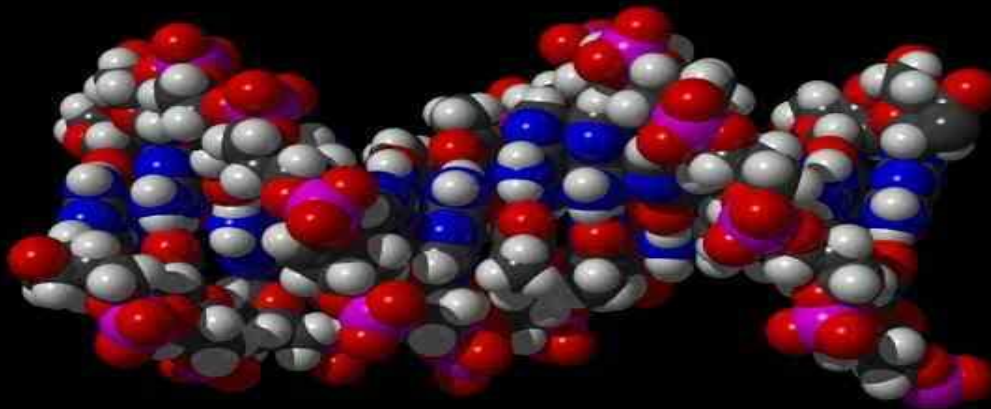


Adleman's First Demonstration of DNA Computing

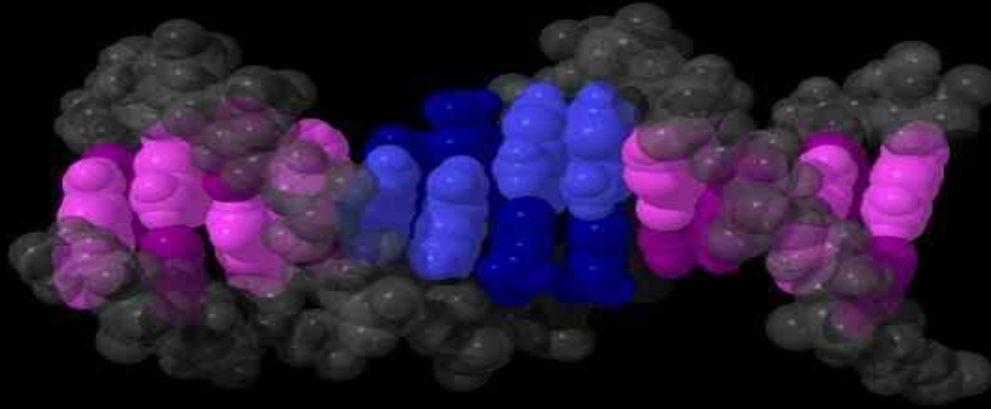
Adapted from PPT of Thierry Metais
& Jaeyeon Jung and Jaehong Lim

Introduction to DNA:

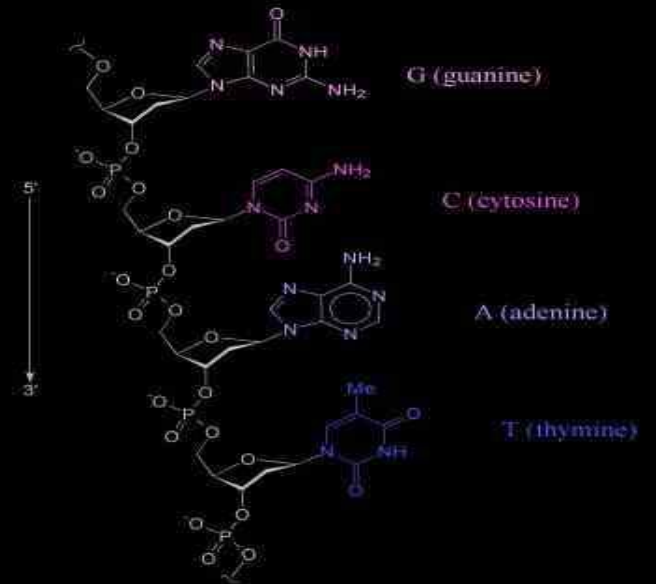
DNA (deoxyribonucleic acid)



Spacefill-model of synthetic B-DNA with sequence CGCGAATTCGCG.



This spacefill-model clearly shows the stacking of the bases along the DNA-backbone.



The linear hydrogen bonds between the complementary bases.

Computing with DNA

- Invented (discovered?) by Dr. Leonard M. Adleman of USC in 1994, a computer scientist and mathematician
- Basic Idea: Perform **molecular biology** experiment to find solution to **hard** problem.
- Use “Molecular Computer” (rather than using a conventional computer for solving “computational biology” problems)

Introduction:

- What is DNA computing ?
 - Around 1950 first idea (precursor Feynman)
 - First important experiment 1994: Leonard Adleman
- Molecular level (just greater than 10^{-9} meter)
- Massive parallelism.
 - In a liter of water, with only 5 grams of DNA we get around 10^{21} bases !
 - Each DNA strand represents a bit-level processor !

