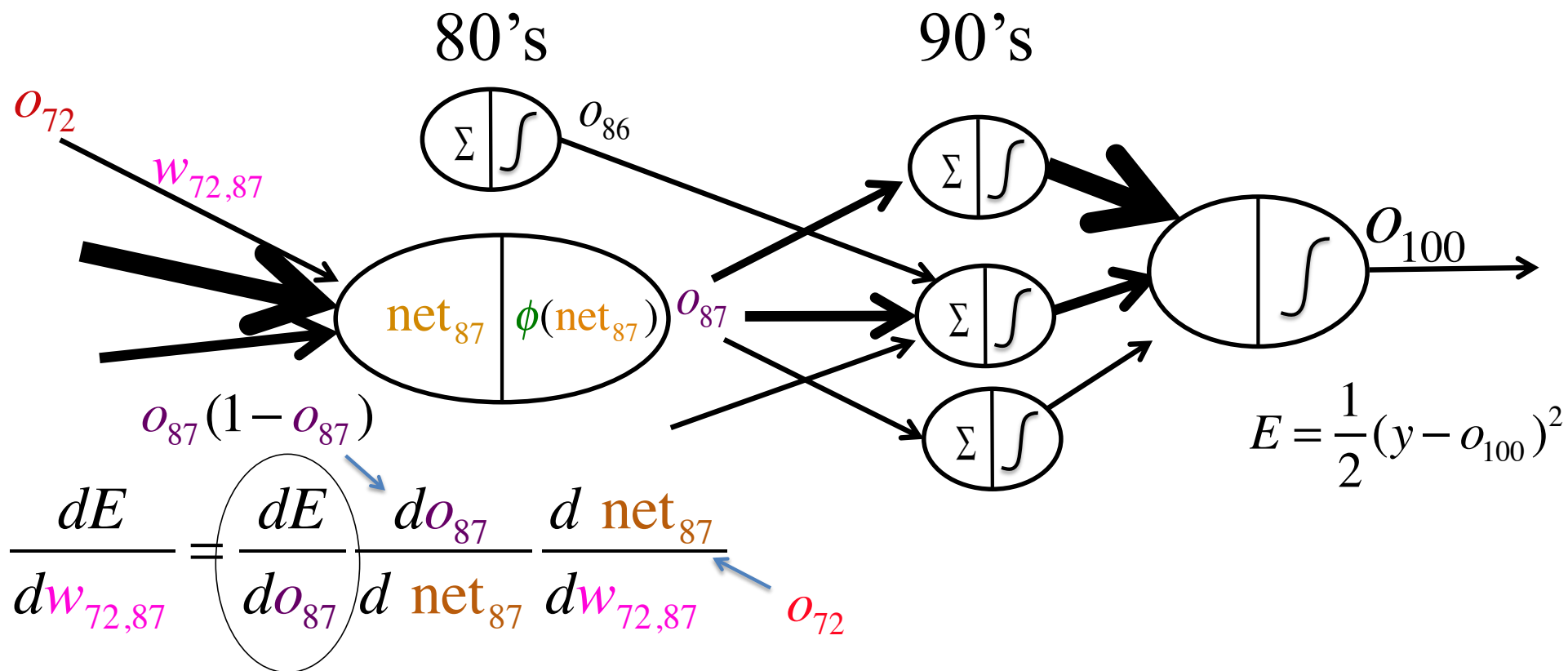




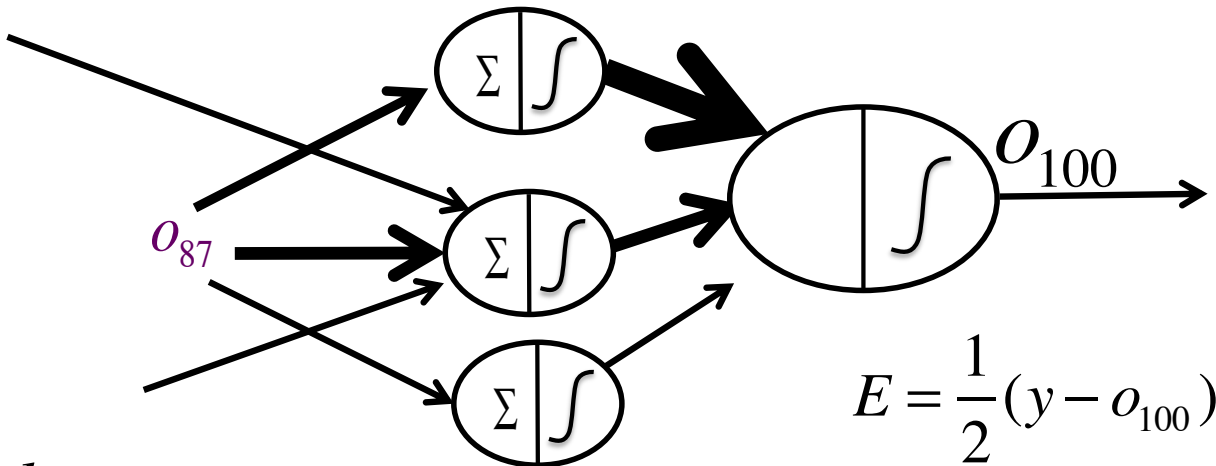
$$\frac{dE}{d\mathbf{w}_{72,87}} = \frac{dE}{do_{87}} \frac{do_{87}}{d\mathbf{net}_{87}} \frac{d\mathbf{net}_{87}}{d\mathbf{w}_{72,87}}$$

$o_{72}$

$$\frac{do_{87}}{d\mathbf{net}_{87}} = \frac{d\phi(\mathbf{net}_{87})}{d\mathbf{net}_{87}} = \phi'(\mathbf{net}_{87}) = \phi(\mathbf{net}_{87})(1 - \phi(\mathbf{net}_{87})) = o_{87}(1 - o_{87})$$



90's



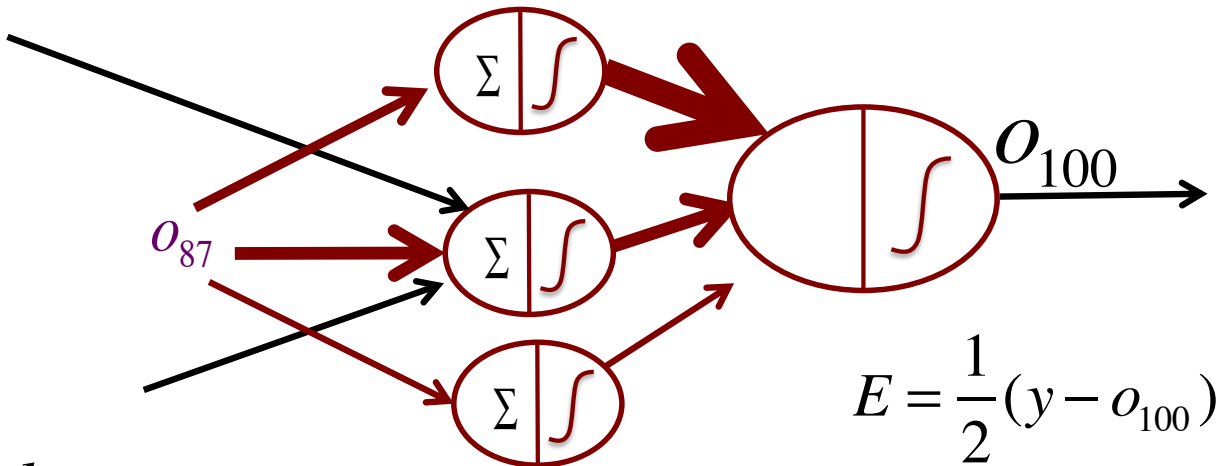
$$E = \frac{1}{2}(y - o_{100})^2$$

$$\frac{dE}{d\mathbf{w}_{72,87}} = \left( \frac{dE}{do_{87}} \right) d\mathbf{net}_{87} \frac{d\mathbf{net}_{87}}{d\mathbf{w}_{72,87}}$$

Diagrammatic annotations for the chain rule equation above:

- A blue arrow points from the term  $do_{87}$  in the middle fraction to the expression  $o_{87}(1 - o_{87})$  above it.
- A blue arrow points from the term  $d\mathbf{net}_{87}$  in the rightmost fraction to the expression  $o_{72}$  below it.

90's

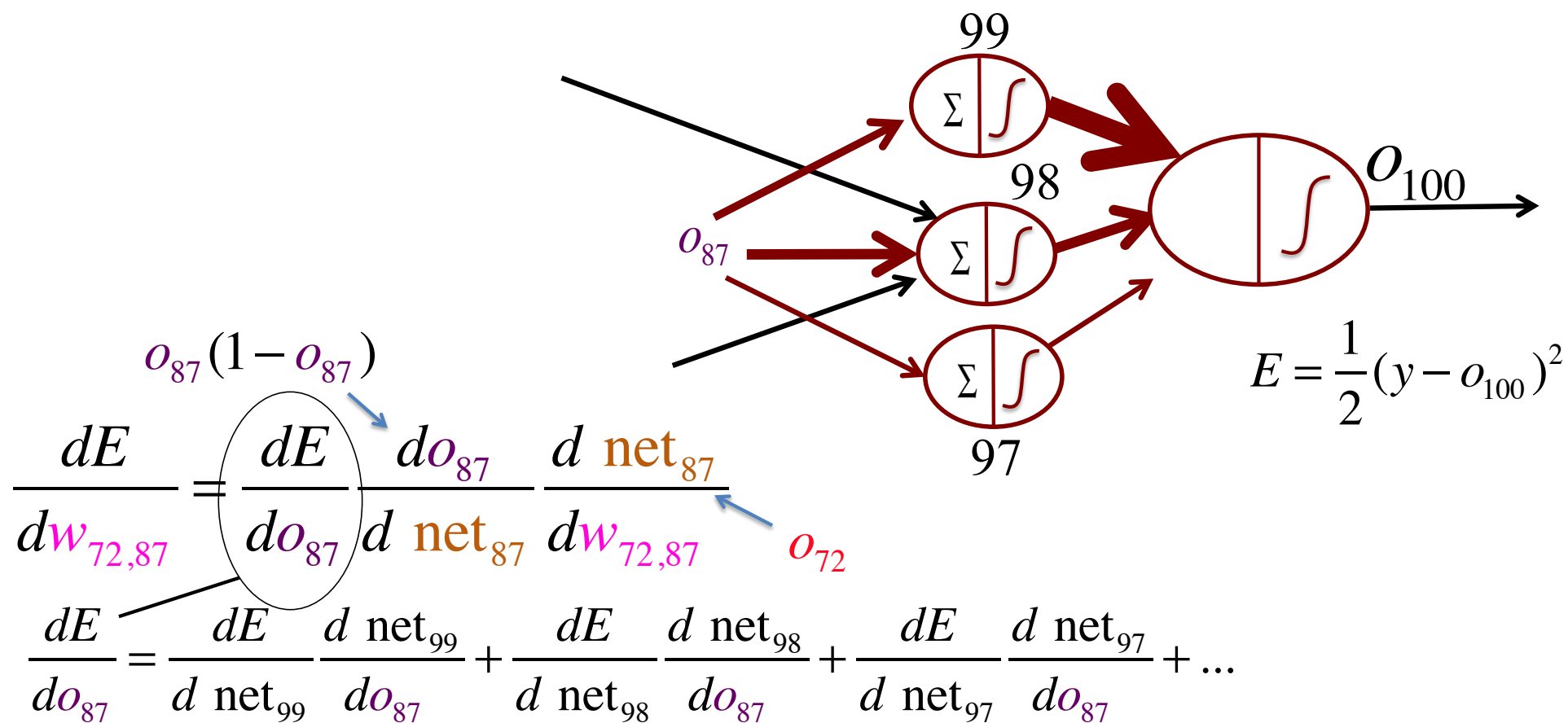


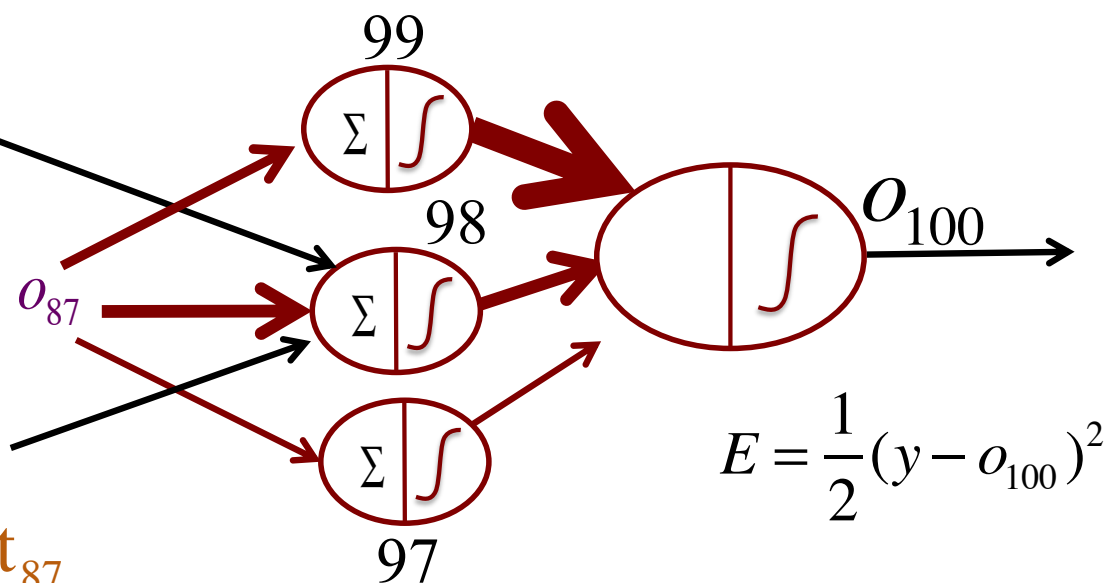
$$E = \frac{1}{2}(y - o_{100})^2$$

$$\frac{dE}{d\mathbf{w}_{72,87}} = \left( \frac{dE}{do_{87}} \right) d\mathbf{net}_{87} \frac{d\mathbf{net}_{87}}{d\mathbf{w}_{72,87}}$$

Diagrammatic annotations for the chain rule above:

- A blue arrow points from  $o_{87}(1 - o_{87})$  to  $\frac{dE}{do_{87}}$ .
- A blue arrow points from  $o_{72}$  to  $\frac{d\mathbf{net}_{87}}{d\mathbf{w}_{72,87}}$ .





