

16.3-5 Give an $O(n^2)$ algorithm to find the longest monotonically increasing sequence in a sequence of n numbers.

Build an example first: (5, 2, 8, 7, 1, 6, 4)

Ask yourself what would you like to know about the first $n - 1$ elements to tell you the answer for the entire sequence?

1. The length of the longest sequence in s_1, s_2, \dots, s_{n-1} .
(seems obvious)
2. The length of the longest sequence s_n will extend!
(not as obvious - this is the idea!)

Let s_i be the length of the longest sequence ending with the i th character:

sequence	5	2	8	7	3	1	6	4
s_i	1	1	2	2	2	1	3	3

How do we compute s_i ?

$$s_i = \max_{0 < j < i, seq[j] < seq[i]} s_j + 1$$

$$s_0 = 0$$

To find the longest sequence - we know it ends somewhere, so Length = $\max_{i=1}^n s_i$