A bit of biology

- The DNA is a double stranded molecule.
- Each strand is based on 4 bases:
 - Adenine (A)
 - Thymine (T)
 - Cytosine (C)
 - Guanine (G)
- Those bases are linked through a sugar (desoxyribose)
- **IMPORTANT:**
 - The linkage between bases has a **direction**.
 - There are **complementarities** between bases (Watson-Crick).

(A) \leftrightarrow (T)

(C) \leftrightarrow (G)

DNA manipulations:

- If we want to use DNA as an information bulk, we must be able to manipulate it .
- However we are talking of handling molecules...
- So instead of using physical processes, we would have to use natural ones (**ENZYMES**), more effective:
 - for lengthening: **polymerases**...
 - for cutting: **nucleases** (exo/endo-nucleases)...
 - for linking: **ligases**...
- 1985: Kary Mullis invented PCR
 - Thank this reaction we get millions of identical strands, and we are allowed to think of massive parallel computing.

Coding the information:

- 1994: THE Adleman's experiment.
 - Given a *directed* graph can we find an hamiltonian path (more complex than the TSP).
 - In this experiment there are 2 keywords:
 - massive parallelism* (all possibilities are generated)
 - complementarity* (to encode the information)
- This experiment proved that DNA computing wasn't just a theoretical study but could be applied to real problems like cryptanalysis (breaking DES).

2. HAMILTONIAN PATH PROBLEM

- (Posed by William Hamilton)
- *Given a network of nodes and directed connections between them, is there a path through the network that begins with the start node and concludes with the end node visiting each node only once (“Hamiltonian path”)?*
- “Does a Hamiltonian path exist, or not?”