$$\frac{dE}{dw_{72,87}} = \frac{dE}{do_{87}} \frac{do_{87}}{d \text{net}_{87}} \frac{d \text{net}_{87}}{dw_{72,87}}$$

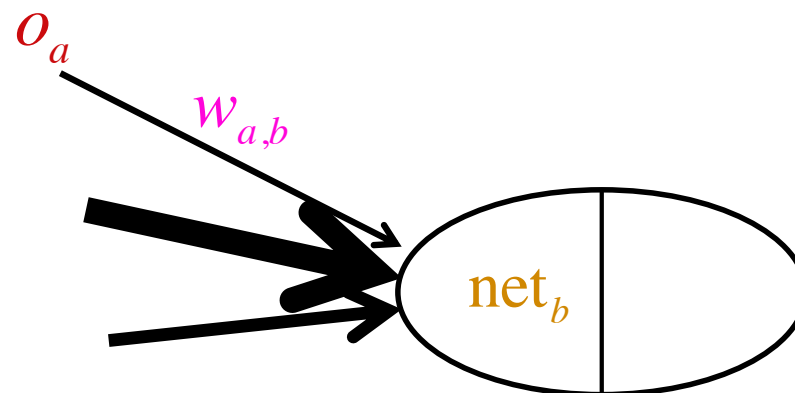
$\text{ } \xrightarrow{o_{87}(1-o_{87})} \text{ } \xleftarrow{o_{72}}$

$$\begin{aligned} \frac{dE}{do_{87}} &= \frac{dE}{d \text{net}_{99}} \frac{d \text{net}_{99}}{do_{87}} + \frac{dE}{d \text{net}_{98}} \frac{d \text{net}_{98}}{do_{87}} + \frac{dE}{d \text{net}_{97}} \frac{d \text{net}_{97}}{do_{87}} + \dots \\ &= \delta_{99} w_{87,99} + \delta_{98} w_{87,98} + \delta_{97} w_{87,97} + \dots = \sum_{\ell \in L} \delta_{87,\ell} w_{87,\ell} \end{aligned}$$

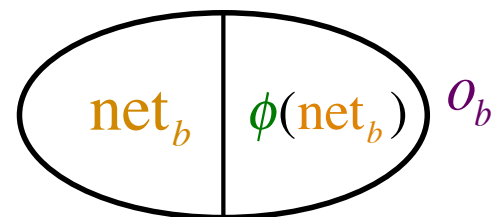



$$\frac{dE}{d\mathbf{w}_{a,b}} = \frac{dE}{do_b} \frac{do_b}{d\mathbf{net}_b} \frac{d\mathbf{net}_b}{d\mathbf{w}_{a,b}}$$

$$= \frac{dE}{do_b} \frac{do_b}{d\mathbf{net}_b} o_a$$

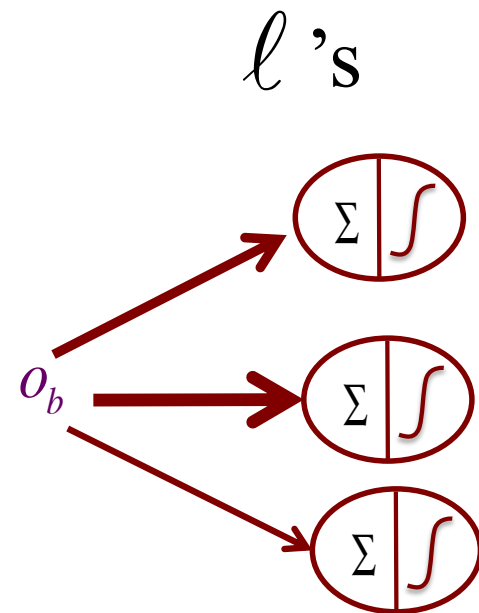


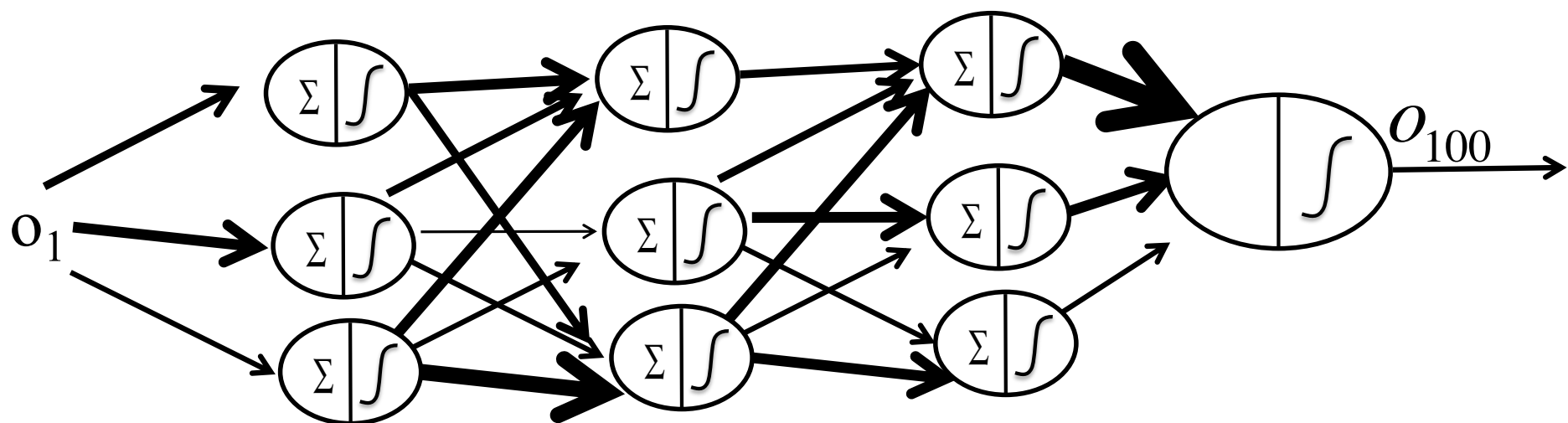
$$\begin{aligned}
 \frac{dE}{d\mathbf{w}_{a,b}} &= \frac{dE}{do_b} \frac{do_b}{d \text{net}_b} \frac{d \text{net}_b}{d\mathbf{w}_{a,b}} \\
 &= \frac{dE}{do_b} \overset{\text{net}_b}{o_b} (1 - \overset{\text{net}_b}{o_b}) \overset{\mathbf{w}_{a,b}}{o_a}
 \end{aligned}$$

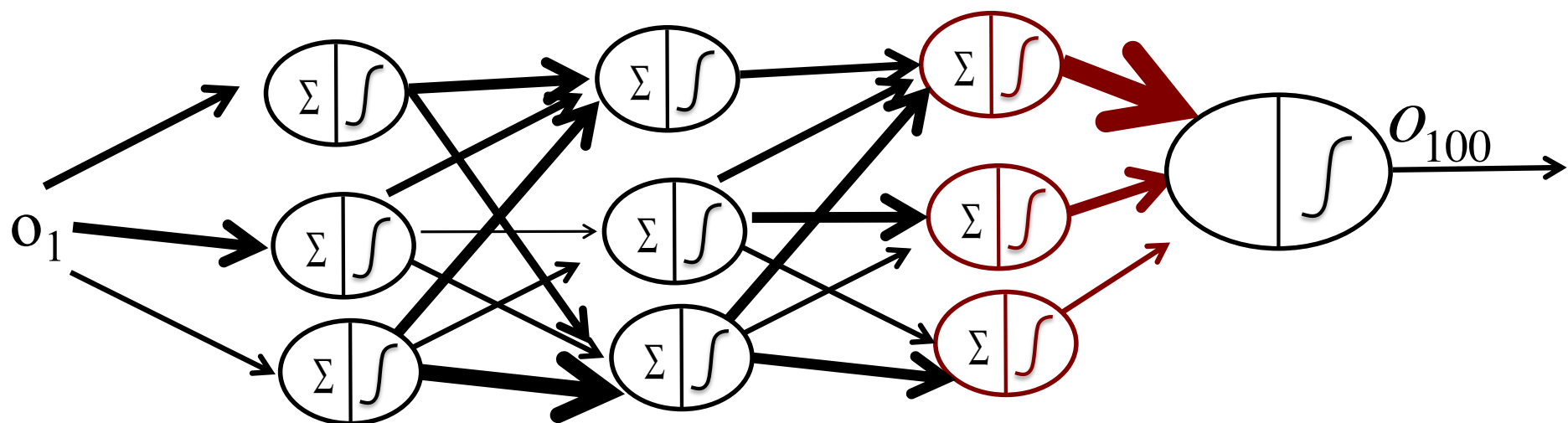


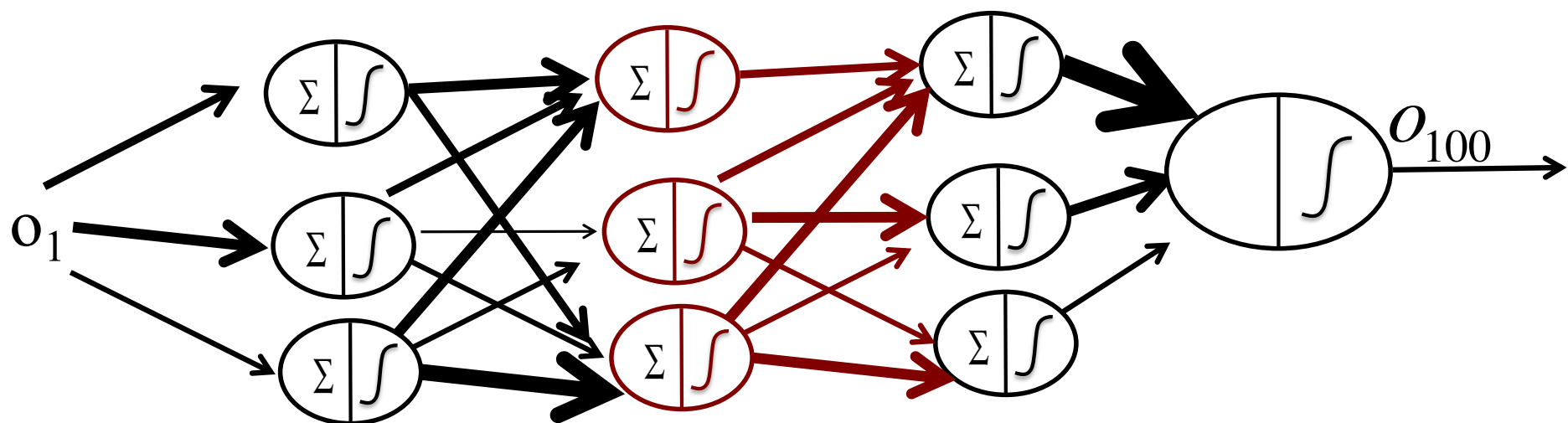
$$\begin{aligned}
 \frac{dE}{d\mathbf{w}_{a,b}} &= \frac{dE}{do_b} \frac{do_b}{d \text{net}_b} \frac{d \text{net}_b}{d\mathbf{w}_{a,b}} \\
 &= \left( \sum_{\ell \in L} \delta_\ell w_{b,\ell} \right) o_b (1 - o_b) o_a
 \end{aligned}$$


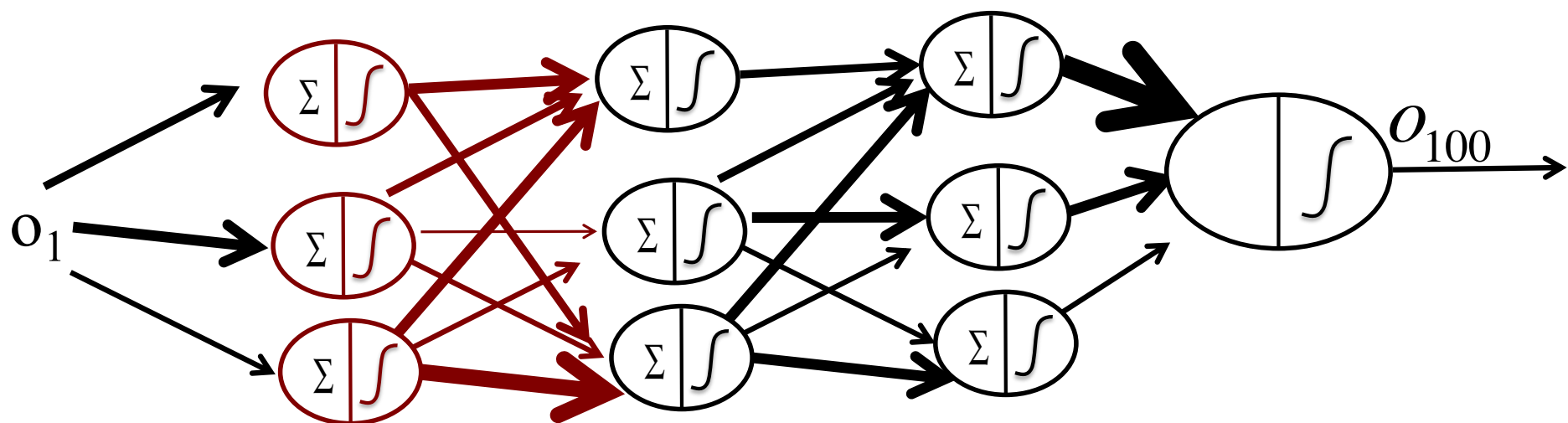
The  $\ell$ 's are downstream. We must have already computed all the  $\delta_\ell$ 's ahead of us to compute this.

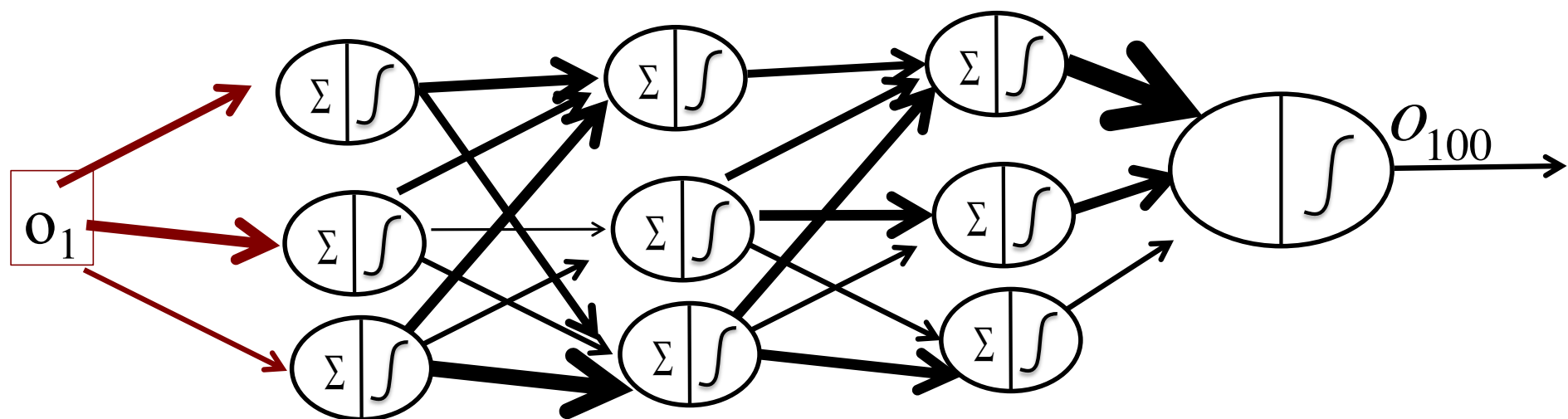




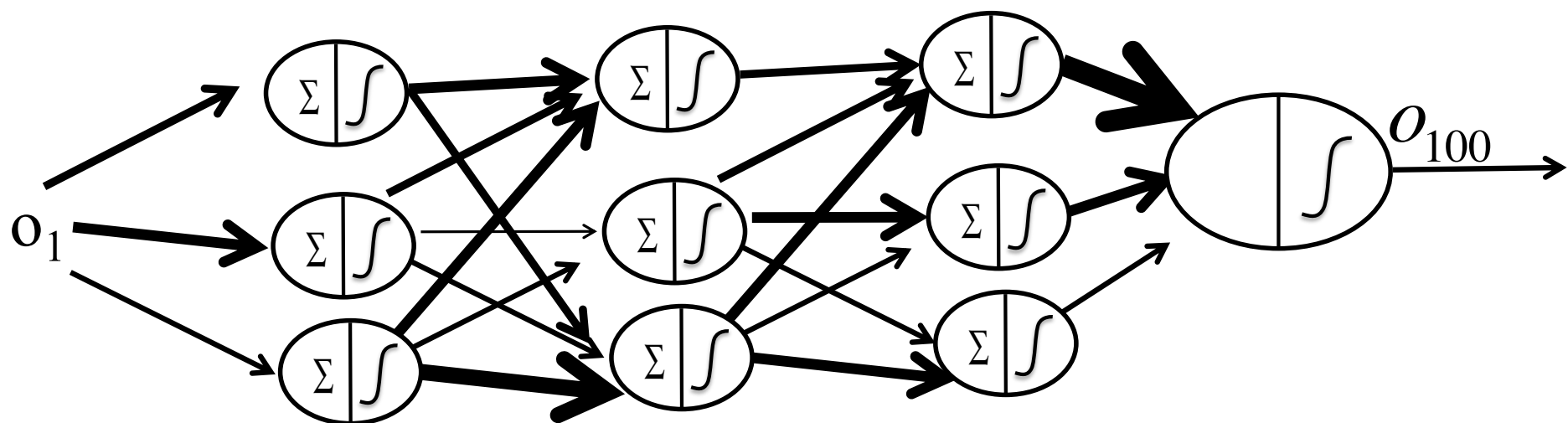










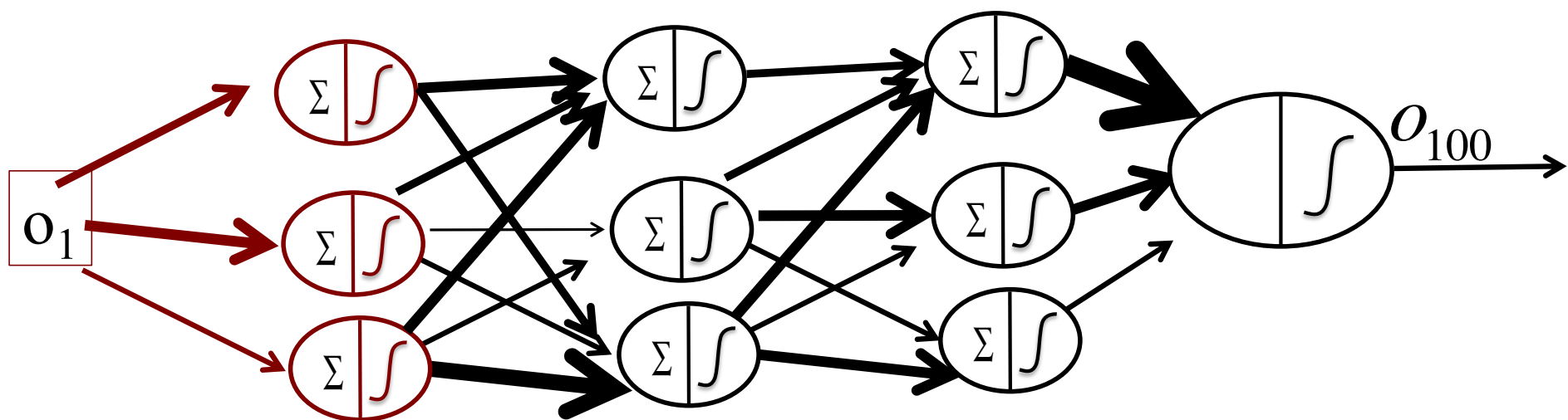


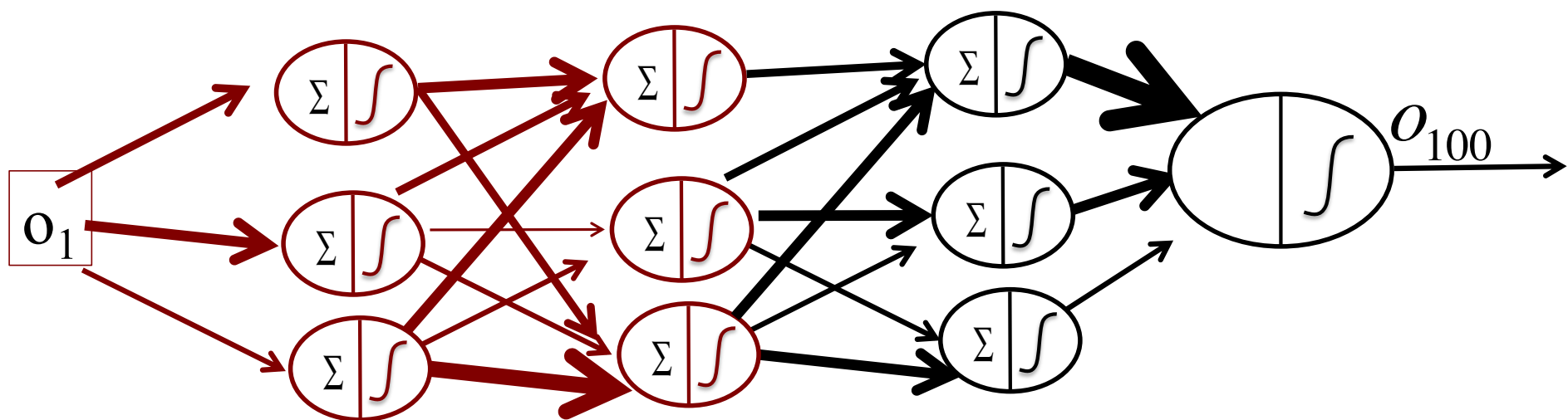
# Backpropagation

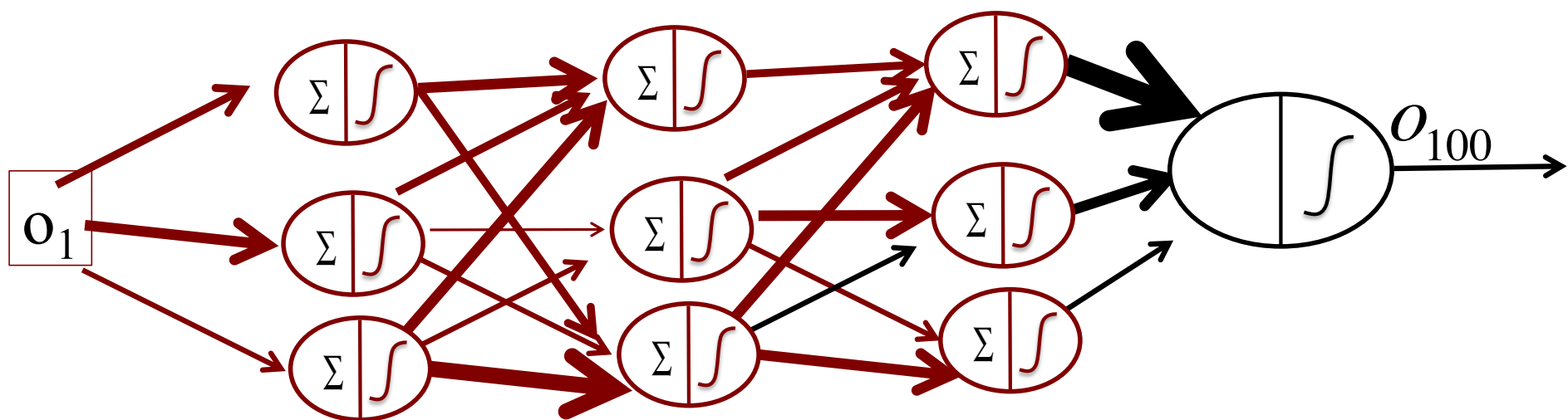
- Now we know how to compute  $\frac{dE}{dw_{a,b}}$  for all  $w_{a,b}$ 's.
- Let's do gradient descent.

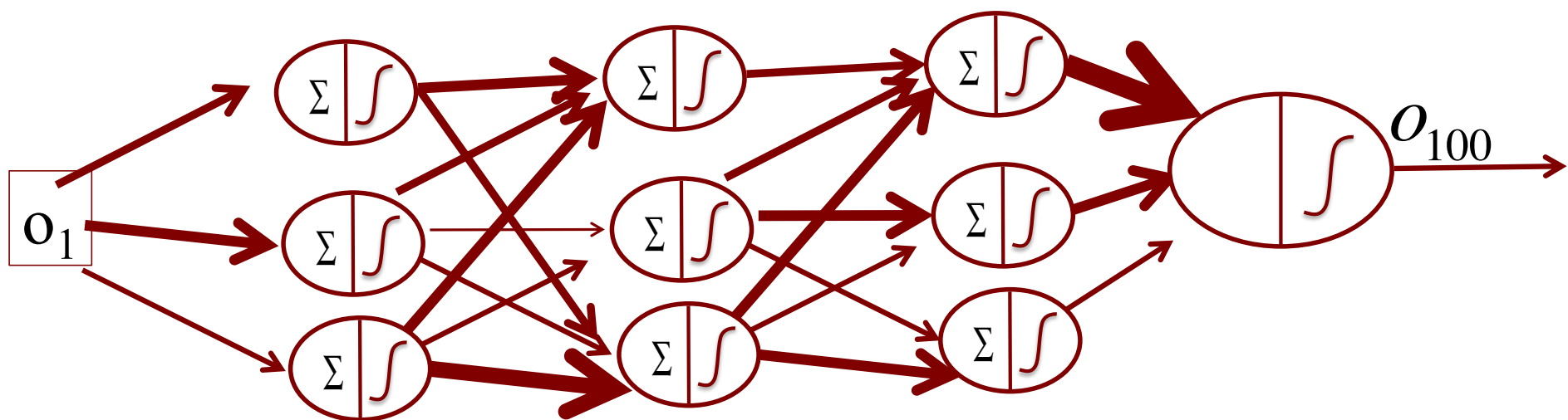
$$w_{a,b} \longleftarrow w_{a,b} - \alpha \frac{dE}{dw_{a,b}}$$

- $\alpha$  is between 0 and 1. Called the “learning rate”.
- Now we know how to propagate errors back through the network.
- Remember how to go forward?









# Backpropagation

- Repeat going backwards (to calculate the gradients), adjusting the weights, and going forwards (to calculate the errors) over and over in order to learn.





# Cross-Entropy is Logistic Loss

Cynthia Rudin

Duke Machine Learning



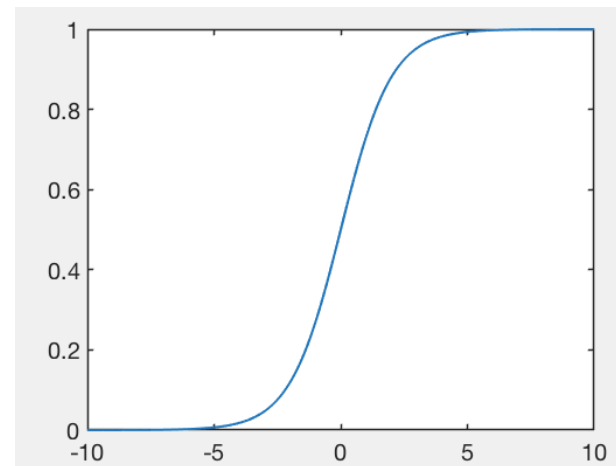
# Convergence Problems in Neural Networks

Cynthia Rudin

Duke Machine Learning

# Convergence Problems

- NN's have **problems with convergence due to vanishing/exploding gradients and saddle points.**
- Vanishing gradients come from the flat part of the activation function.
- Exploding gradients happen when we realize that our gradient has vanished and so increase the learning rate and take huge step sizes to compensate (but then mess everything up!)
- Stick to  $10^{-5}$  to  $10^{-3}$  learning rate perhaps?