*Hamiltonian path **does** exist!*



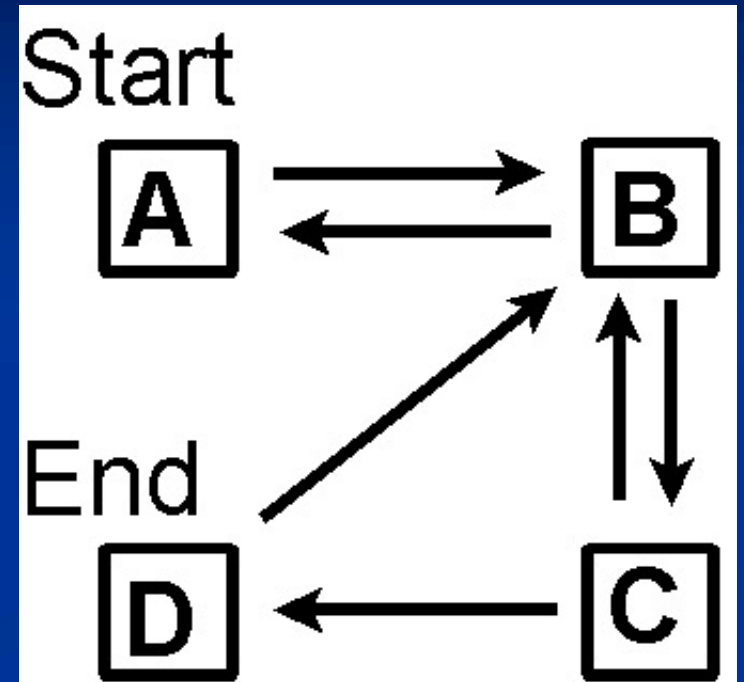
*Hamiltonian path **does not** exist!*



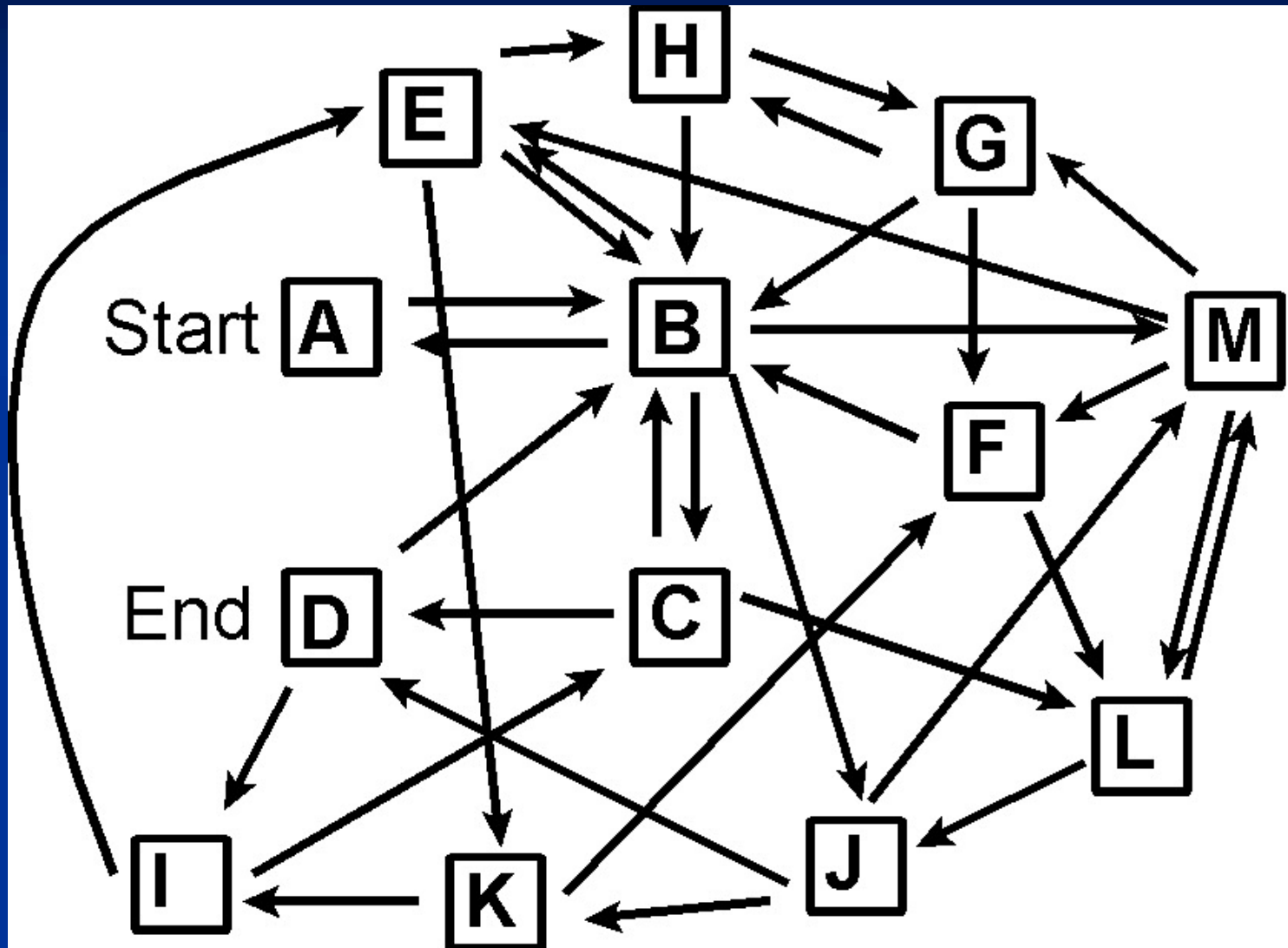
Solving the Hamiltonian Problem

- **Generation-&-Test Algorithm:**
- Step 1: Generate random paths on the network.
- Step 2: Keep only those paths that begin with start city and conclude with end city.
- Step 3: If there are N cities, keep only those paths of length N .
- Step 4: Keep only those that enter all cities at least once.
- Step 5. Any remaining paths are solutions (I.e., Hamiltonian

- [X] D -> B -> A
- [X] B -> C -> D ->
B -> A -> B
- [X] A -> B -> C ->
B
- [X] C -> D -> B ->
A
- [X] A -> B -> A ->
D
- [O] A -> B -> C ->
D



Does a Hamiltonian path exist for the following network?



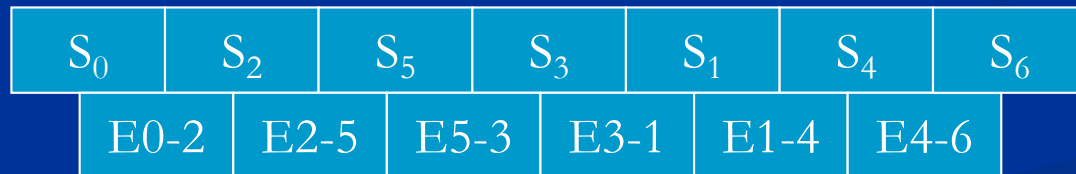
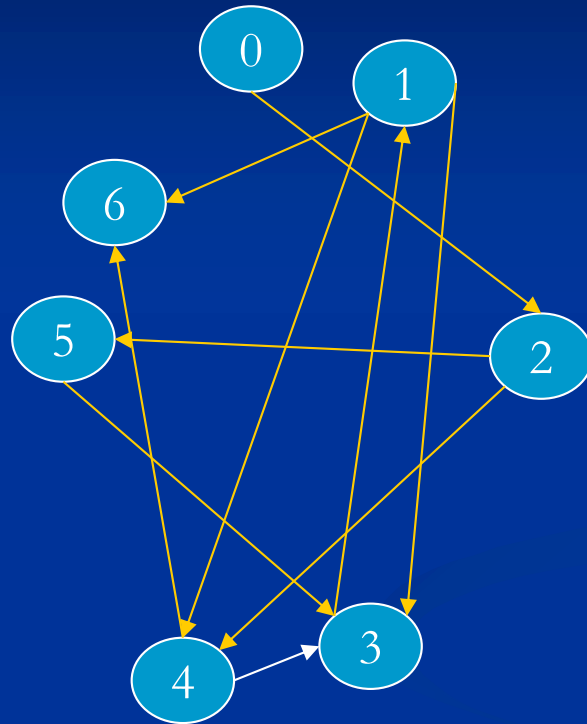
Combinatorial Explosion

- The Hamiltonian Problem is **NP-hard**, and
- The total number of paths grows exponentially as the network size increases
- For example:
 - 10^6 paths for $N=10$ cities,
 - 10^{12} paths ($N=20$),
 - 10^{100} paths!! ($N=100$)
- The *Generation- \mathcal{C} -Test* algorithm takes “forever”. Some sort of smart algorithm must be devised; none has been found so far (*NP-hard*).