# Convergence Problems

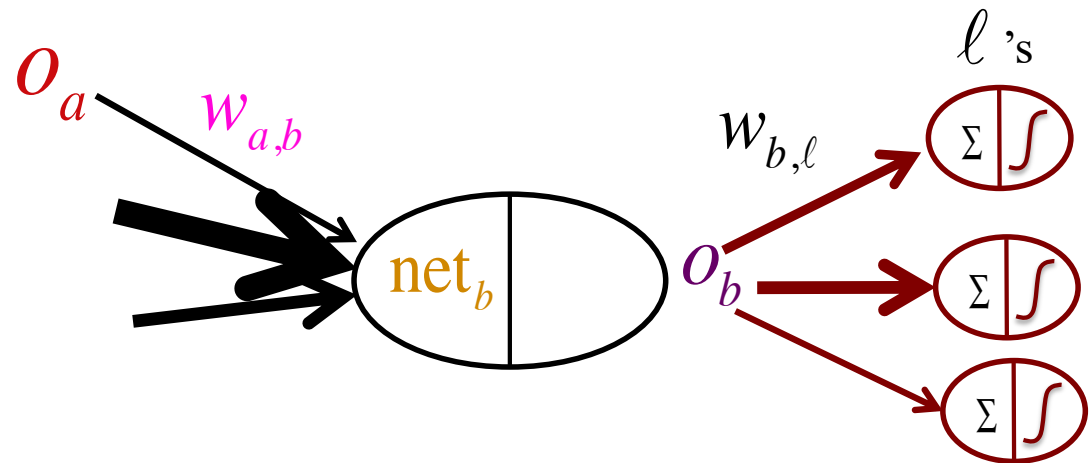
- With the sigmoid activation, the derivatives of the input weights for each node are always **either all positive or all negative**. This is a limitation.

$$\frac{dE}{dw_{a,b}} = \frac{dE}{do_b} \frac{do_b}{d \text{net}_b} \frac{d \text{net}_b}{dw_{a,b}}$$

$$= \left( \sum_{\ell \in L} \delta_{\ell} w_{b,\ell} \right) o_b (1 - o_b) o_a$$

does not  
depend on a

positive, since all outputs of  
sigmoid are between 0 and 1.

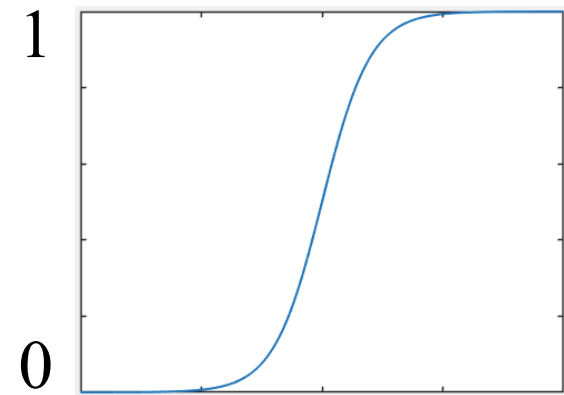


# Convergence Problems

- Bottom line – most people do not use sigmoid-like activation functions, even though this is more biologically relevant.

Sigmoid

$$\sigma(x) = \frac{1}{1 + e^{-x}}$$

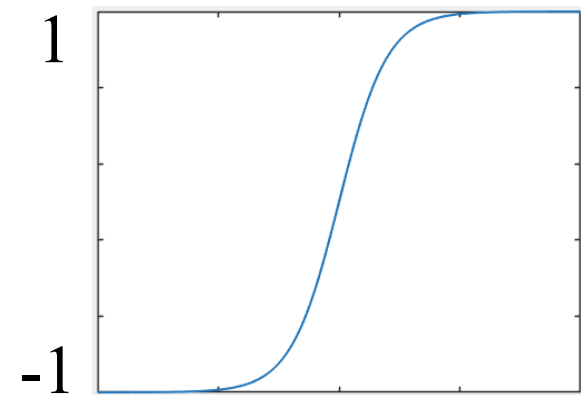


# Convergence Problems

- Bottom line – most people do not use sigmoid-like activation functions, even though this is more biologically relevant.

Sigmoid  $\sigma(x) = \frac{1}{1 + e^{-x}}$

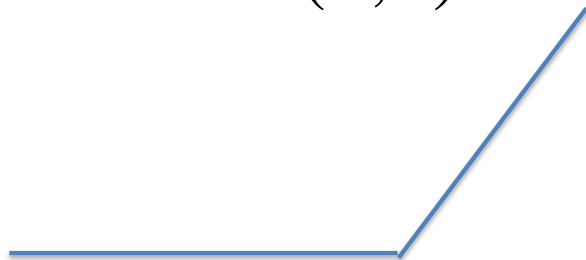
Hyperbolic tangent  $\tanh(x)$



# Convergence Problems

## Rectified Linear Unit (ReLU)

$$\max(0, x)$$



Removes vanishing gradients when nodes are “activated,” meaning  $x > 0$ .

(Krizhevsky et al., 2012)

## Leaky ReLU

$$\max(0.1x, x)$$

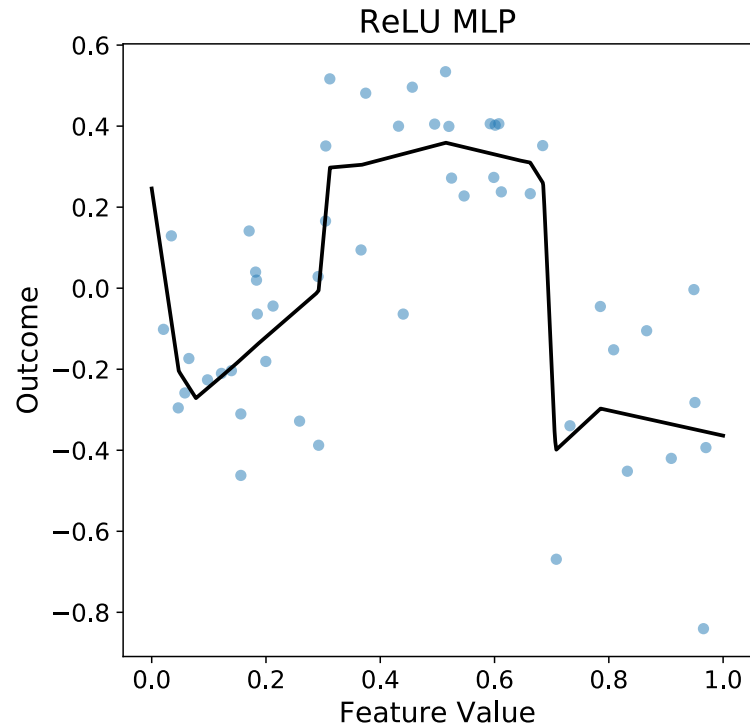
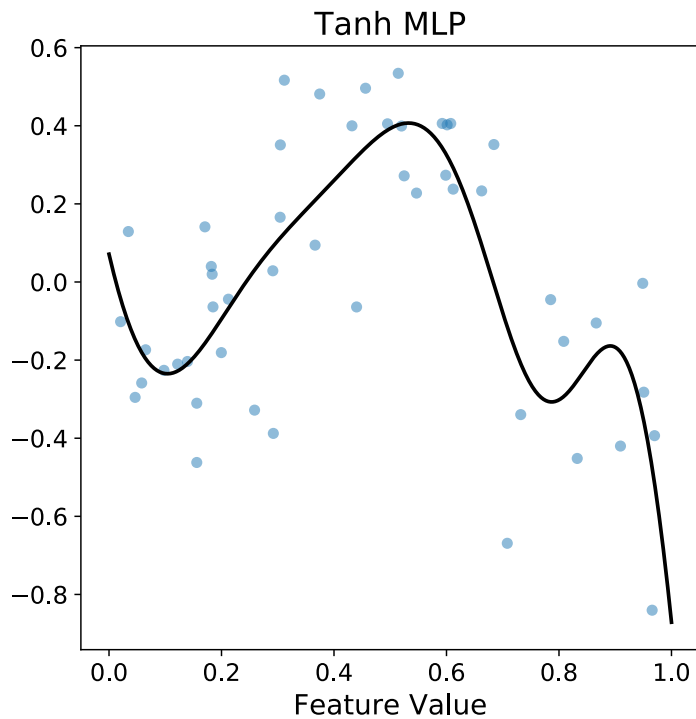


Removes vanishing gradients, but prefers that non-activated nodes be as “non-activated” as possible (doesn’t make much sense)

(Mass et al., 2013; He et al., 2015)



# Convergence Problems



Rudin and Carlson. The Secrets of Machine Learning: Ten Things You Wish You Had Known Earlier to be More Effective at Data Analysis. INFORMS TutORial, 2019.

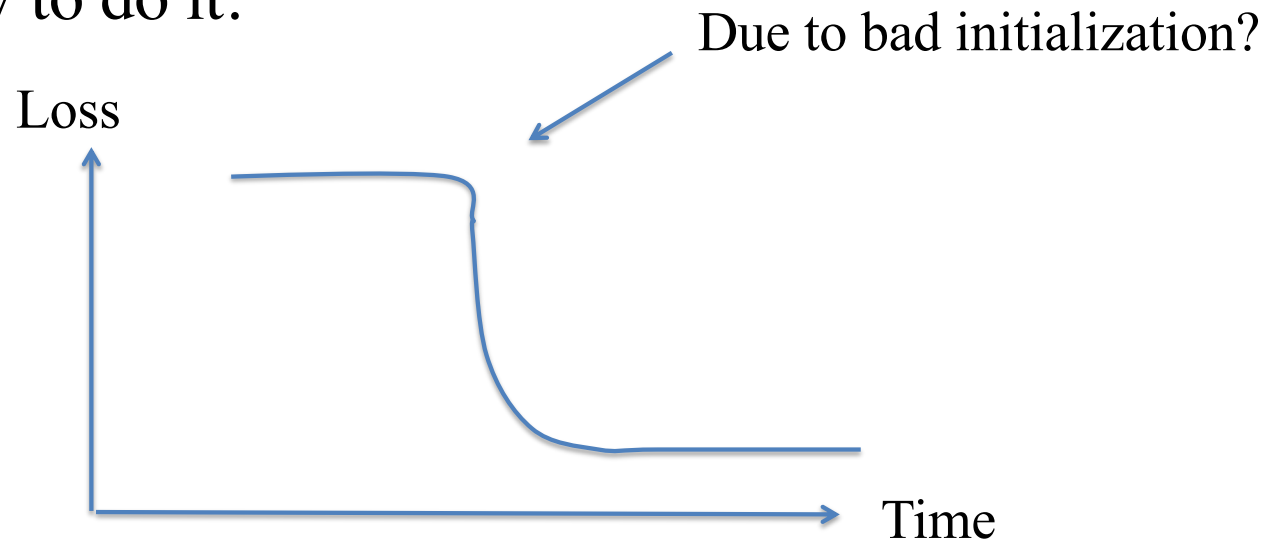
# Convergence Problems

Adding momentum to gradients

- adjust gradient to make current gradient similar to previous gradients

# Convergence Problems

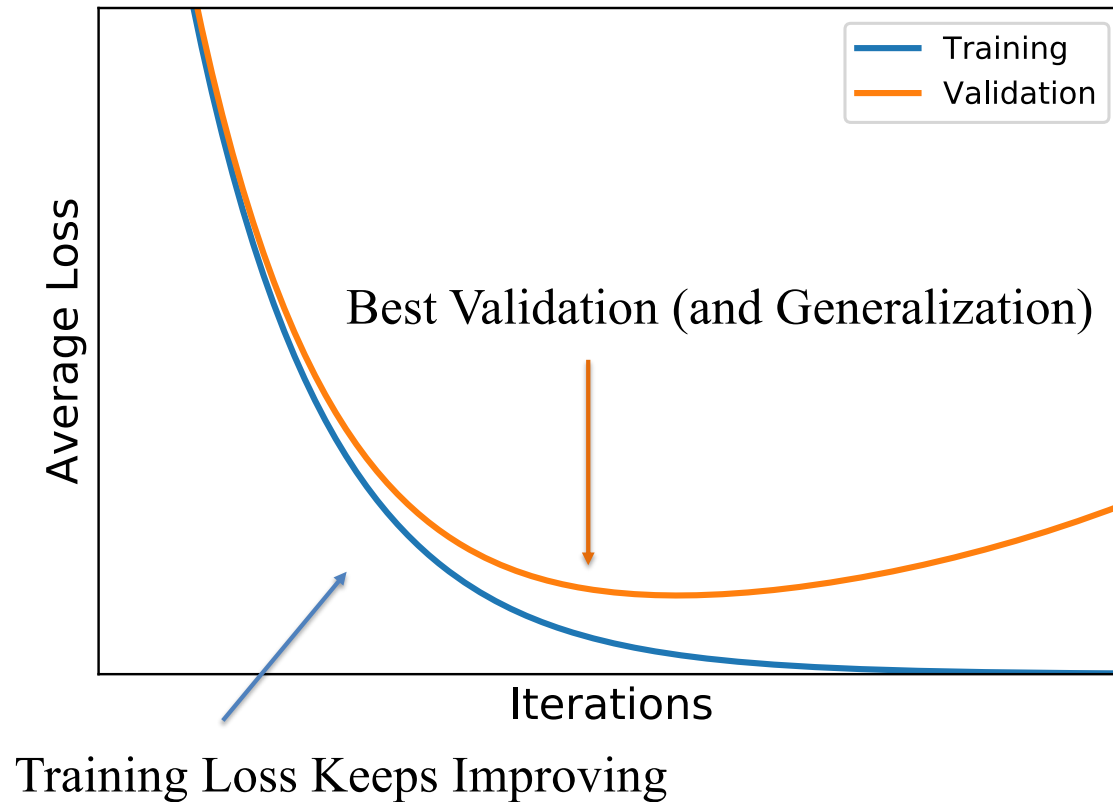
- **Initialization** of the networks weights is really important. I have no idea how to do it.



# Convergence Problems

- **Batch Normalization** (Ioffe and Szegedy, 2015) is a step that:
  - Normalizes the outputs  $o_i$  of several nodes (a “mini-batch”) in the same layer. (As usual, subtract the mean of the  $o_i$ ’s divide by their standard deviation).
  - Includes the mean and standard deviation as separate parameters to be learned.
  - Usually the normalization is before the nonlinear activation function.
  - This adds regularization and helps to prevent flat gradients in the network but sometimes it messes things up.

# Early stopping via validation set



Rudin and Carlson. The Secrets of Machine Learning: Ten Things You Wish You Had Known Earlier to be More Effective at Data Analysis. INFORMS TutORial, 2019.

# Convergence Problems Summary

- There are lots of convergence problems
- vanishing gradients
  - Adjust the learning rate
  - Change the activation function (tanh, ReLU, leaky ReLU, etc.)
  - Use Batch Norm
  - Add Momentum
- bad minima
  - Initialization (somehow...)
- overfitting
  - Stop early using validation set

# Convergence Problems Summary

When training a NN, you “become” part of the algorithm because you control its convergence so heavily.





# Convolutional neural networks and the intuition behind their architectures

Cynthia Rudin

Duke Machine Learning

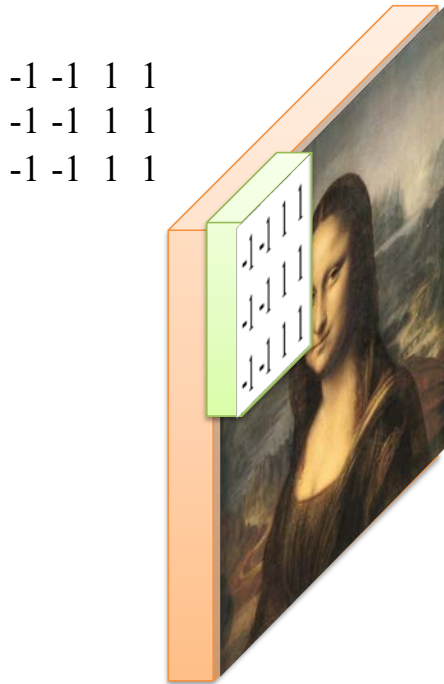
# Convolutional NN's

- Convolve means to slide the filter over all spatial locations and sum up the filter weights times the inputs.



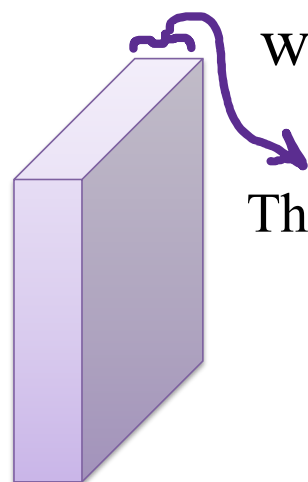
# Convolutional NN's

- Convolve means to slide the filter over all spatial locations and sum up the filter weights times the inputs.
- An edge filter will detect edges.



# Convolutional NN's

- Convolve means to slide the filter over all spatial locations and sum up the filter weights times the input.



- Stride of 5 means we step by 5's when we convolve.

The thickness is the number of filters

The following layer is smaller by a factor of 5.

# Convolutional NN's

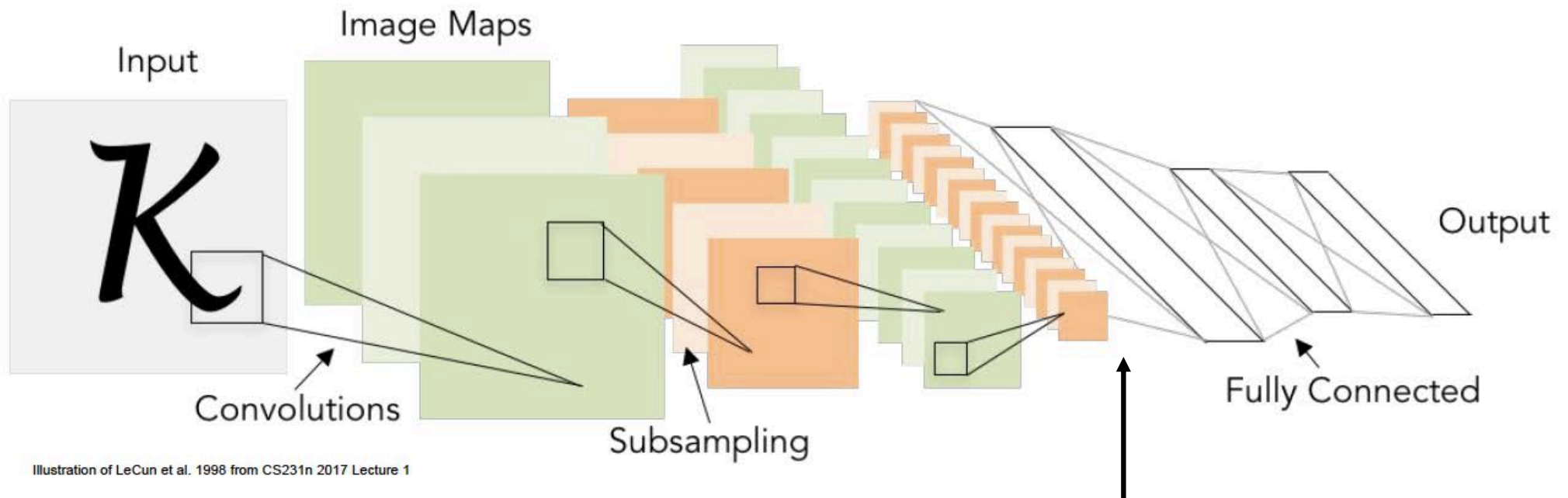
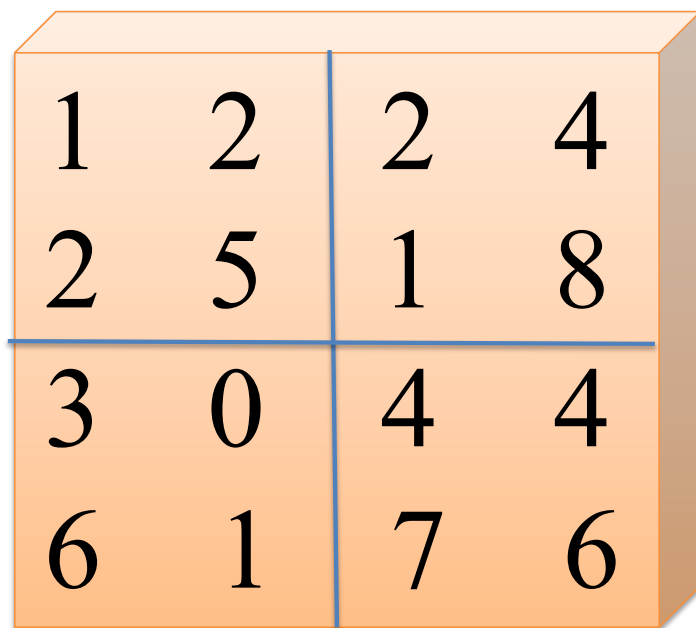


Illustration of LeCun et al. 1998 from CS231n 2017 Lecture 1

Image from LeCun et al 1998, reproduced in color from Li, Johnson, Yeung, 2017

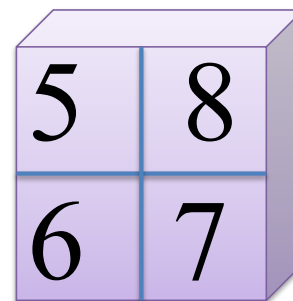
# Convolutional NN's

- **Max pooling** means to convolve with a max function.
- Intuitively keeps track of whether an earlier filter has detected something.



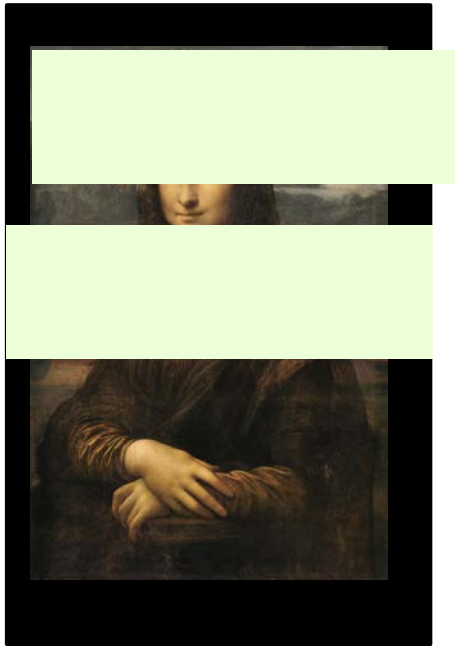
1	2	2	4
2	5	1	8
3	0	4	4
6	1	7	6

2 x 2 max pool filter and stride 2



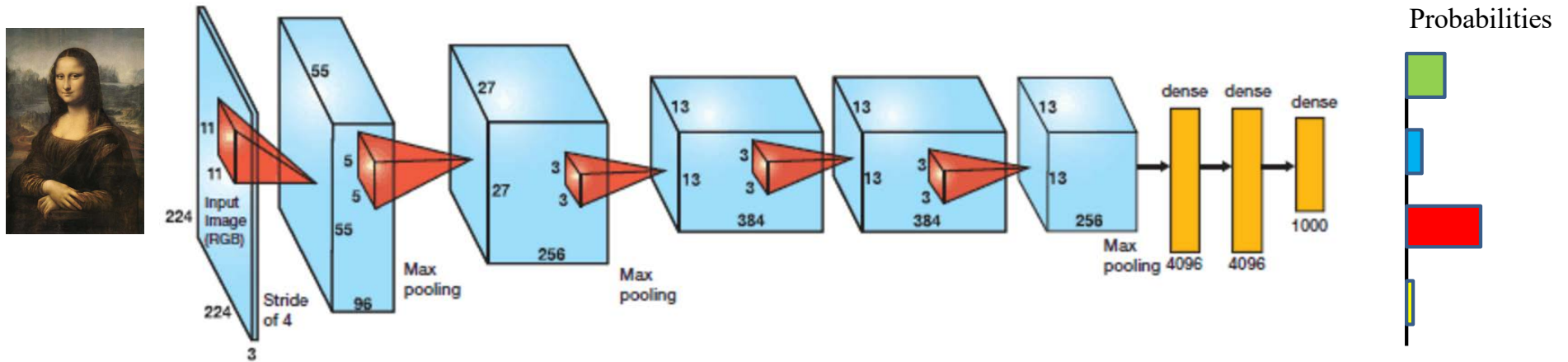
5	8
6	7

# Zero-padding



- Add zeros around the image so that the dimensions work out.

- AlexNet (Krizhevsky et al. 2012)

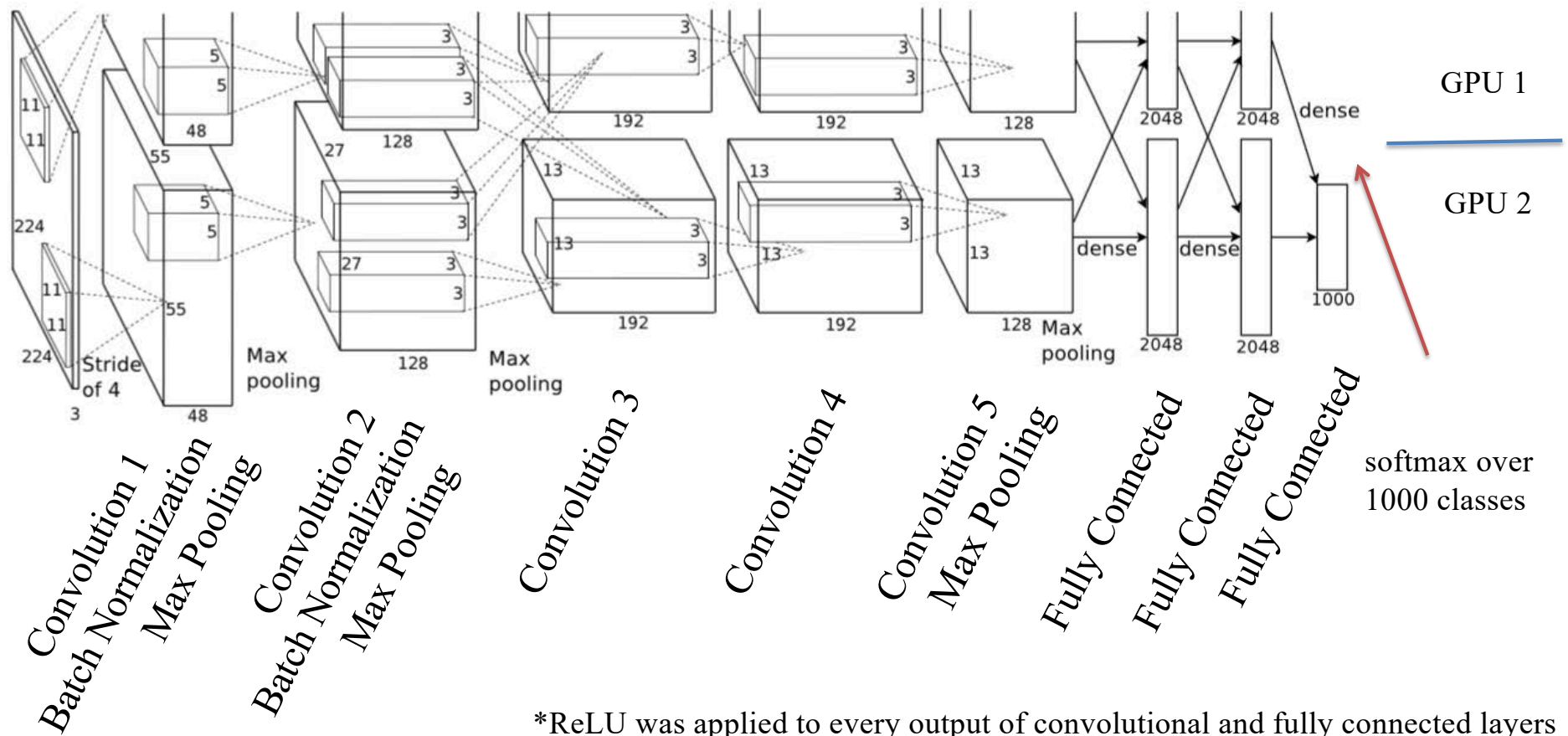


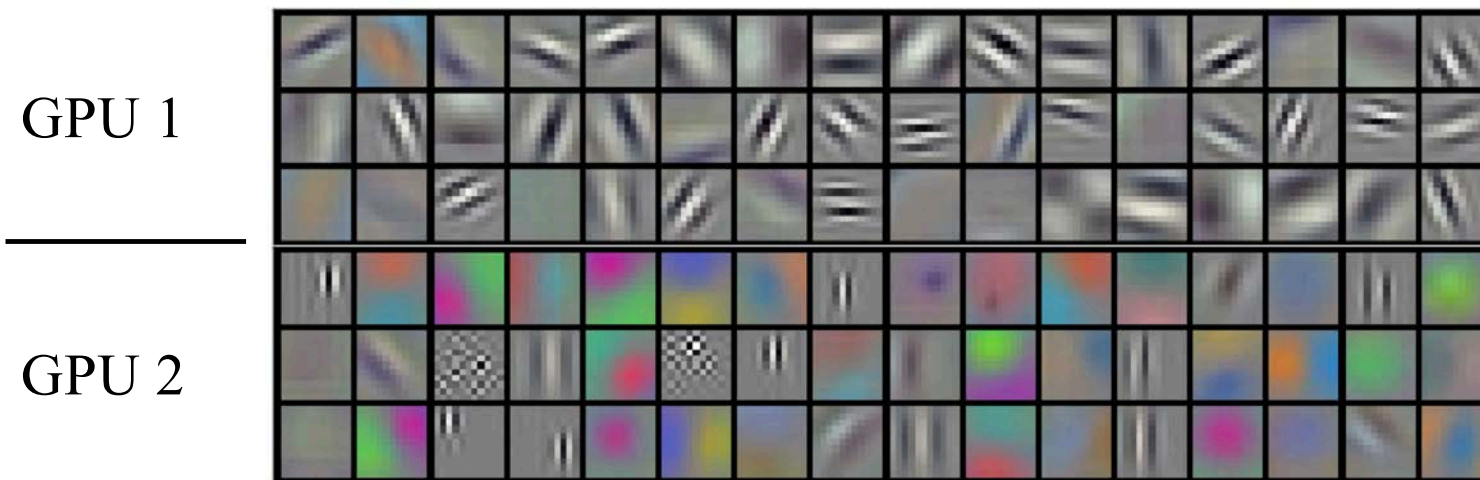
AlexNet won the ImageNet Large Scale Visual Recognition Challenge in 2012. It achieved a top-5 error of 15.3%, more than 10.8 percentage points ahead of the runner up.