Adleman experiment:

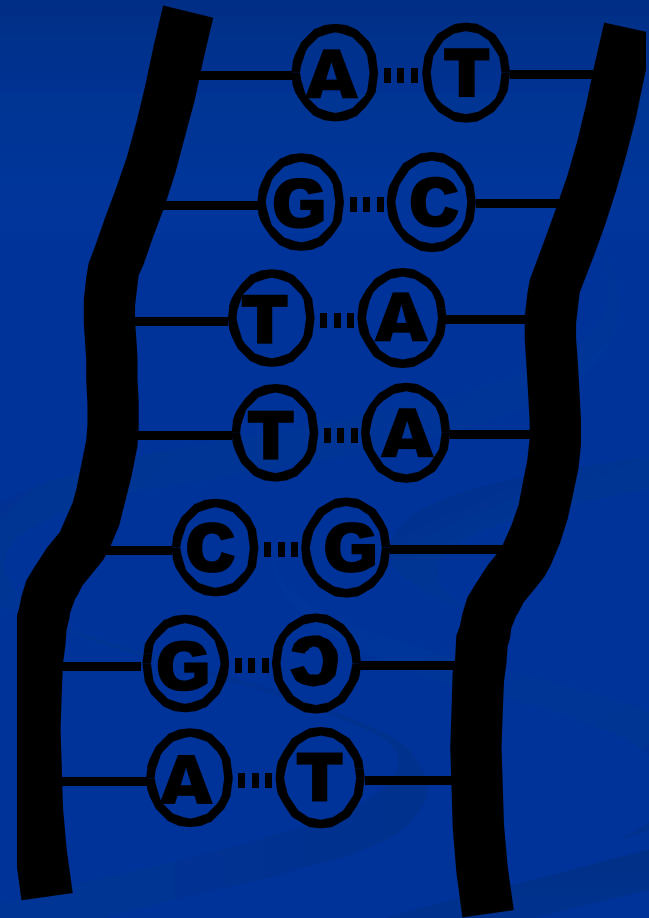
- Each node is coded randomly with 20 bases.
- Let S_i be a code, h be the complementarity mapping.
 $h(ATCG) = TAGC$.
- Each S_i is decomposed into 2 sub strands of length 10:
$$S_i = S_i' S_i''$$
- Edge(i,j) will be encode as $h(S_i'' S_j')$ (preserve edge orientation).
- **Code:**
 - Input(N) // All vertices and edges are mixed, *Nature is working*
 - $N \leftarrow B(N, S_0)$ // S_0 was chosen as input vertex.
 - $N \leftarrow E(N, S_4)$ // S_4 was chosen as output vertex.
 - $N \leftarrow E(N, \leq 140)$ // due to the size of the coding.
 - For $i=1$ to 5 do $N \leftarrow +N(N, S_i)$ // Testing if Hamiltonian path
 - Detect(N) // conclusion ...

Example:



3. FINDING SOLUTION WITH DNA EXPERIMENT

- DNA is a double-strand polymer made up of alternating series of four bases, A, T, C, G.
- DNA makes multiple copies of itself during cell differentiation.



DNA for Hamiltonian Problem

- The key to solving the problem is using DNA to perform the five steps of the Generation-&-Test algorithm in **parallel search**, instead of serial search.

Solving the Hamiltonian Problem

Generation-Test Algorithm:

Step 1: Generate random paths on the network.

Step 2: Keep only those paths that begin with the start city and conclude with the end city.

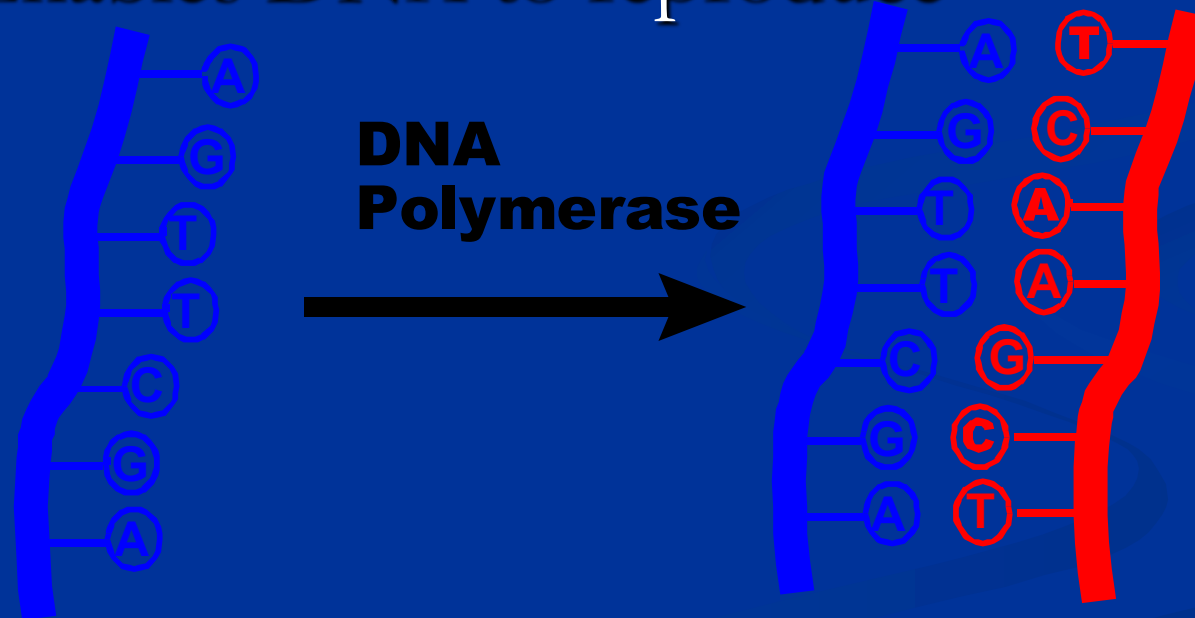
Step 3: If there are N cities, keep only those paths of length N .

Step 4: Keep only those paths that enter all cities at least once.

Step 5. Any remaining paths are solutions.

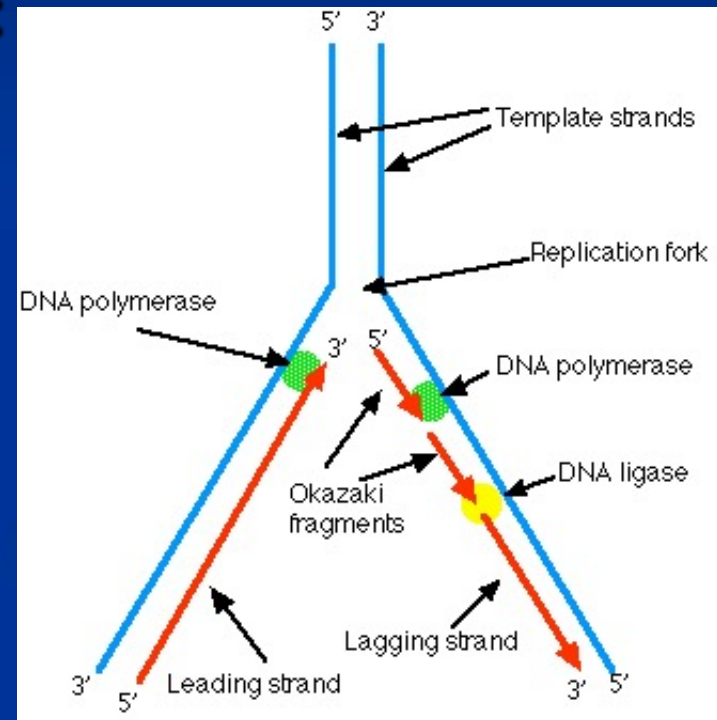
DNA Polymerase

- - Protein that produces complementary DNA strand
- - A -> T, T -> A, C -> G, G -> C
- - Enables DNA to reproduce



Polymerase in Action

- The “Bio” nano-machine:
 - *hops* onto DNA strand
 - *slides* along
 - *reads* each base
 - *writes* its complement onto new strand