Image source: unknown



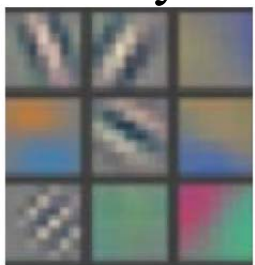
- AlexNet (Krizhevsky et al. 2012)



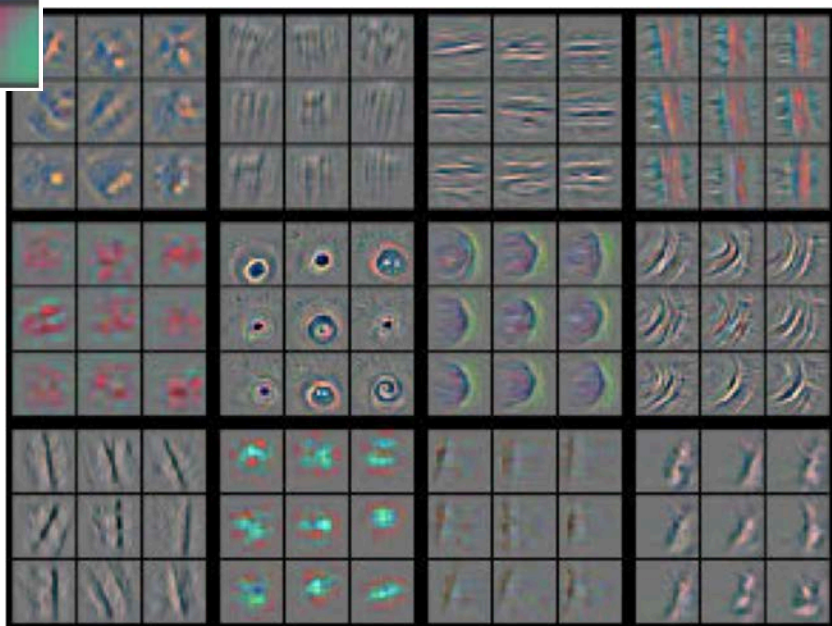


Layer 1 AlexNet filters (Krizhevsky et al. 2012)

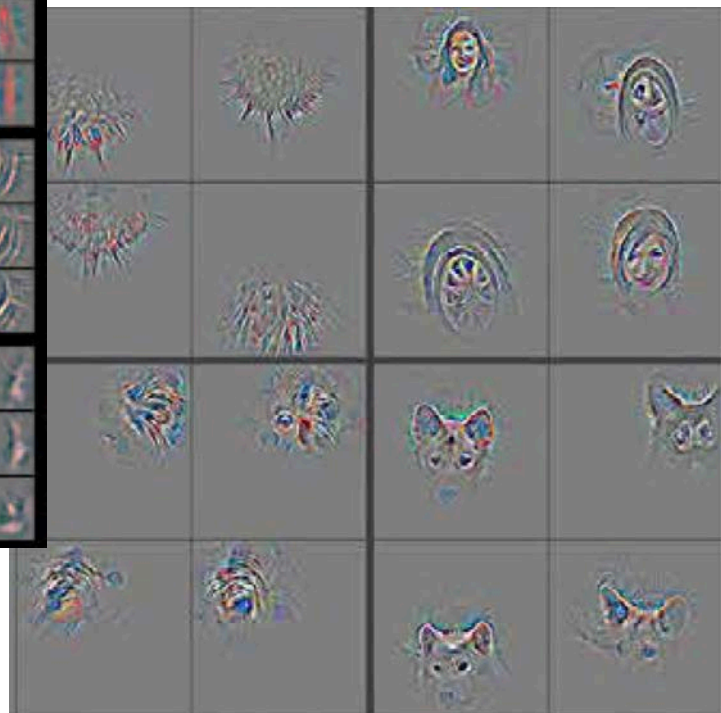
from layer 1



from layer 2



from layer 5



Source: Zeiler and Fergus, 2013

# Convolutional NN's

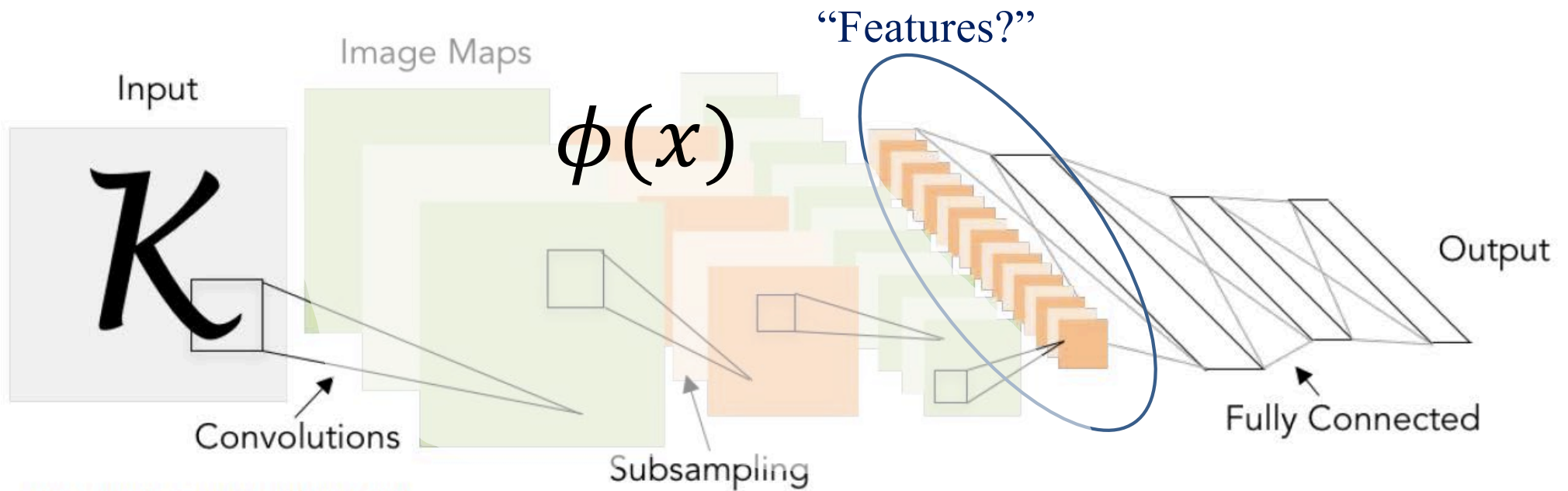
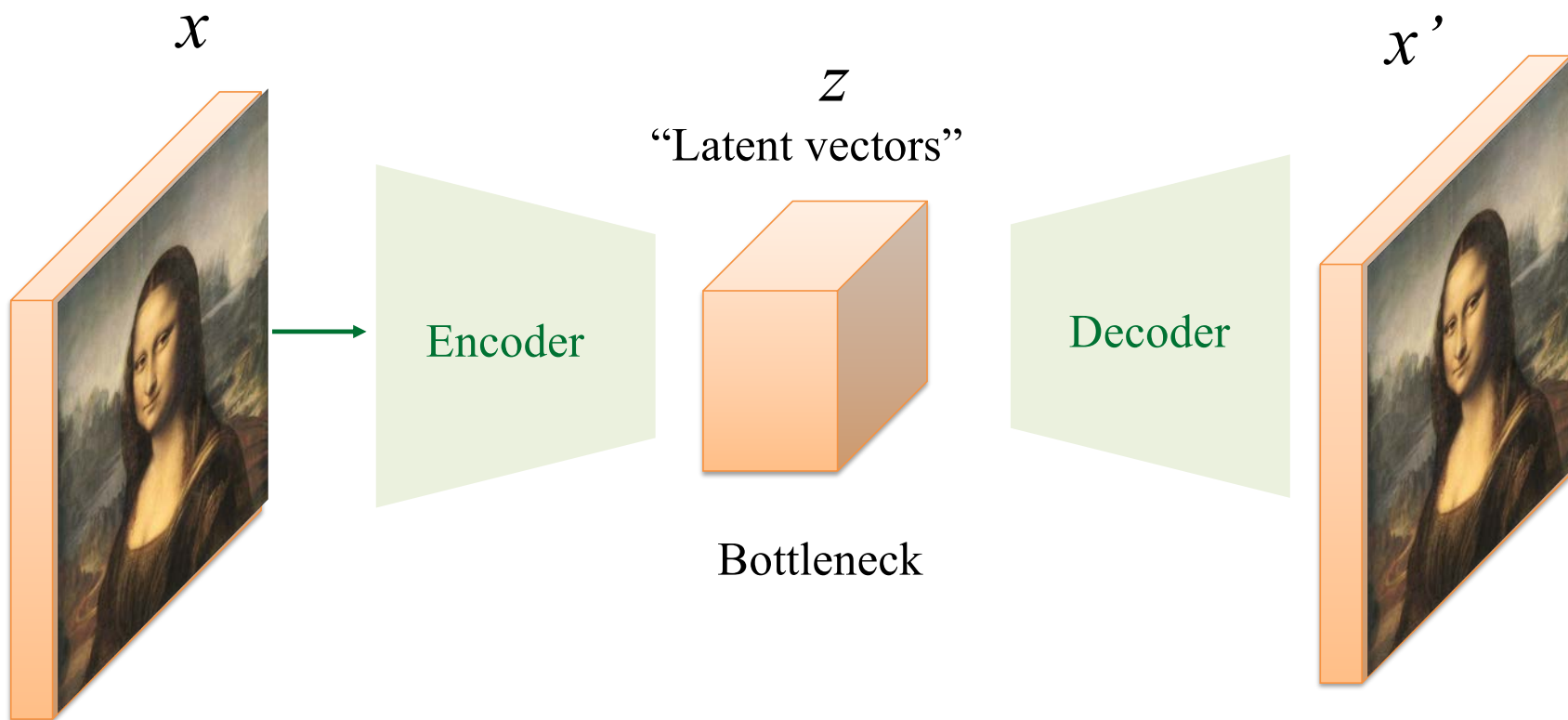


Illustration of LeCun et al. 1998 from CS231n 2017 Lecture 1

Image from LeCun et al 1998, reproduced also from Li, Johnson, Yeung, 2017

# Autoencoders



There has been much work since AlexNet.

Next: Improving performance of CNNs for computer vision.



# Improving Performance of Neural Networks

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# Data Augmentation



Chinese Lantern Festival, Cary NC, 2017

# Data Augmentation

- include artificial data, such as horizontal flips, rotations, resized, cropped training images, change contrast and brightness, distortion, etc.



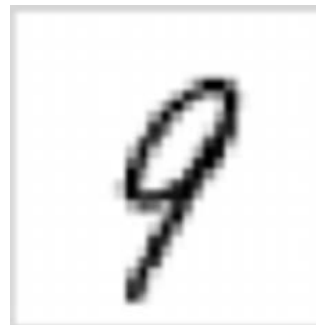
Chinese Lantern Festival, Cary NC, 2017

# Data Augmentation

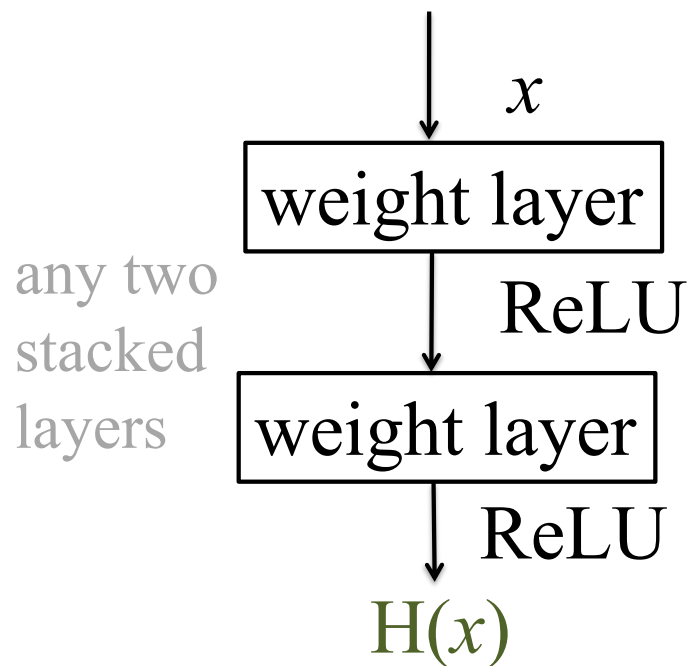
- include artificial data, such as horizontal flips, rotations, resized, cropped training images, change contrast and brightness, distortion, etc.