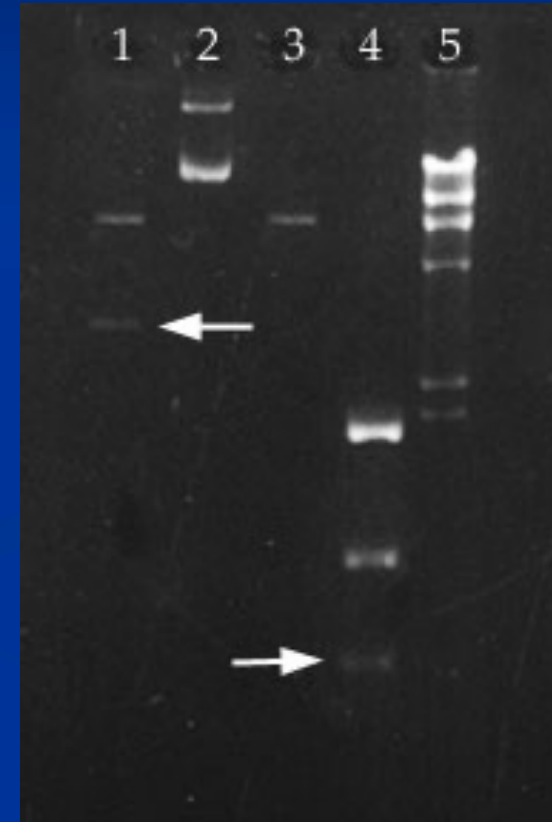
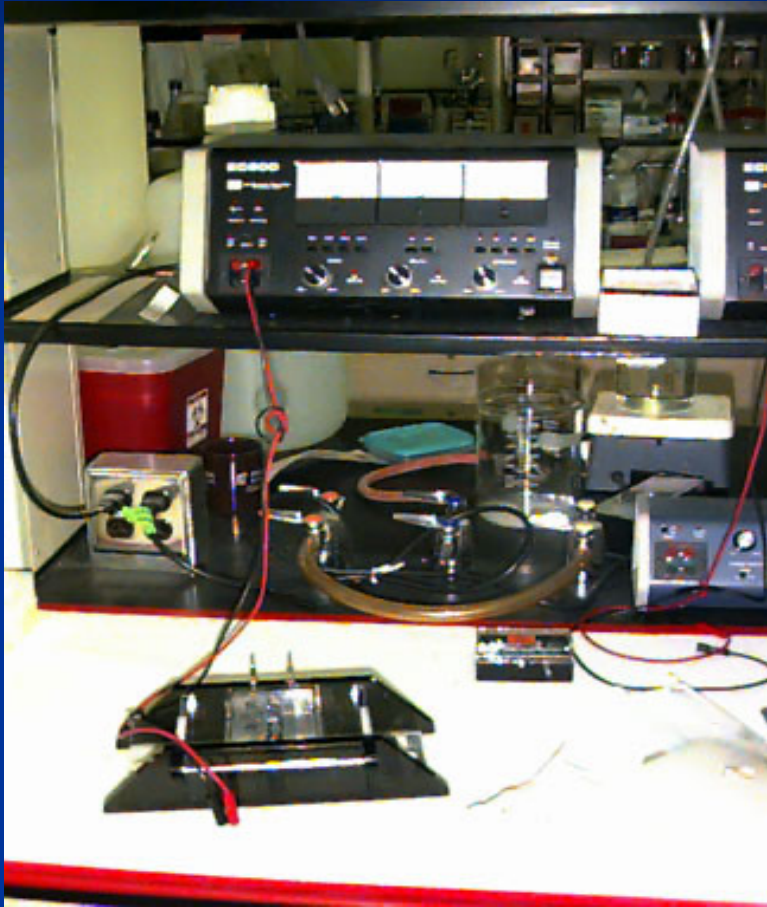


DNA Experiment Set-up

Ingredients and tools needed:

- DNA strands that encode city names and connections between them
- Ligase, water, salt, other ingredients
- Polymerase chain reaction (PCR) set
- Gel electrophoresis tool (that filters out non-solution strands)

Gel Electrophoresis



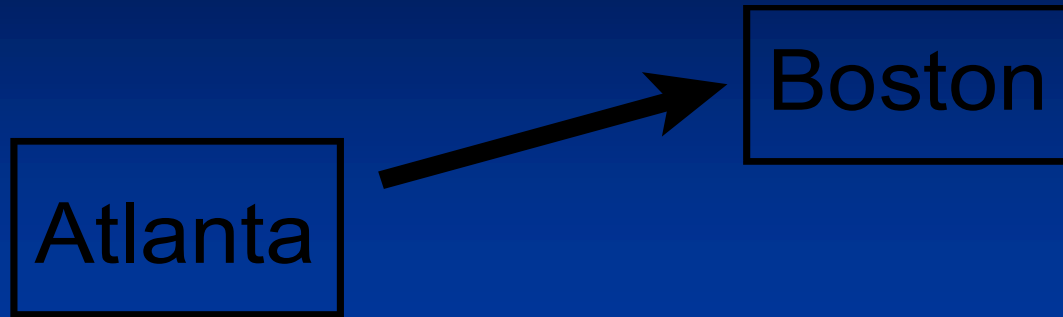
<http://www.life.uiuc.edu/molbio/geldigest/equipment.html>



CITY	DNA NAME	COMPLEMENT
ATLANTA	ACTT <i>GCAG</i>	TGAACGTC
BOSTON	TCGG <i>ACTG</i>	AGCCTGAC
CHICAGO	GGCTATGT	CCGATACA
DETROIT	CCGAGCAA	GGCTCGTT

CONNECTING PATH	DNA PATH
ATLANTA-BOSTON	<i>GCAGTCGG</i>
ATLANTA-DETROIT	GCAGCCGA
BOSTON-CHICAGO	ACTGGGCT
BOSTON-DETROIT	ACTGCCGA
BOSTON-ATLANTA	ACTGACTT
CHICAGO-DETROIT	ATGTCCGA