Chinese Lantern Festival, Cary NC, 2017



# Residual Nets (He et al., 2016)

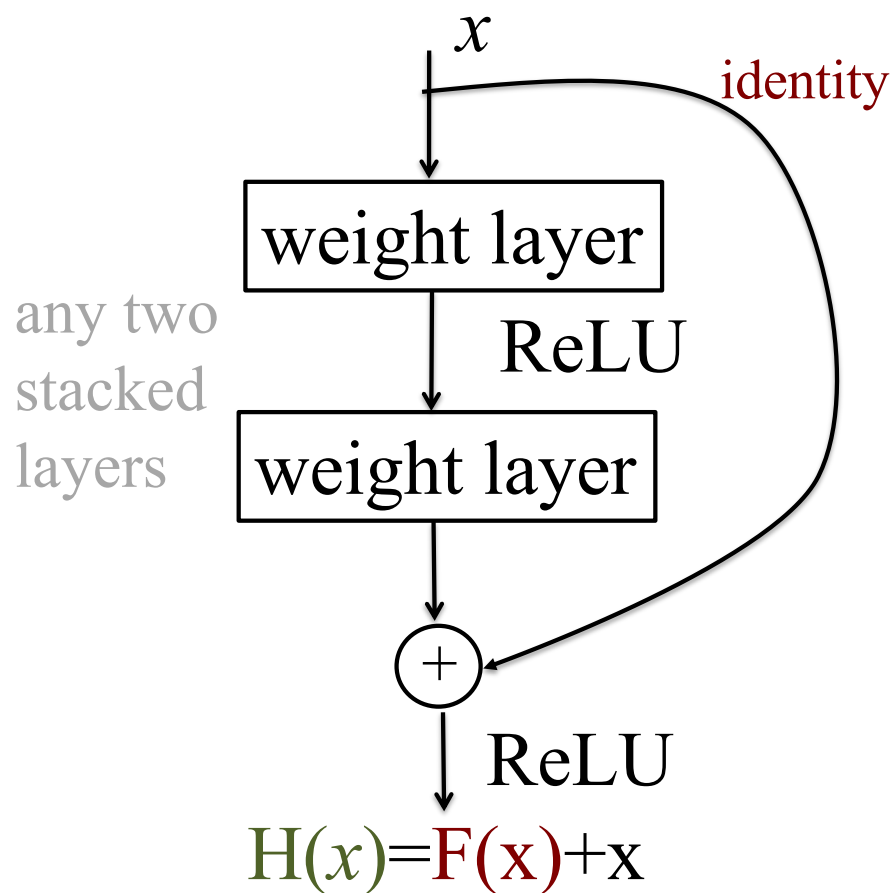


~~We hope to fit  $H(x)$ .~~

Slides recreated from Kaiming He's tutorial

[http://kaiminghe.com/icml16tutorial/icml2016\\_tutorial\\_deep\\_residual\\_networks\\_kaiminghe.pdf](http://kaiminghe.com/icml16tutorial/icml2016_tutorial_deep_residual_networks_kaiminghe.pdf)

# Residual Nets



~~We hope to fit  $H(x)$ .~~

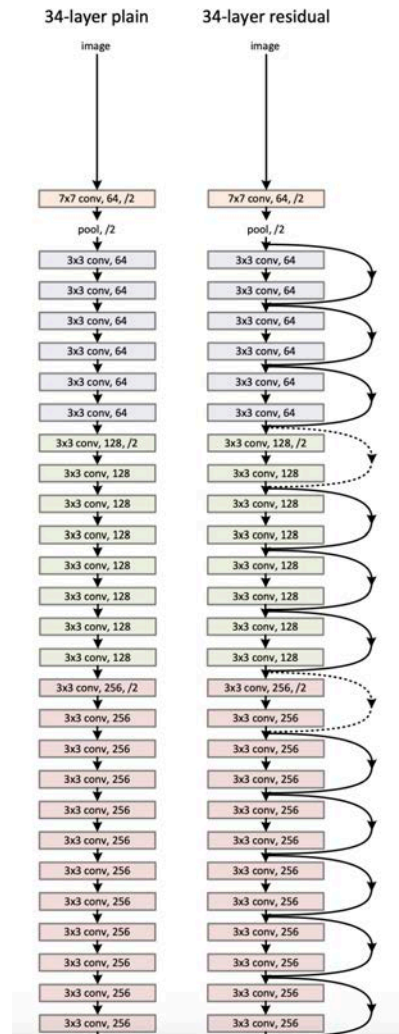
We hope to fit  $F(x)$ .  
We are now learning a residual of identity.

# Residual Nets

- By adding  $x$ , the derivative of the error with respect to  $x$  increases by 1. Thus, less vanishing derivatives.
- Allowed networks to go much deeper than before.  
“From 10 to 1000 layers”

$$H(x) = F(x) + x$$

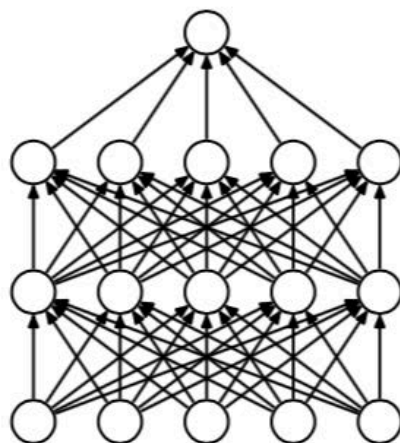
# Residual Nets



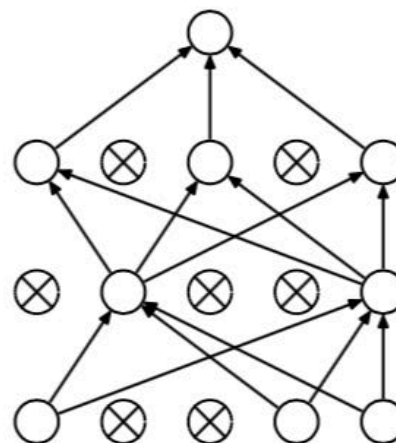
He et al. Deep Residual Learning for Image Recognition, arXiv2015

# Dropout (Srivastava et al., JMLR 2014)

- Forces signal to be “carried” throughout the network
- In each forward pass, for each neuron, with probability  $p$ , set all of its output weights to 0.
- $p$  is a hyperparameter, usually  $p = 0.5$ .
- During testing, use all nodes.



(a) Standard Neural Net



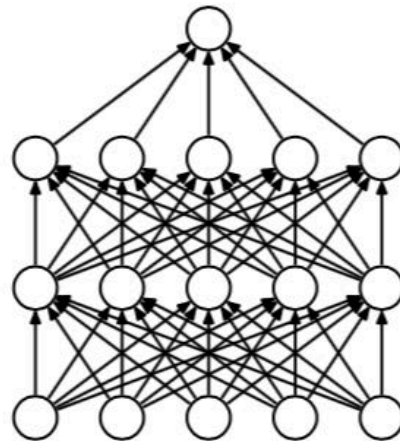
(b) After applying dropout.

Image from Srivastava et al JMLR 2014)

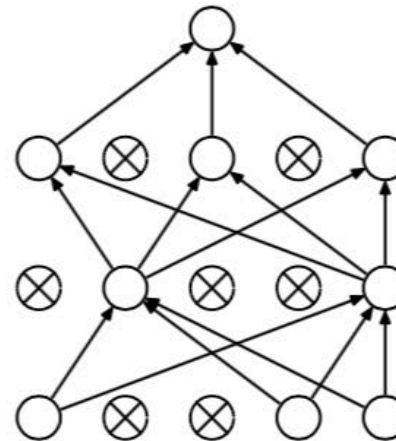


# Dropout (Srivastava et al., JMLR 2014)

- As if we are training exponentially many “sub” models. Similar idea to bagging (averaging many separately trained models together).
- Creates a redundant encoding.



(a) Standard Neural Net

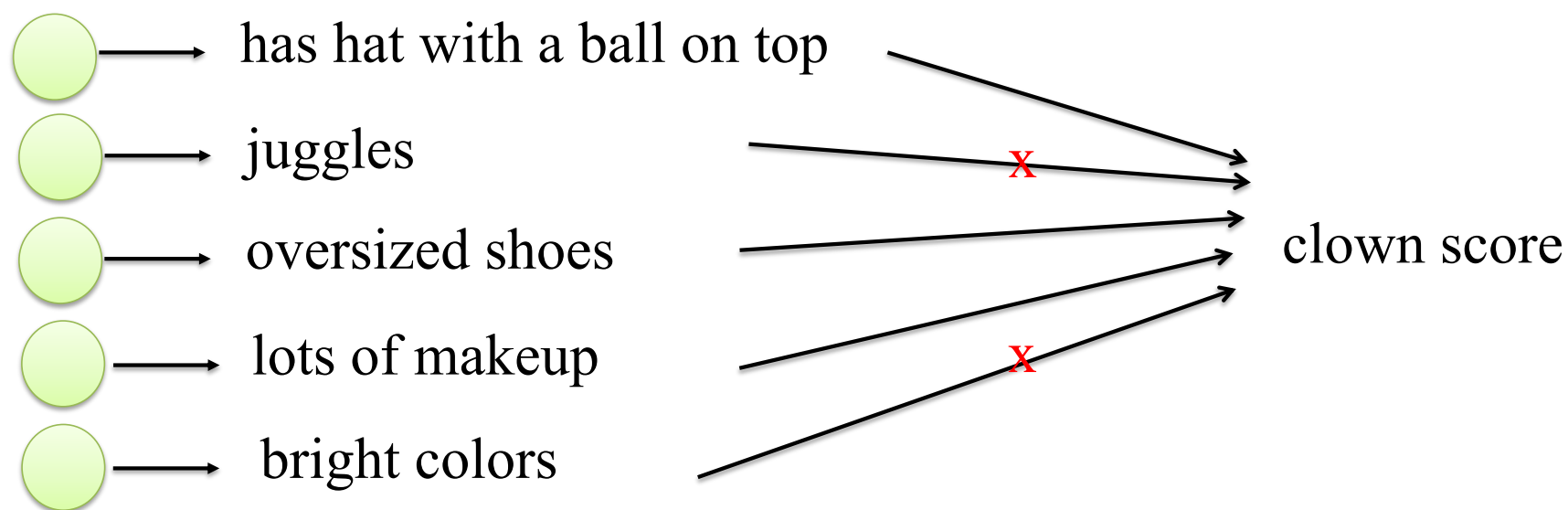


(b) After applying dropout.

Image from Srivastava et al JMLR 2014)

# Dropout (Srivastava et al., JMLR 2014)

- As if we are training exponentially many “sub” models. Similar idea to bagging (averaging many separately trained models together).
- Creates a redundant encoding.



# “Transfer” Learning

- Using information about the solution to one problem to help solve another.
- Use the early layers from a pretrained model in another network. Retrain only the weights from the last few layers.

Published as a conference paper at ICLR 2015

---

VERY DEEP CONVOLUTIONAL NETWORKS  
FOR LARGE-SCALE IMAGE RECOGNITION

← VGG

Karen Simonyan\* & Andrew Zisserman\*  
Visual Geometry Group, Department of Engineering Science, University of Oxford  
{karen,az}@robots.ox.ac.uk

# A Big Bag of Tricks

- Dropout
- Batch Normalization
- Data Augmentation
- Residual Networks
- Activation Functions (ReLU, Leaky ReLU)
- Initialization
- Transfer Learning
- :

## Other ways to improve neural networks

- Change the dataset. Use fine-grained labels



Is there a fence in this picture?

- Understand the model so you know what's wrong with it.



# Warnings about Neural Networks for Computer Vision

Cynthia Rudin

Duke Machine Learning

CNNs can use the wrong information  
(confounding)



# CNNs can use the wrong information (confounding)



Source: Wikimedia commons, West German soldiers in 1983

Ok, well, that was a bad dataset...

# CNNs can use the wrong information (confounding)



[NPJ Digit Med](#). 2019; 2: 31.

PMCID: PMC6550136

Published online 2019 Apr 30. doi: [10.1038/s41746-019-0105-1](https://doi.org/10.1038/s41746-019-0105-1)

PMID: [31304378](https://pubmed.ncbi.nlm.nih.gov/31304378/)

## Deep learning predicts hip fracture using confounding patient and healthcare variables

[Marcus A. Badgeley](#),<sup>1,2,3</sup> [John R. Zech](#),<sup>4</sup> [Luke Oakden-Rayner](#),<sup>5</sup> [Benjamin S. Glicksberg](#),<sup>6</sup> [Manway Liu](#),<sup>1</sup> [William Gale](#),<sup>7</sup> [Michael V. McConnell](#),<sup>1,8</sup> [Bethany Percha](#),<sup>2</sup> [Thomas M. Snyder](#),<sup>1</sup> and [Joel T. Dudley](#)<sup>2,3</sup>

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Solution to this? Interpretability? Heavy testing? Massive data augmentation?

Deep fakes are dangerous

# Deep fakes are dangerous

## UW NEWS

[ENGINEERING](#) | [NEWS RELEASES](#) | [RESEARCH](#) | [SCIENCE](#) | [TECHNOLOGY](#)

July 11, 2017

### Lip-syncing Obama: New tools turn audio clips into realistic video

[Jennifer Langston](#)

UW News



University of Washington researchers have developed new algorithms that solve a thorny challenge in the field of computer vision: [turning audio clips into a realistic, lip-synced video](#) of the person speaking those words.



## Deepfakes and the New AI-Generated Fake Media Creation-Detection Arms Race

Manipulated videos are getting more sophisticated all the time—but so are the techniques that can identify them


# Deep fakes are dangerous

www.forbes.com/sites/jessedamiani/2019/09/03/a-voice-deepfake-was-11


**Forbes**

36,789 views | Sep 3, 2019, 04:42pm EDT

## A Voice Deepfake Was Used To Scam A CEO Out Of \$243,000

 **Jesse Damiani** Contributor ©  
Consumer Tech  
*I cover the human side of VR/AR, Blockchain, AI, Startups, & Media.*

f  
t  
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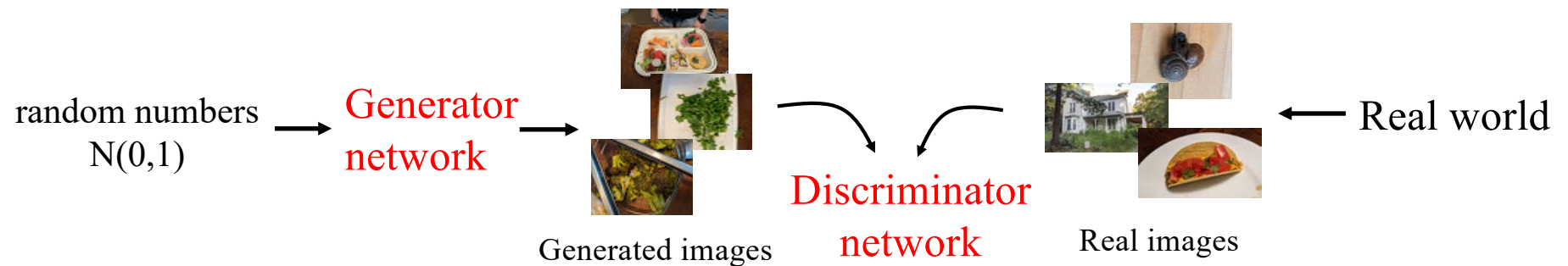


Anonymous hacker programmer uses a laptop to hack the system in the dark. Creation and infection of ... [+] GETTY

**It's the first noted instance of an artificial intelligence-generated voice deepfake used in a scam.**

# GANs – Generative Adversarial Networks

- GANs are actor-critic models
- They produce realistic-looking images/data
- Used commonly for AI artwork / deep fakes



If the generator creates images that the discriminator can't tell apart, it's good.  
(The “arms race” is between the generators and the discriminators.)

(Goodfellow et al 2014)

# GANs – Generative Adversarial Networks

From Goodfellow et al 2014:

$D$  and  $G$  play the following two-player minimax game with value function  $V(G, D)$ :

$$\min_G \max_D V(D, G) = \mathbb{E}_{\mathbf{x} \sim p_{\text{data}}(\mathbf{x})} [\log D(\mathbf{x})] + \mathbb{E}_{\mathbf{z} \sim p_{\mathbf{z}}(\mathbf{z})} [\log(1 - D(G(\mathbf{z})))].$$



Discriminator maximizes  
likelihood of real data



Discriminator minimizes  
likelihood of generated data.



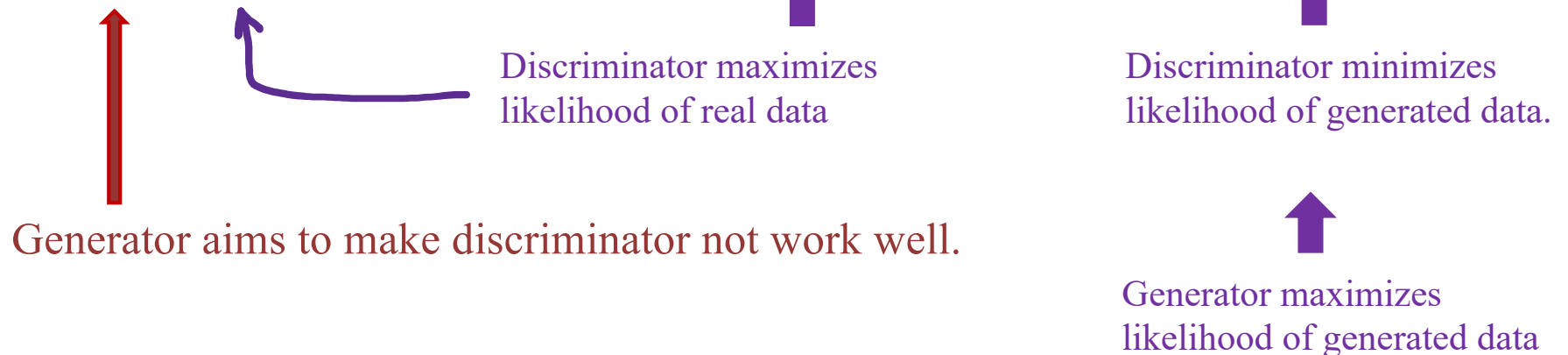
Generator maximizes  
likelihood of generated data

# GANs – Generative Adversarial Networks

From Goodfellow et al 2014:

$D$  and  $G$  play the following two-player minimax game with value function  $V(G, D)$ :

$$\min_G \max_D V(D, G) = \mathbb{E}_{\mathbf{x} \sim p_{\text{data}}(\mathbf{x})} [\log D(\mathbf{x})] + \mathbb{E}_{\mathbf{z} \sim p_{\mathbf{z}}(\mathbf{z})} [\log(1 - D(G(\mathbf{z})))].$$





# GANs – Generative Adversarial Networks

From Goodfellow et al 2014:

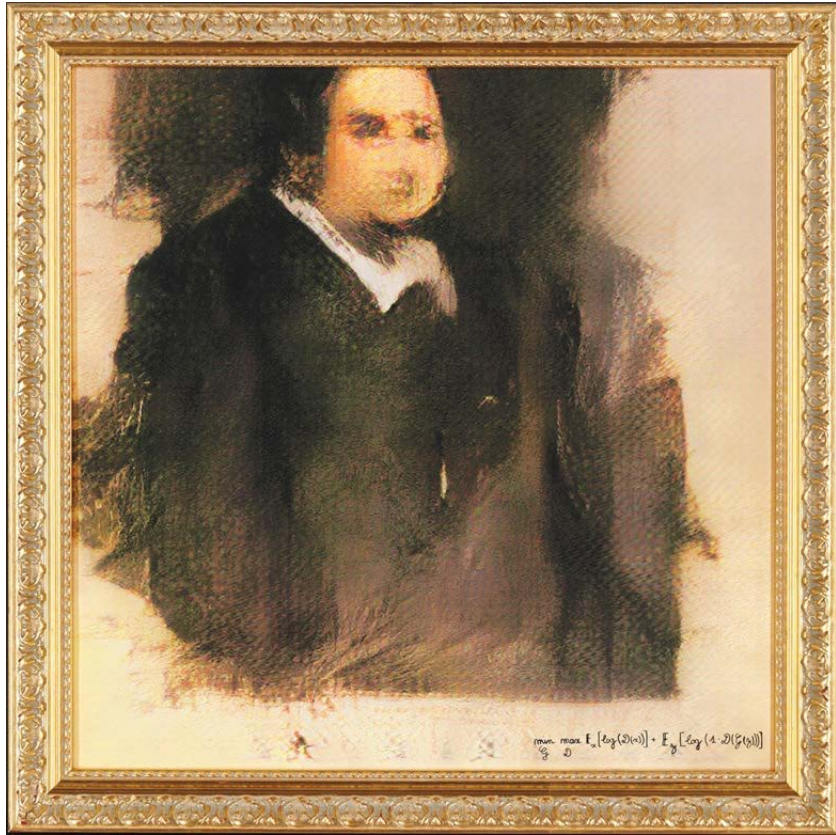
$D$  and  $G$  play the following two-player minimax game with value function  $V(G, D)$ :

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$$\max_G \mathbb{E}_{\mathbf{z} \sim p_{\mathbf{z}}(\mathbf{z})} [\log(\cancel{1 - D(G(\mathbf{z}))})].$$

Gradient ascent steps on discriminator

Gradient descent steps on generator



## Is artificial intelligence set to become art's next medium?

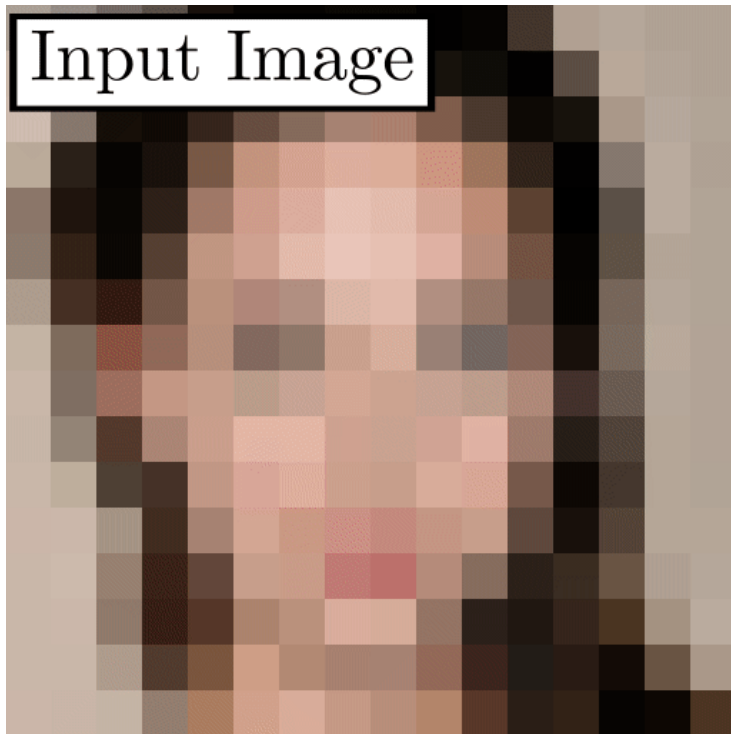
GANs are totally useful for artwork!

AI artwork sells for \$432,500 — nearly 45 times its high estimate — as Christie's becomes the first auction house to offer a work of art created by an algorithm



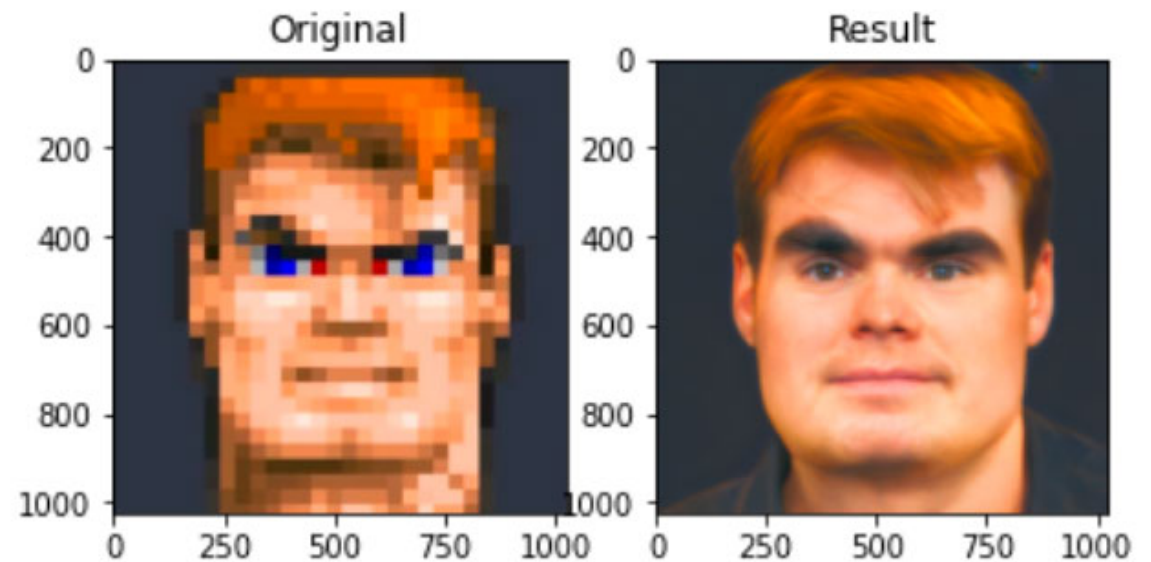
Figure adapted from L. Gatys et al. "[A Neural Algorithm of Artistic Style](#)" (2015) by Google AI Blog

GANs are totally useful for artwork!



Menon et al. PULSE: Self-Supervised Photo Upsampling via Latent Space Exploration of Generative Models, CVPR 2020

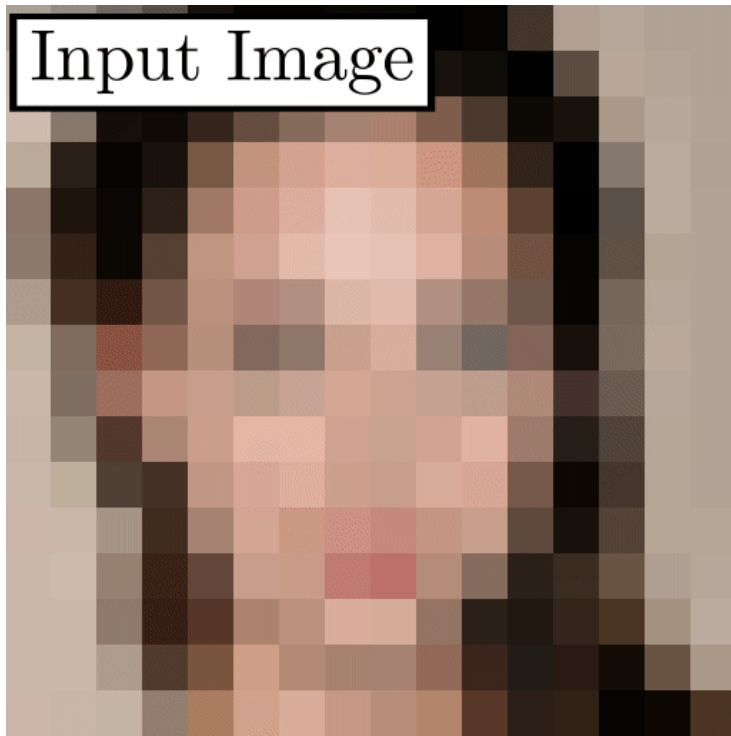
Tero Karras et al. A style-based generator architecture for generative adversarial networks. CVPR, 2019.



A twitter user's result from the PULSE algorithm, which uses StyleGAN

GANs are totally useful for artwork!





Menon et al. PULSE: Self-Supervised Photo Upsampling via Latent Space Exploration of Generative Models, CVPR 2020

Tero Karras et al. A style-based generator architecture for generative adversarial networks. CVPR, 2019.

PULSE shows us that there is often no hope of identifying someone in a grainy security video.

There could be many high res images corresponding to one low res image.

GANs are totally useful for artwork!

# Neural networks can be brittle

- Adversarial attacks show that changing a *single pixel* in an image can change the predicted class in modern ML systems.
- It is easy to fool a computer vision system.



?



Need better data augmentation...

Eykholt et al., 2018 **Robust Physical-World Attacks on Deep Learning Models**,

# The model will not always be used in the way it is intended

[VIDEO](#)[LIVE](#)[SHOWS](#)[2020 ELECTIONS](#)[CORONAVIRUS](#)

## Black man wrongfully arrested because of incorrect facial recognition

*Robert Williams spent nearly 30 hours in a detention center.*

By [Ella Torres](#)

June 25, 2020, 2:01 PM • 6 min read



# So...

- Much care is needed in many applications of neural networks.
  - medical image processing (confounding)
  - automated driving systems (not robust, not perfect)
  - facial recognition (not perfect, watch for bias)
  - deep fakes (easily fraudulent)
- Neural networks are great for artwork.