DNA encoding of city-network



Atlanta -Boston

GCAGTCGG

TGAACGTC **AGCCTGAC**

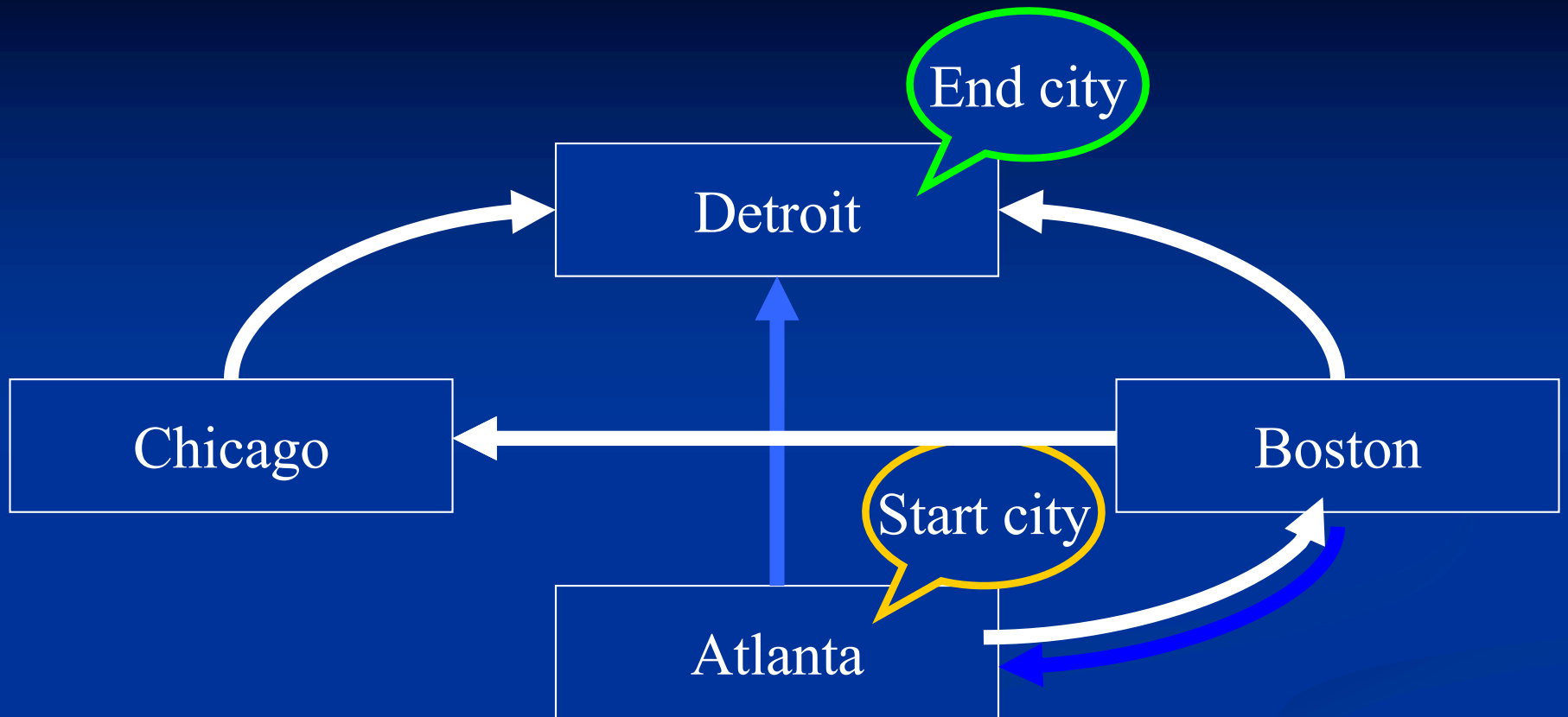
Atlanta

Boston



Atlanta-Boston	Boston-Chicago	Chicago-Detroit
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Atlanta*	Boston*	Chicago*	Detroit*
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Boston-Atlanta	Atlanta-Detroit
----------------	-----------------

Boston*	Atlanta*	Detroit*
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Adleman's DNA Experiment

- 1. In a test tube, mix the prepared DNA pieces together
 - Which will randomly link with each other, forming all different paths.
 - Ligase will heal nicks between consecutive cities, allowing each path to be a DNA strand (representing a possible Hamiltonian path) .

Adleman's DNA Experiment

- 2. Perform PCR with two 'start' and 'end' DNA pieces as primers
 - Which creates many copies of each DNA strand (representing a possible Hamiltonian path) with the correct start and end.

Adleman's DNA Experiment

- 3. Perform gel electrophoresis to identify only those pieces of right length (e.g., $N=4$).

- 4. For each city:
 - Use DNA-attached magnetic probe separation to separate out the DNA sequences that contain that city.
 - These magnetic probes are magnetic nanoparticles with an attached DNA strand that is complementary to the given city.
 - Discard the DNA sequences that do not contain that city.

- 5. All DNA pieces that are left in the final test tube should be precisely those representing Hamiltonian paths.
 - If the final test tube contains any DNA at all, then conclude that a Hamiltonian path exists, and otherwise not.
 - When it does, the DNA sequence represents the specific path of the solution.

4. SUMMARY & CONCLUSION

- **Enormous parallelism,**
 - with 10^{23} DNA pieces working in parallel to find solution simultaneously.
 - Takes less than a week (vs. thousands yrs for supercomputer)
- **Extraordinary energy efficient**
 - (10^{-10} of supercomputer energy use)
- **But limited by exponential size growth of amount of DNA needed**

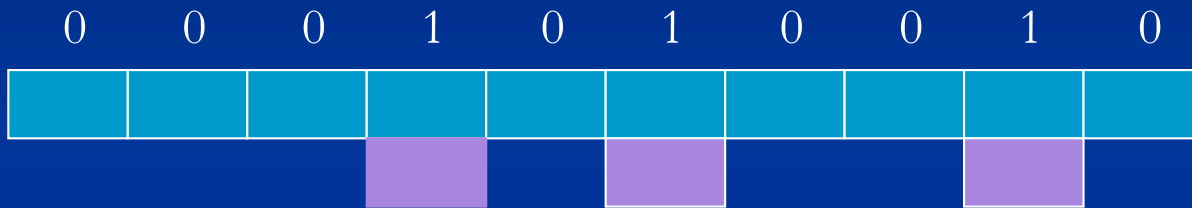
New generation of computers?

- In the second part of [1], it is proven through language theory that DNA computing “guarantees universal computations”.
- Many architectures have been invented for DNA computations.
- The Adleman experiment is not the single application case of DNA computing...

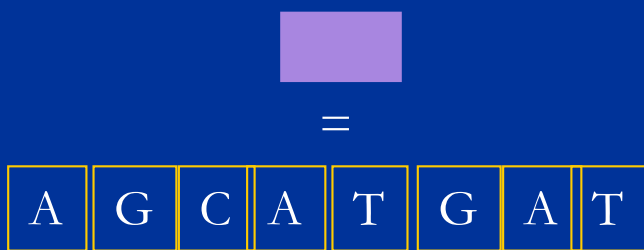
Stickers model:

- Memory complex = Strand of DNA (single or semi-double).
- Stickers are segments of DNA, that are composed of a certain number of DNA bases.
- To use correctly the stickers model, each sticker must be able to anneal only at a specific place in the memory complex.

To visualize:

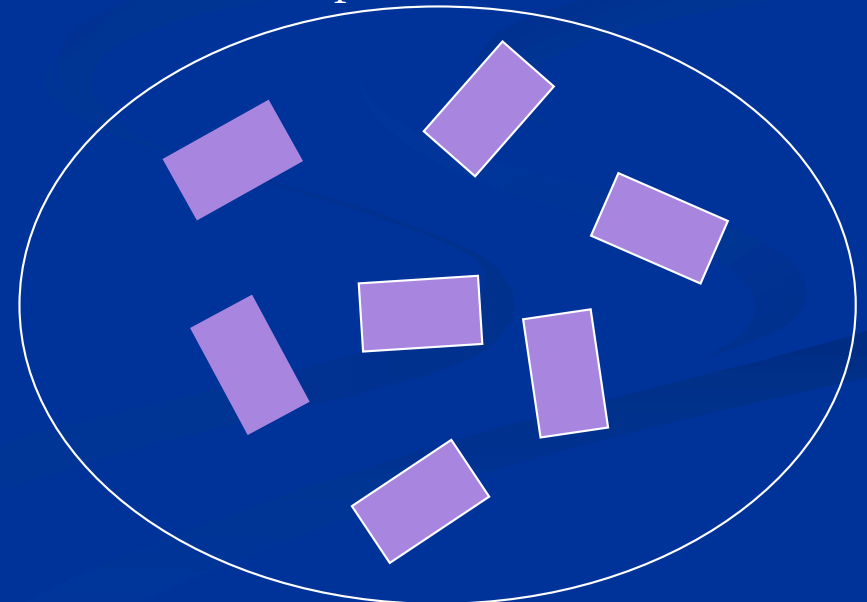


Memory complex:
Semi-double



←
Zoom

Soup of stickers:



About a stickers machine?

- Simple operations: merge, select, detect, clean.
- → Tubes are considered (cylinders with two entries)
- However for a mere computation (DES):
 - Great number of tubes is needed (1000).
 - Huge amount of DNA needed as well.
- Practically no such machine has been created....
 - Too much engineering issues.

Why don't we see DNA computers everywhere?

- DNA computing has wonderful possibilities:
 - Reducing the time of computations* (parallelism)
 - Dynamic programming !
- However one important issue is to find “the killer application”.
- Great hurdles to overcome...

Some hurdles:

- Operations done manually in the lab.
- Natural tools are what they are...
 - Formation of a library (statistic way)
 - Operations problems

Conclusion:

- The paradigm of DNA computing has led to a very important theoretical research.
- However DNA computers won't flourish soon in our daily environment due to the technological issues.
- Adleman's renouncement toward electronic computing.
- Is all this work lost ?
- NO ! → "Wet computing"